



#### 4.3 Footings



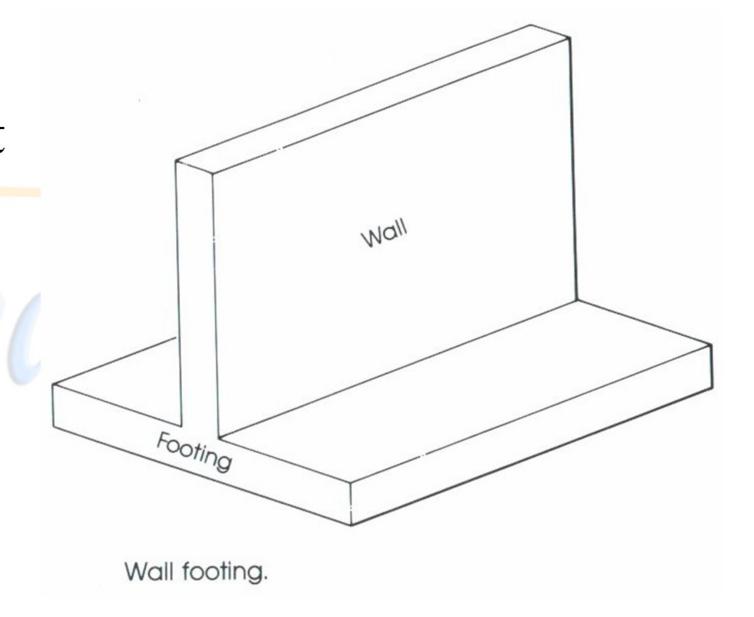
#### **Definition**

Footings are structural members used to support columns and walls and to transmit and distribute their loads to the soil in such a way that the load bearing capacity of the soil is not exceeded, excessive settlement, differential settlement, or rotation are prevented and adequate safety against overturning or sliding is maintained.





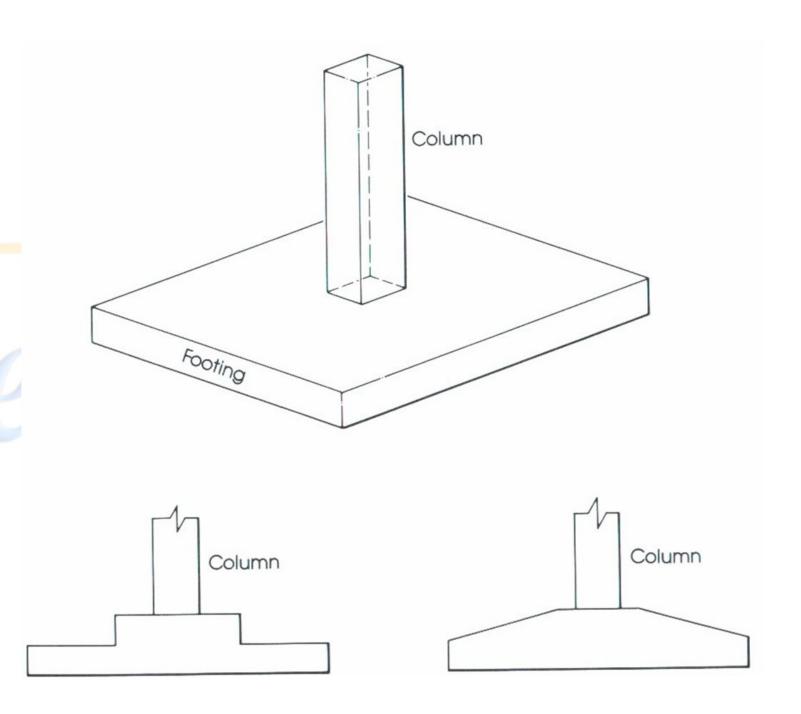
Wall footings are used to support structural walls that carry loads for other floors or to support nonstructural walls.







Isolated or single footings are used to support single columns. This is one of the most economical types of footings and is used when columns are spaced at relatively long distances.

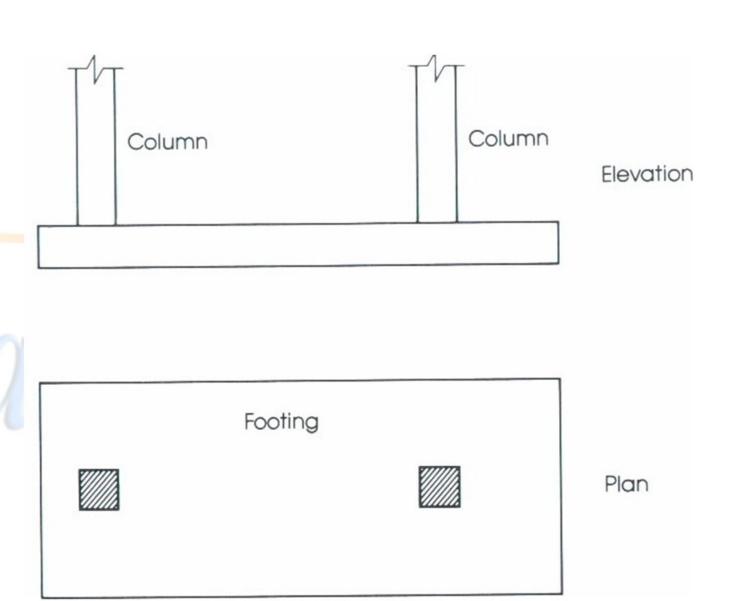






Combined footings usually support two columns, or three columns not in a row.

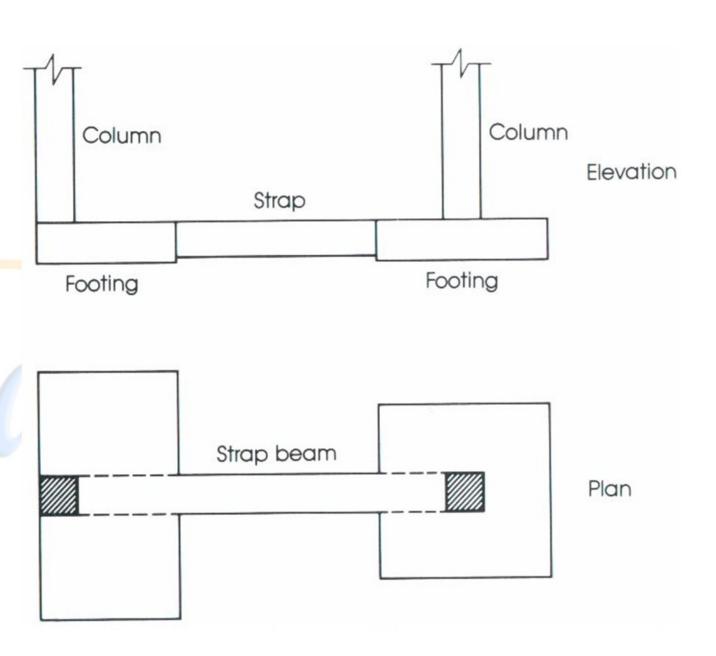
Combined footings are used when two columns are so close that single footings cannot be used or when one column is located at or near a property line.







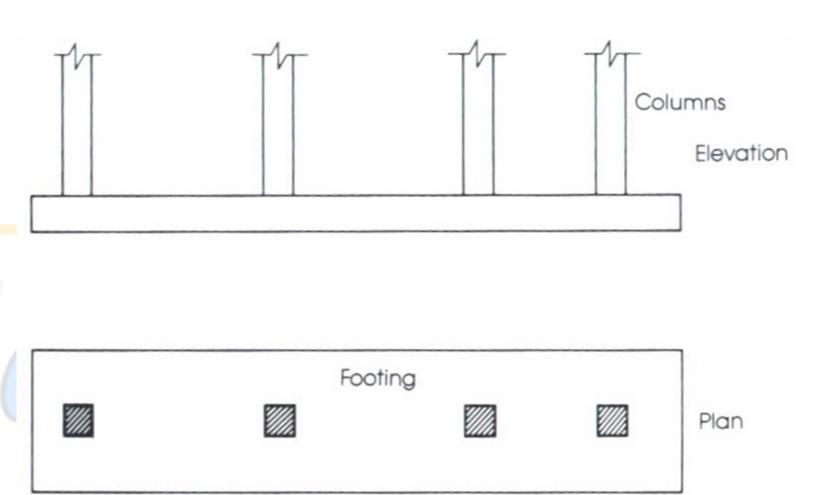
Cantilever or strap footings consist of two single footings connected with a beam or a strap and support two single columns. This type replaces a combined footing and is more economical.







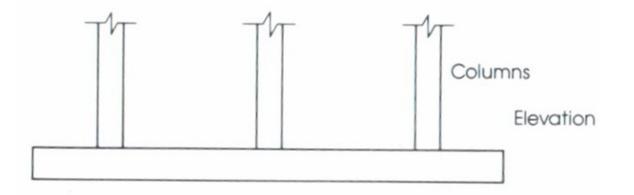
Continuous footings
support a row of three or
more columns. They have
limited width and continue
under all columns.

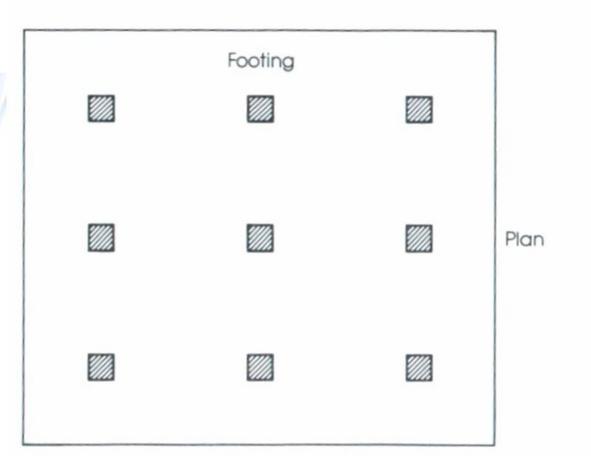






Rafted or mat foundation consists of one footing usually placed under the entire building area. They are used, when soil bearing capacity is low, column loads are heavy, single footings cannot be used, piles are not used and differential settlement must be reduced.

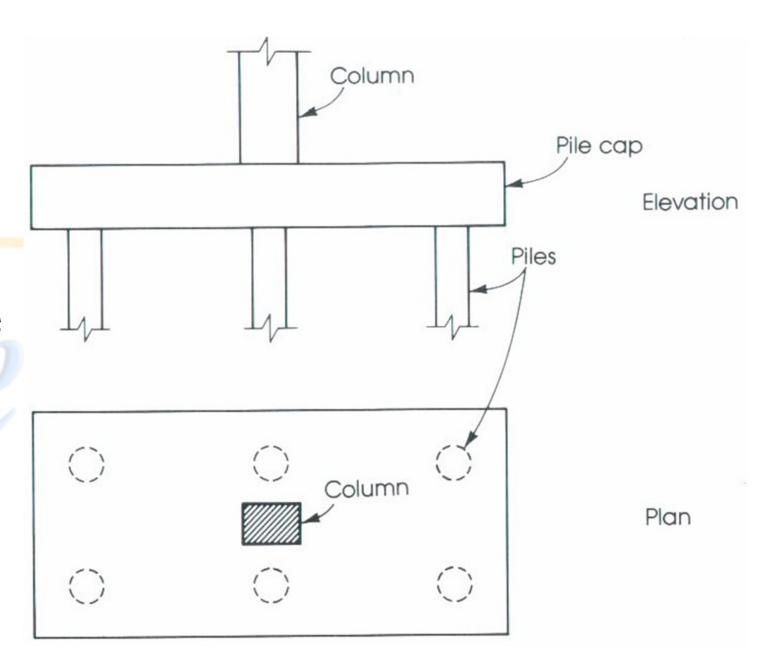








Pile caps are thick slabs used to tie a group of piles together to support and transmit column loads to the piles.

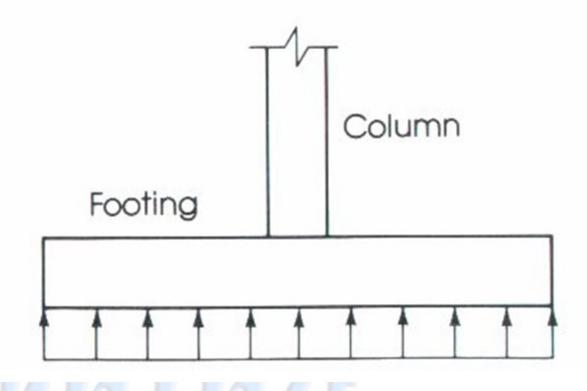




#### **Sewlearning** Distribution of Soil Pressure



When the column load P is applied on the centroid of the footing, a uniform pressure is assumed to develop on the soil surface below the footing area.



However the actual distribution of the soil is not uniform, but depends on many factors especially the composition of the soil and degree of flexibility of the footing.



#### Design Considerations



Footings must be designed to carry the column loads and transmit them to the soil safely while satisfying code limitations.

- 1. The area of the footing based on the allowable bearing soil capacity
- 2. Two-way shear or punch out shear.
- 3. One-way wide beam shear
- 4. Bending moment and steel reinforcement required



#### Size of Footings



The area of footing can be determined from the actual external loads such that the allowable soil pressure is not exceeded.

Strength design requirements

$$q_{\rm u} = \frac{P_{\rm u}}{\text{area of footing}}$$

#### SeglearTiwg-Way Shear (Punching Shear)



For two-way shear in slabs (& footings) V<sub>c</sub> is smallest of

$$V_{\rm c} = \left(1 + \frac{2}{\beta_{\rm c}}\right) \frac{\sqrt{f_{\rm c}}}{6} b_0 d$$
 ACI 11-31

where,  $\beta_c$  = long side/short side of column concentrated load or reaction area < 2

b<sub>0</sub> = length of critical perimeter around the column

When  $\beta_c > 2$  the allowable  $V_c$  is reduced.

#### Seolearning Design of two-way shear



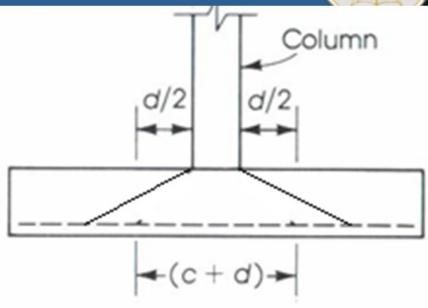


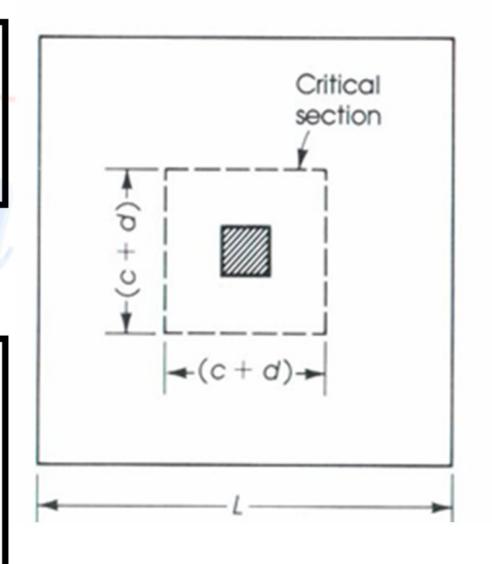
$$b_0 = 4(c+d)$$

for square columns where one side = c

$$b_0 = 2(c_1+d) + 2(c_2+d)$$

for rectangular columns of sides  $c_1$  and  $c_2$ .



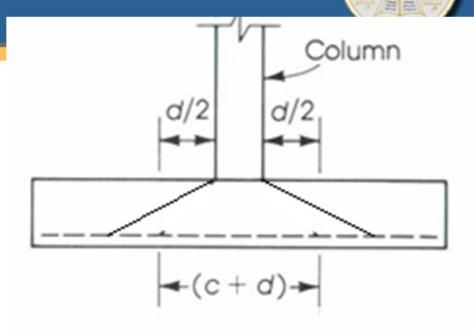


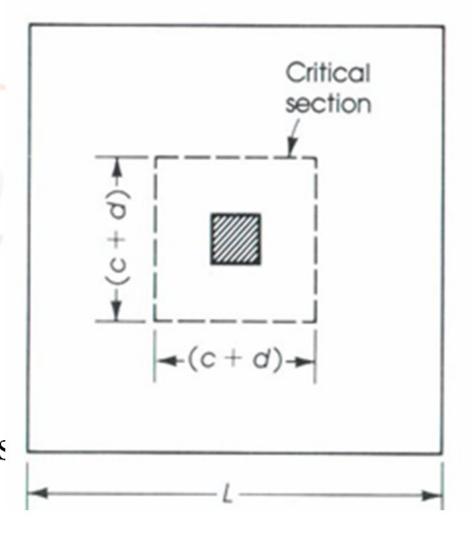
# eolearning Design of two-way shear

3. The shear force  $V_{11}$  acts at a section that has a length  $b_0 = 4(c+d) \text{ or } 2(c_1+d) + 2(c_2+d)$ and a depth d; the section is subjected to a vertical downward load P<sub>11</sub> and vertical upward pressure q<sub>11</sub>.

$$V_{\rm u} = P_{\rm u} - q_{\rm u} (c+d)^2 \text{ for square columns}$$

$$V_{\rm u} = P_{\rm u} - q_{\rm u} (c_1+d)(c_2+d) \text{ for rectangular columns}$$





#### Seglearning Design of two-way shear



4. Allowable 
$$\phi V_c = \phi \frac{\sqrt{f_c}}{3} b_0 d$$

Column
$$d/2$$

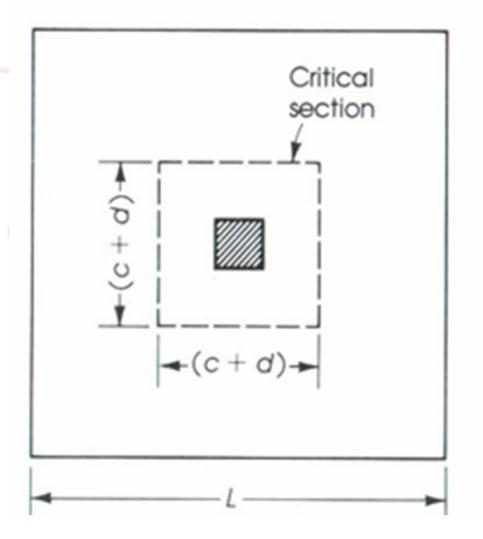
$$d/2$$

$$+(c+d)+$$

Let 
$$V_u = \phi V_c$$

$$d = \frac{3V_u}{\phi \sqrt{f_c} b_0}$$

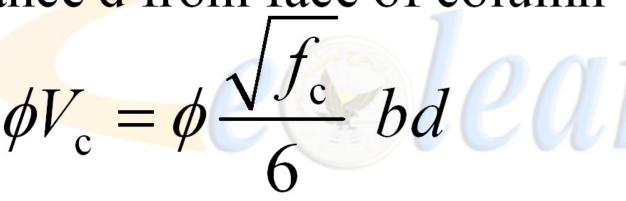
If d is not close to the assumed d, revise your assumptions

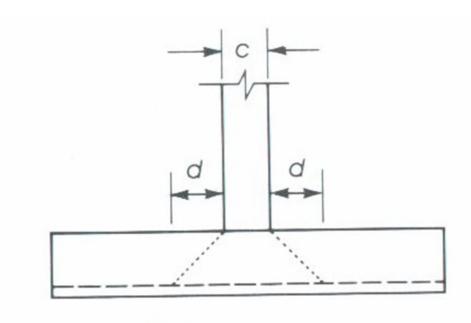


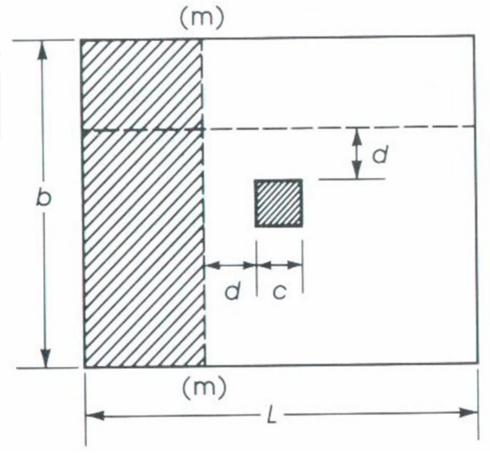
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### Seolearning Design of one-way shear

For footings with bending action in one direction the critical section is located a distance d from face of column





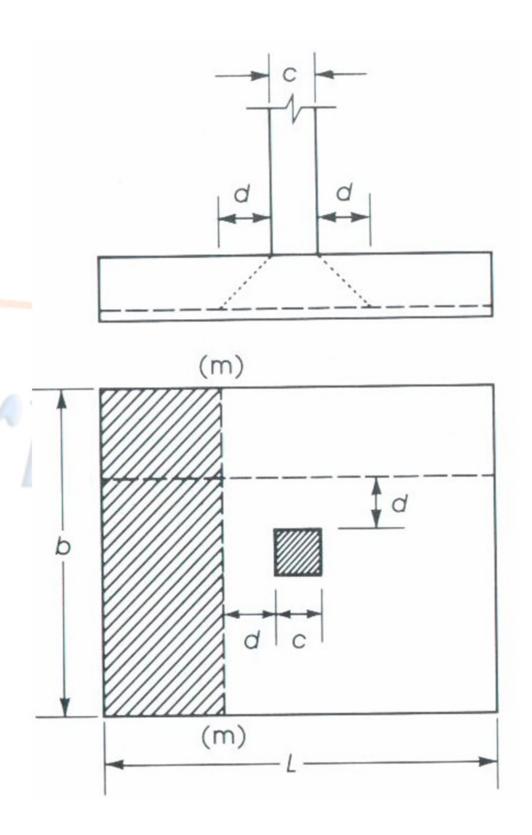


### Seolearning Design of one-way shear



The ultimate shearing force at section m-m can be calculated

$$V_{\mathbf{u}} = q_{\mathbf{u}} b \begin{pmatrix} L & c \\ \frac{L}{2} - \frac{c}{2} - d \\ 2 & 2 \end{pmatrix}$$

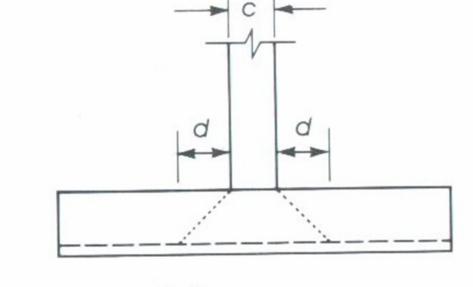




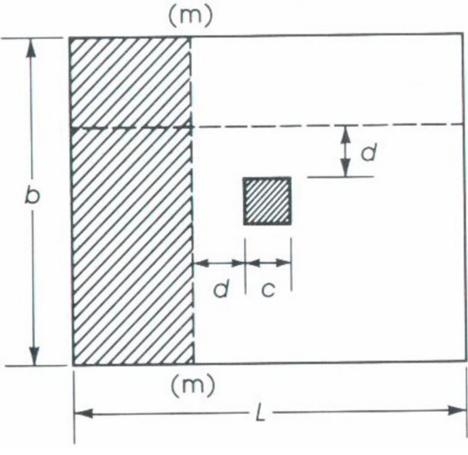
# Ceolearning Design of one-way shear



If no shear reinforcement is to be used, then d can be checked, assuming  $V_{11} = \phi V_{c}$ 

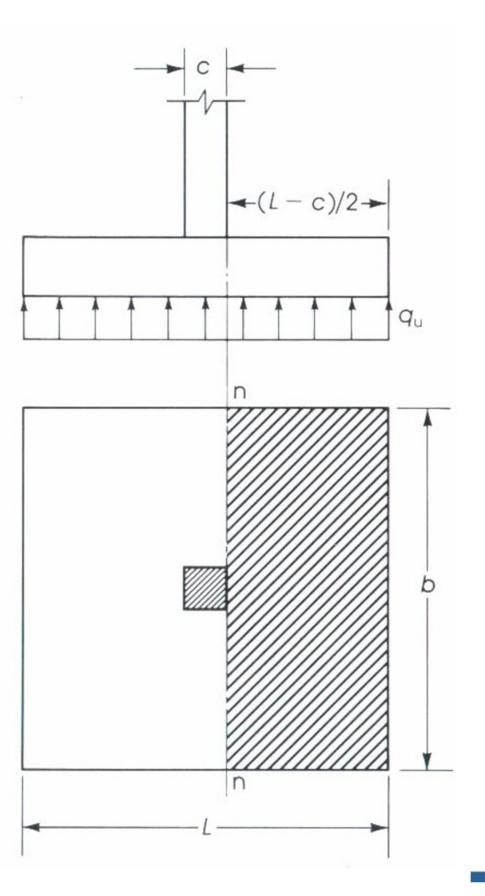


$$d = \frac{6V_{\rm u}}{\phi \sqrt{f_{\rm c}} b}$$



The bending moment in each direction of the footing must be checked and the appropriate reinforcement must be provided.

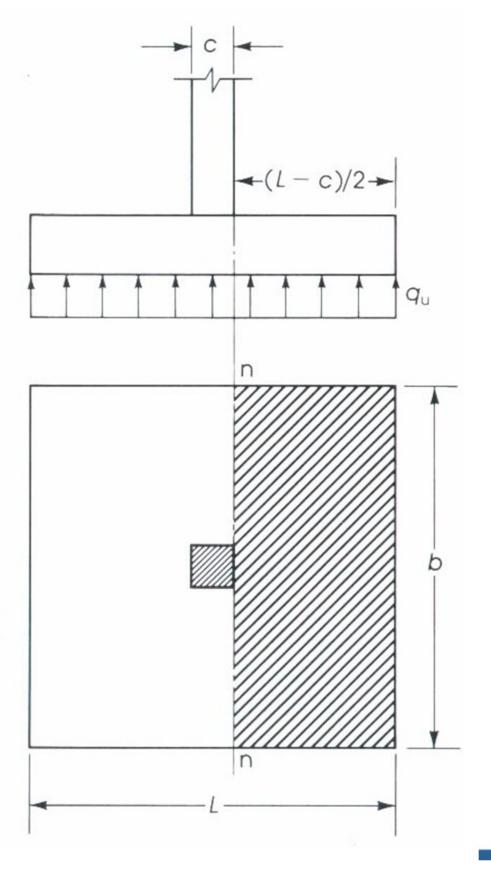
$$A_{\rm s} = \frac{3M_{\rm u}}{d}$$



#### Celexural Strength and Footing reinforcemen

The minimum steel percentage required shall be as required for shrinkage temperature reinforcement.







#### Problem set #5



- Design a panel 4m by 5m supported on four columns.
  - Design the slab as one-way rib in the 4m direction. The superimposed load is 3kN/m<sup>2</sup>, the live load is 3kN/m<sup>2</sup>
  - Design the beam, column and isolated footing to support four stories, concrete is B250.
  - Soil allowable bearing capacity is 350kN/m<sup>2</sup>





## End of chapter 4

Let Learning Continue

