

elearning Beams: 4.2.1 Flexure

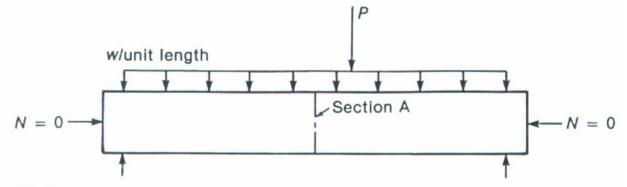


The beam is a structural member used to support the internal moments and shears. It would be called a beam-column if a compressive force existed.

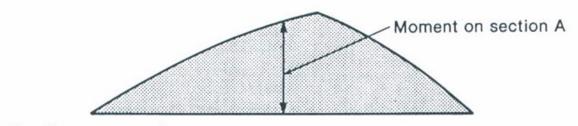
$$C = T$$

$$M = C*(jd)$$

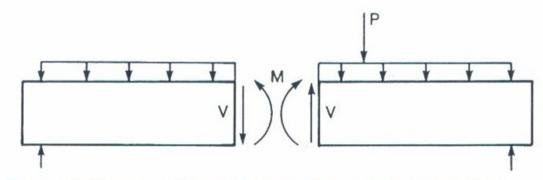
$$= T*(jd)$$



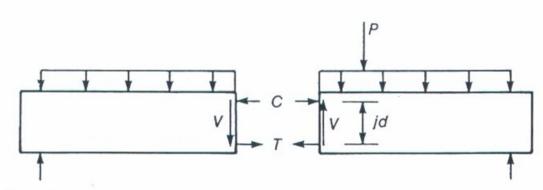
(a) Beam.



(b) Bending moment diagram.



(c) Free body diagrams showing internal moment and shear force.



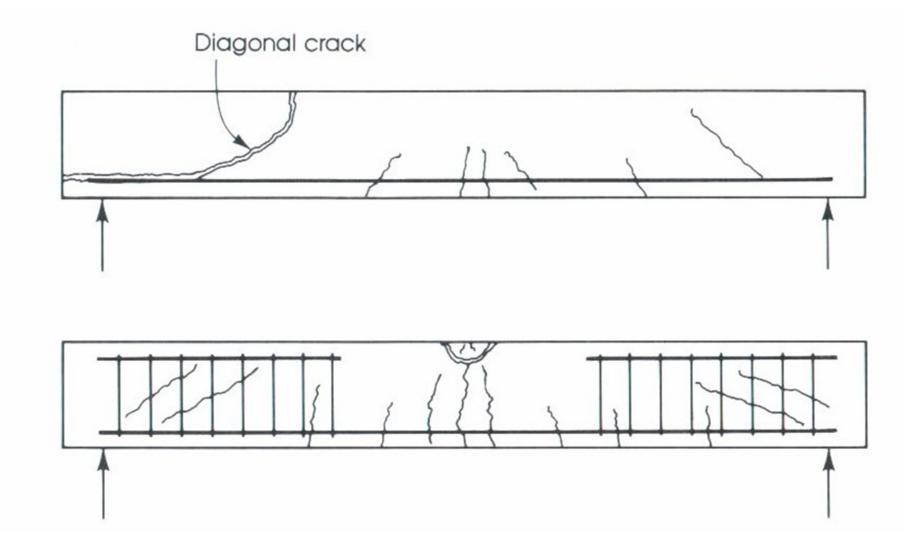
(d) Free body diagrams showing internal moment as a compression-tension force couple.



Flexure



The first beam fails in shear, the second fails in bending moment.





Approximate analysis



- Use of tributary area (area of floor or roof which supports all of the loads whose load path leads to the beam) determines the beam load.
- Perform approximate analysis through:
 - Approximate deflected shape to locate points of inflection, hence transform to determinate beam and analyze using statics.
 - Use analysis coefficients (e.g. ACI coefficients)
 - Use finite element programs



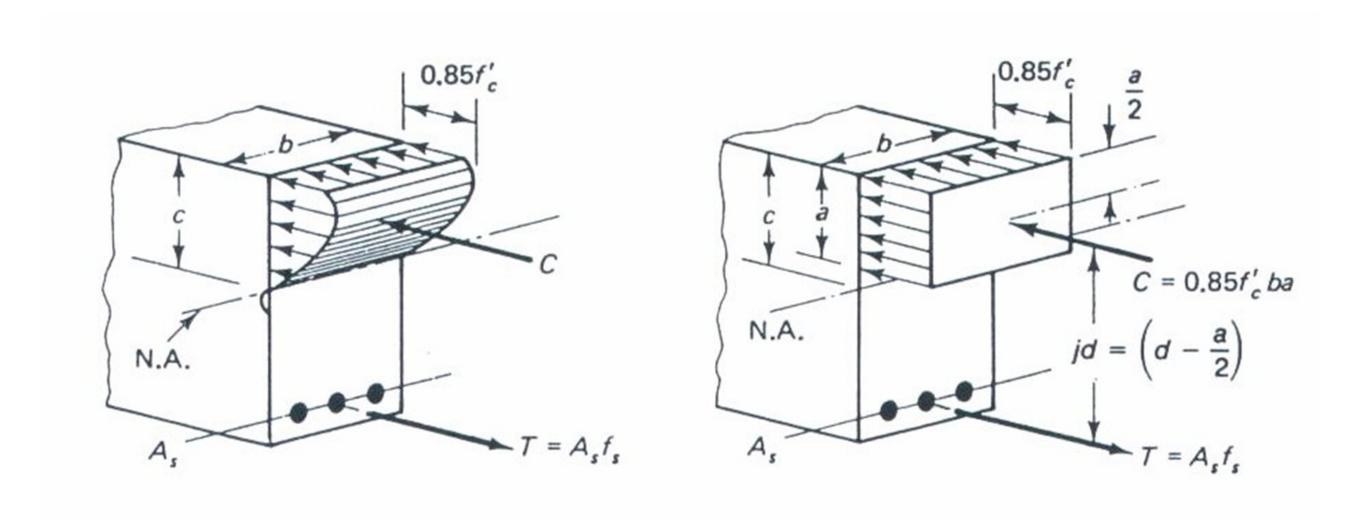
Basic Assumptions in Flexure Theory

- Plane sections remain plane (not true for deep beams h > 4b)
- The strain in the reinforcement is equal to the strain in the concrete at the same level, i.e. $\varepsilon_s = \varepsilon_c$.
- Stress in concrete & reinforcement may be calculated from the strains using f-\varepsilon curves for concrete & steel.
- Tensile strength of concrete is neglected.
- Concrete is assumed to fail in compression, when $\varepsilon_c = 0.003$
- Compressive f-\varepsilon relationship for concrete may be assumed to be any shape that results in an acceptable prediction of strength.

Seolearning Design for Flexure: review



The compressive zone is modeled with an equivalent stress block.



Seolearning Design for Flexure: review



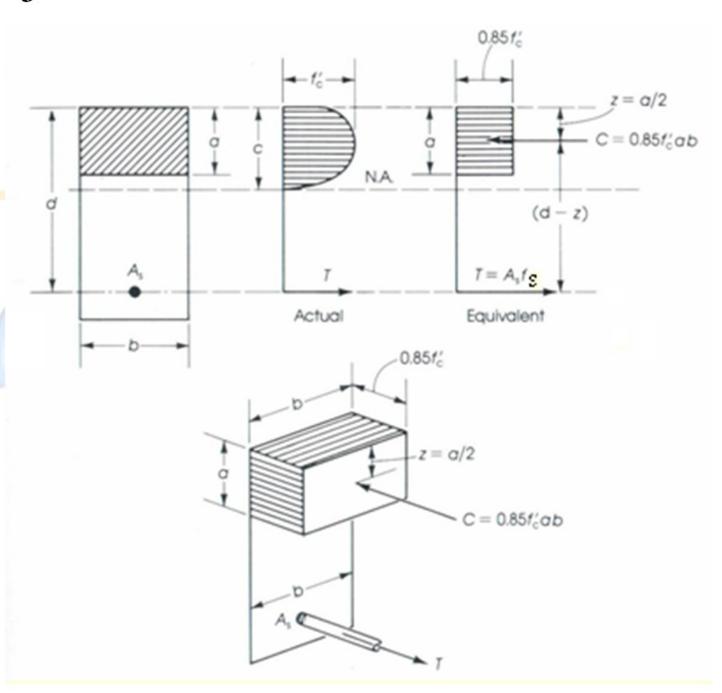
Example of rectangular reinforced concrete beam.

Setup equilibrium.

$$\sum F_{\rm x} = 0 \implies T = C$$

$$A_{\rm s}f_{\rm s}=0.85f_{\rm c}ab$$

$$\sum M = 0 \implies T\left(d - \frac{a}{2}\right) = M_n$$





Design for Flexure: review



The ultimate load, which is used in the design and analysis of the structural member is:

$$M_{\rm u} = \phi M_{\rm n}$$

M_u – Ultimate Moment

M_n – Nominal Moment

Φ – Strength Reduction Factor

The strength reduction factor, Φ , varies depending on the tensile strain in steel in tension. Three possibilities:

Compression Failure - (over-reinforced beam)

Tension Failure - (under-reinforced beam)

Balanced Failure - (balanced reinforcement)

Seolearning Design for Flexure: review



Which type of failure is the most desirable?

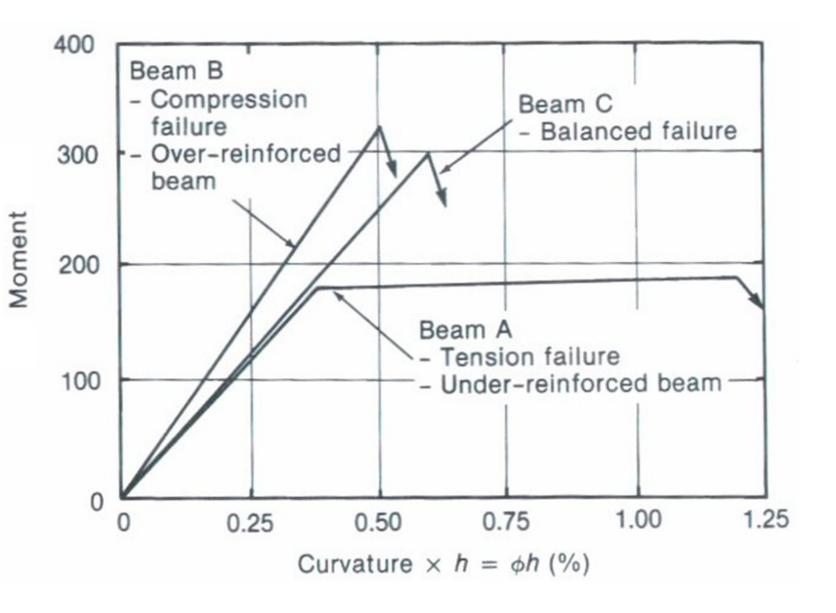
The *under-reinforced* beam is the most desirable.

$$f_s = f_y$$

$$\varepsilon_s >> \varepsilon_y$$

You want ductility

system deflects and still carries load.



PeolApproximate Design for Flexure: J



For under-reinforced, the equation can be rewritten as:

$$C = T \implies 0.85 f_{c}' ba = A_{s} f_{y}$$

$$a = \frac{f_{y}A_{s}}{0.85f_{c}'b}$$

$$a = \frac{f_{y}A_{s}}{0.85f_{c}'b}$$

$$M_{n} = A_{s}f_{y}d\left(1 - \frac{f_{y}A_{s}}{1.7f_{c}'bd}\right)$$

$$M_{\rm d} = \phi M_{\rm n} = A_{\rm s} d\phi f_{\rm y} \left(1 - \frac{\rho f_{\rm y}}{1.7 f_{\rm c}'} \right) = A_{\rm s} dj$$

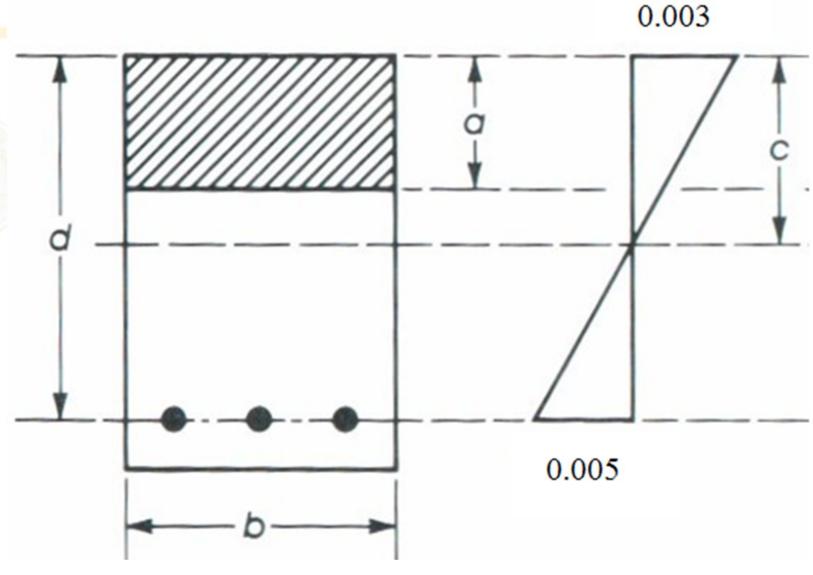
Celapproximate Design for Flexure: J



 ρ_{max} = maximum ρ value recommended to get simultaneous ϵ_c = 0.003 & ϵ_s = 0.005

Use similar triangles:

$$\frac{0.003}{c} = \frac{0.005}{d-c}$$



CeolApproximate Design for Flexure: J



For a yield stress 420MPa, the equation can be rewritten to find c as

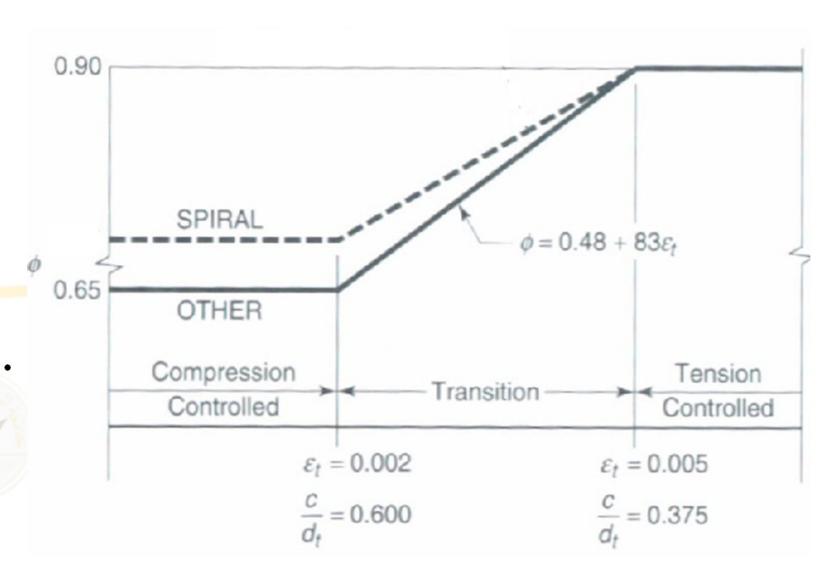
$$c = \frac{0.003d}{0.008}$$
 $\Rightarrow c = 0.375d$
 $a = 0.85c = 0.319d$
 $\rho = 0.271f'_{c}/f_{y}$

: J (

13 / 67

Approximate Design for Flexure: J

The strength reduction factor, ϕ , will come into the calculation of the strength of the beam.



e learnin The factor J for large steel ratios

$$M_{\rm d} = \phi M_{\rm n} = A_{\rm s} d\phi f_{\rm y} \left(1 - \frac{\rho f_{\rm y}}{1.7 f_{\rm c}'} \right) = A_{\rm s} dj$$

$$j = \phi f_{y} \left(1 - \frac{\rho f_{y}}{1.7 f_{c}'} \right)$$

• For concrete strength variation 20MPa to 42Mpa, the value of J for maximum recommended steel ratio varies is 0.317. Moment in kN.m, area of steel in square cm and depth in cm.

Collumitations on Reinforcement Ratio

15 / 67

Lower Limit on ρ ACI 10.5.1

$$A_{\text{s(min)}} = \frac{\sqrt{f_{\text{c}}'}}{4f_{\text{v}}} * b_{\text{w}} d \ge \frac{1.4}{f_{\text{v}}} * b_{\text{w}} d$$
 ACI Eqn. (10-3)

f_c & f_y are in MPa

Lower limit used to avoid "Piano Wire" beams.

Very small As $(M_n < M_{cr})$

Strain in steel is huge (large deflections)

when beam cracks ($M_u/\Phi > M_{cr}$) beam fails right away because nominal capacity decreases drastically.

$$j = \phi f_{y} \left(1 - \frac{\rho f_{y}}{1.7 f_{c}'} \right) = \phi f_{y} \left(1 - \frac{1.4}{1.7 f_{c}'} \right)$$

• For concrete strength variation 20MPa to 42Mpa, the value of J for minimum steel varies from 0.36 to 0.37



The factor J



• It is obvious that variation of J is not sensitive to changes in concrete strength. Thus a mean value of 0.33 is representative for all types of concrete used in Palestine (B250-B500)

$$M_d = \frac{A_s d}{3}$$

Temperature & Shrinkage reinforcement in structural slabs and footings (ACI 7.12) place perpendicular to direction of flexural reinforcement.

GR 40 or GR 50 Bars:
$$A_s$$
 (T&S) = 0.0020 A_g

$$A_s (T&S) = 0.0018 A_g$$

 $A_{\rm g}$ - Gross area of the concrete





End of 4.2.7

Let Learning Continue





4.2.2 Beams: serviceability



Beam Depths

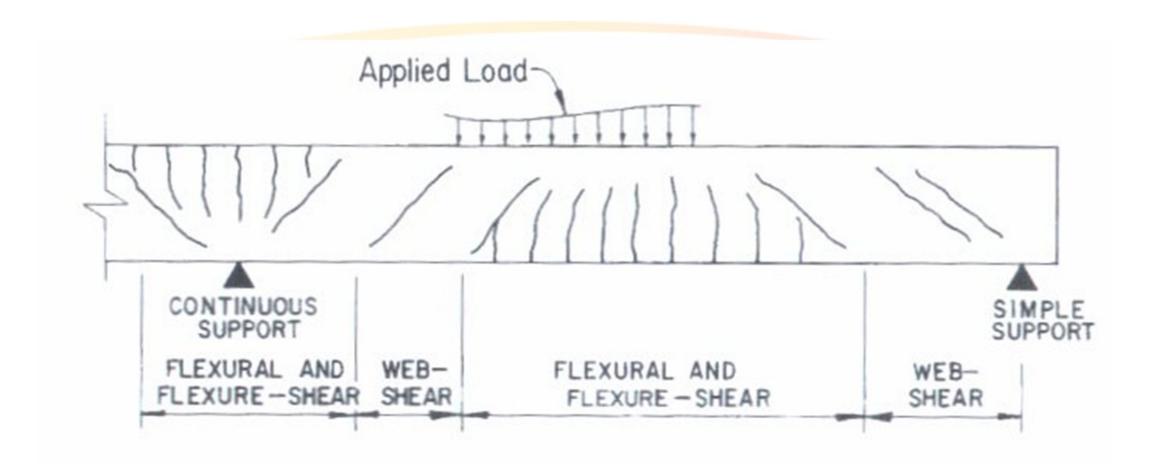
- ACI 318 Table 9.5(a) min. h based on span (slab & beams)
- •Design for max. moment over a support to set depth of a continuous beam.



4.2.3 Shear



Typical Crack Patterns for a deep beam.





Shear Design: review



Shear Strength (ACI 318 Sec 11.1)

$$\phi V_n \ge V_u$$

capacity \geq demand $\phi = 0.75$ (shear) – strength reduction factor

$$V_n = V_c + V_s$$

 $V_c = \frac{\sqrt{f_c'}}{\zeta} b_w d=$ Nominal shear resistance provided by concrete

 $V_{\rm s}$ = Nominal shear resistance provided by the shear reinforcement

11.4.6.1 — A minimum area of shear reinforcement, $A_{v,min}$, shall be provided in all reinforced concrete flexural members (prestressed and nonprestressed) where V_u exceeds $0.5\phi V_c$, except in members satisfying one or more of (a) through (f):

23 / 67

- (a) Footings and solid slabs;
- (c) Concrete joist construction defined by 8.13;
- (d) Beams with h not greater than 250 mm;
- (e) Beam integral with slabs with h not greater than 600 mm and not greater than the larger of 2.5 times thickness of flange, and 0.5 times width of web;

24 / 67

Seglearni Approximate design for shear

eolearning

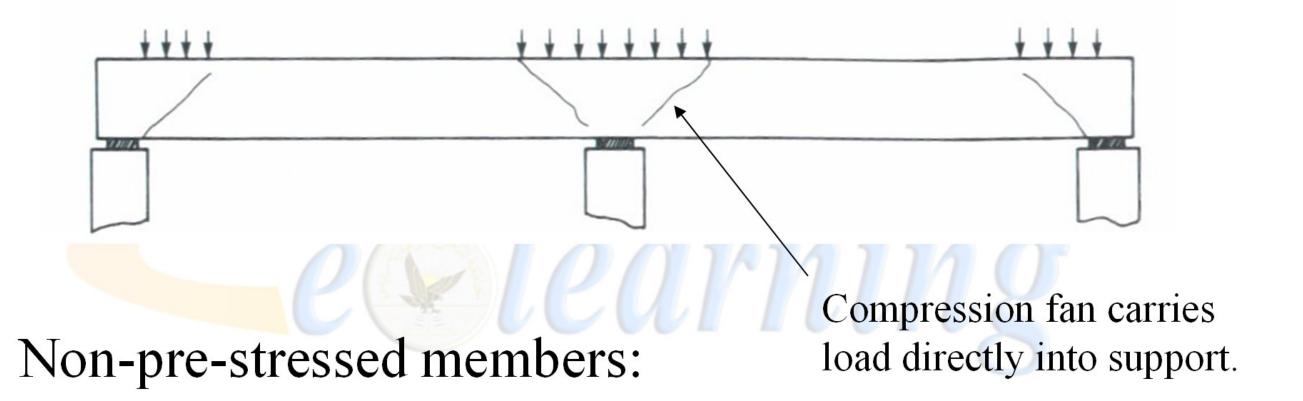
Better to use

$$V_u < 0.5\phi \sqrt{f_c'} b_w d$$

Hence

$$s_{\text{max}} \le \frac{d}{2} \le 60cm$$





Sections located less than a distance d from face of support may be designed for same shear, V_u , as the computed at a distance d.

When:

- 1. The support reaction introduces <u>compression</u> into the end regions of the member.
- 2. The loads are applied at or near the top of the beam.
- 3. No concentrated load occurs with in d from face of support.

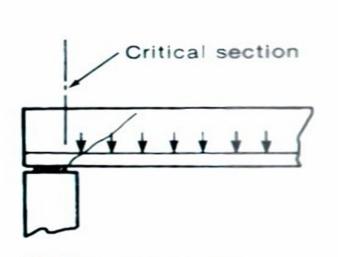


Ceolearning Shear Design: review/ max hear

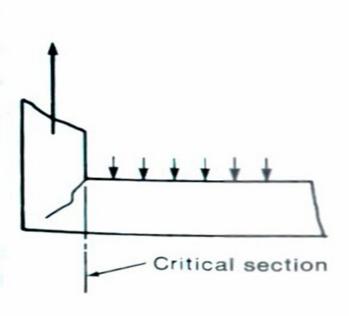


Critical sections

Girder

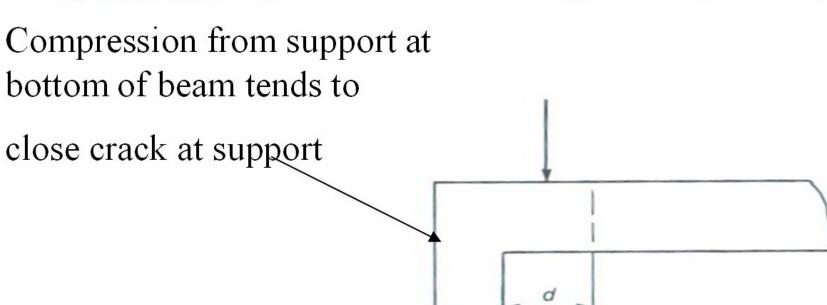


(a) Beam loaded on tension flange.



Critical sections

(b) Beam column joint.



(d) Beam supported by tension force.

(e) Beam with concentrated load close to support.

Beam

Hanger

reinforcement

(c) Beam supported by shear.



eolearning 4.2.4 Development Length



12.2.1 — Development length for deformed bars and deformed wire in tension, ℓ_d , shall be determined from either 12.2.2 or 12.2.3 and applicable modification factors of 12.2.4 and 12.2.5, but ℓ_d shall not be less than 300 mm.

12.2.2 — For deformed bars or deformed wire, \(\ell_d\) shall be as follows:

Spacing and cover	No. 19 and smaller bars and deformed wires	No. 22 and larger bars
Clear spacing of bars or wires being developed or spliced not less than d_b , clear cover not less than d_b , and stirrups or ties throughout ℓ_d not less than the Code minimum or Clear spacing of bars or wires being developed or spliced not less than $2d_b$ and clear cover not less than d_b	$\left(\frac{I_{y}\psi_{t}\psi_{o}}{2.1\lambda\sqrt{I_{o}^{\prime}}}\right)d_{b}$	$\left(\frac{I_y \psi_t \psi_o}{1.7 \lambda_s / I_o^{\prime\prime}}\right) d_b$
Other cases	$\left(\frac{f_y\psi_t\psi_o}{1.4\lambda\sqrt{f_o'}}\right)d_b$	$\left(\frac{f_y \psi_t \psi_o}{1.1 \lambda \sqrt{f_o'}}\right) d_b$

12.2.3 — For deformed bars or deformed wire, ℓ_d shall be

$$\ell_d = \left(\frac{f_y}{1.1\lambda \sqrt{f_c'}} \frac{\psi_t \psi_\theta \psi_s}{\left(\frac{c_b + K_{tr}}{d_b}\right)}\right) d_b \qquad (12-1)$$

in which the confinement term $(c_b + K_{tr})/d_b$ shall not be taken greater than 2.5, and

$$K_{tr} = \frac{40A_{tr}}{sn} \tag{12-2}$$

where n is the number of bars or wires being spliced or developed along the plane of splitting. It shall be permitted to use $K_{tr} = 0$ as a design simplification

- (a) Where horizontal reinforcement is placed such that more than 300 mm of fresh concrete is cast below the development length or splice, $\psi_t = 1.3$. For other situations, $\psi_t = 1.0$.
- (c) For No. 19 and smaller bars and deformed wires, $\psi_s = 0.8$. For No. 22 and larger bars, $\psi_s = 1.0$.

Seglearning 4.2.5 Bar Splices in tension



Why do we need bar splices? -- for long spans

Types of Splices

- 2. Mechanical Connectors
- 3. Lab Splices



Types of Splices



Class A Splice

(ACI

When
$$\frac{A_{\text{s(provided)}}}{A_{\text{s(req'd)}}} \ge 2$$
 over entire splice length.

and 1/2 or less of total reinforcement is spliced within the req'd lap length.



Types of Splices



Class B Splice

(ACI

12.15.2)

All tension lab splices not meeting requirements of Class A Splices

32/67

Seglearn Tension Lap Splice (ACI 12.15)



As,prov/As,req'd	%As Spliced	Splice Class	Lap, req'd	Notes
	≤ 50	A	l_d	Desirable
≥ 2.0				
	> 50	В	1.3 l _d	ok
	≤ 50	В	1.3 l _d	ok
< 2.0				
	> 50	В	1.3 l _d	Avoid

where $A_{s (req'd)}$

= determined for bending

development length for bars (not allowed to use excess reinforcement modification factor)

l_d must be greater than or equal to 30cm

Lab Splices should be placed in away from regions of high tensile stresses -locate near points of inflection (ACI R12.15.2)



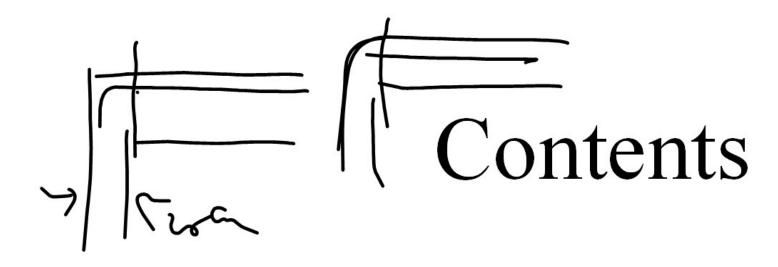


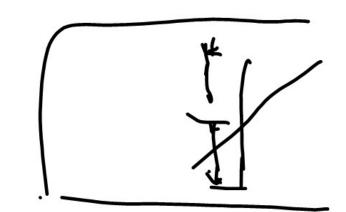
End of 4.2.2-5

Let Learning Continue

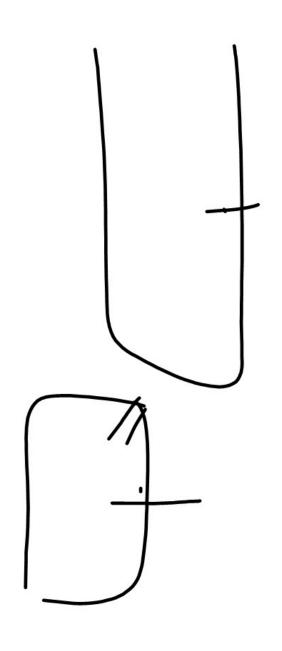


Innovations in Slab Systems Voided Slab Technology





- INTRODTION
- <u>SLAB PERFORMANCE REQUIREMENTS</u>
- CHARACTERISTICS OF <u>INNOVATIVE DESIGN</u>
- HISTORY OF VOIDED SLABS IN PALESTINE
- THEORETICAL COMPARISIONS
- TYPES OF VOIDED SLABS
- <u>EXAMP</u>ELS
- CONCLSION



مقدمة INTRODTION

- -Conceptually a good design only if (LL/DL<1)
- -DL increases with span in RC structures
- -Solutions:
 - -Avoid tension in selection of structural systems (dome, arch, ...)
 - -Prestressed concrete
 - -Voided slab

-...

SLAB PERFORMANCE REQUIREMENTS

Structure

- 1. Strength
- 2. Serviceability
- 3. Stability



مپلره

القوة

المنفعة

الثيات

Other requirements.

المتطلبات تزداد باستمرار

(durability, thermal protection, sound absorption, fire resistance, economical requirements....)

Slab Performance Requirements متطلبات أداء البلاطات



• Must support loads: strength: essential.

لدعم الأحمال →قوة

• Must have adequate stiffness: serviceability: essential

صلابة مناسبة بمنفعة

Withstand severe events
 (earthquakes...): stability: optional
 دعم أحمال شديدة (الزلازل ...) →ثبات

Slab Performance Requirements متطلبات أداء البلاطات

Axial stiffness hundred times flexural stiffness





CHARACTERISTICS OF INNOVATIVE DESIGN

- Innovative design: sustainability التصميم الإبداعي هو تحقيق الحاجة من خلال المصادر المتوفرة (الديمومة)
- Voided slab removes/replaces concrete with lighter material.
- However, cavities decrease the slab resistance to shear.

• Ribbed slab: decrease dwell action, aggregate interlock

Characteristics of innovative design

- Very simple
- Cost effective
- Environment effective
- Sustainability
- Earthquake design?

History: Pal Kal System



- Before
- قبل الصب
- Concrete thickness in the lower flange
- Lower flange rebar location, diameter and dimensions

- During أثناء الصب
- Concrete web width and their continuity
- Concrete web height
- Presence of vertical rebar in the webs, its location, diameter and height above the lower flange
- Penetration depth of the Pal-Kal sheets to the lower flange
- Geometric shape of the Pal-Kal sheets

History of Voided Slabs in Palestine

- -Example in Nablus
- -Lecture from inventor of Pal-Kal

Debates

- Shear
- Earthquake resistance







- The Versailles wedding hall in <u>Jerusalem</u>
- 23 people dead, 380 were injured



- At start: the cause is Pal Kal
- Later investigations:
 - An additional story was built
 - Internal partitions were removed, few inches deflection were noticed, considered as aesthetic problem solved by injection

Theoretical Comparisons

- -Analysis: based on assumptions (can be modified, no problem)
- -Design:
 - -Flexure: minor, major players are f_y, A_s, d
 - -Deflection: minor

-Shear: major loss in aggregate interlock

Theoretical Comparisons

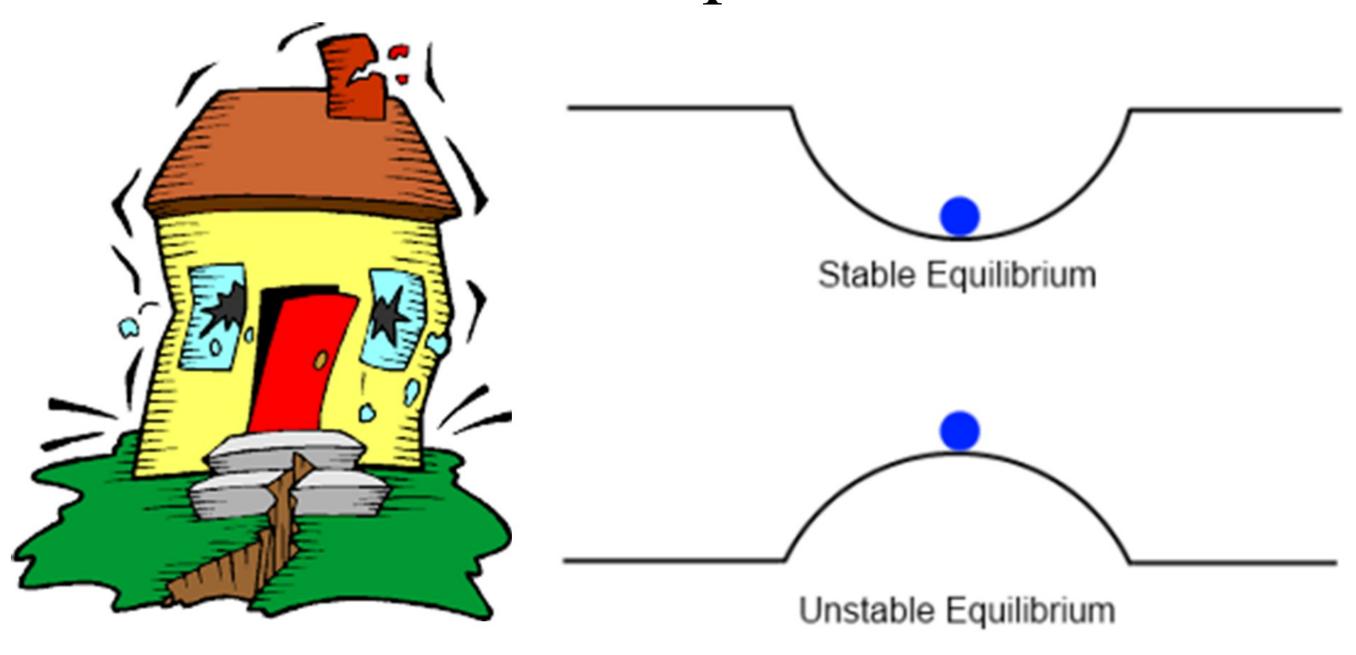
Assumptions

Theories

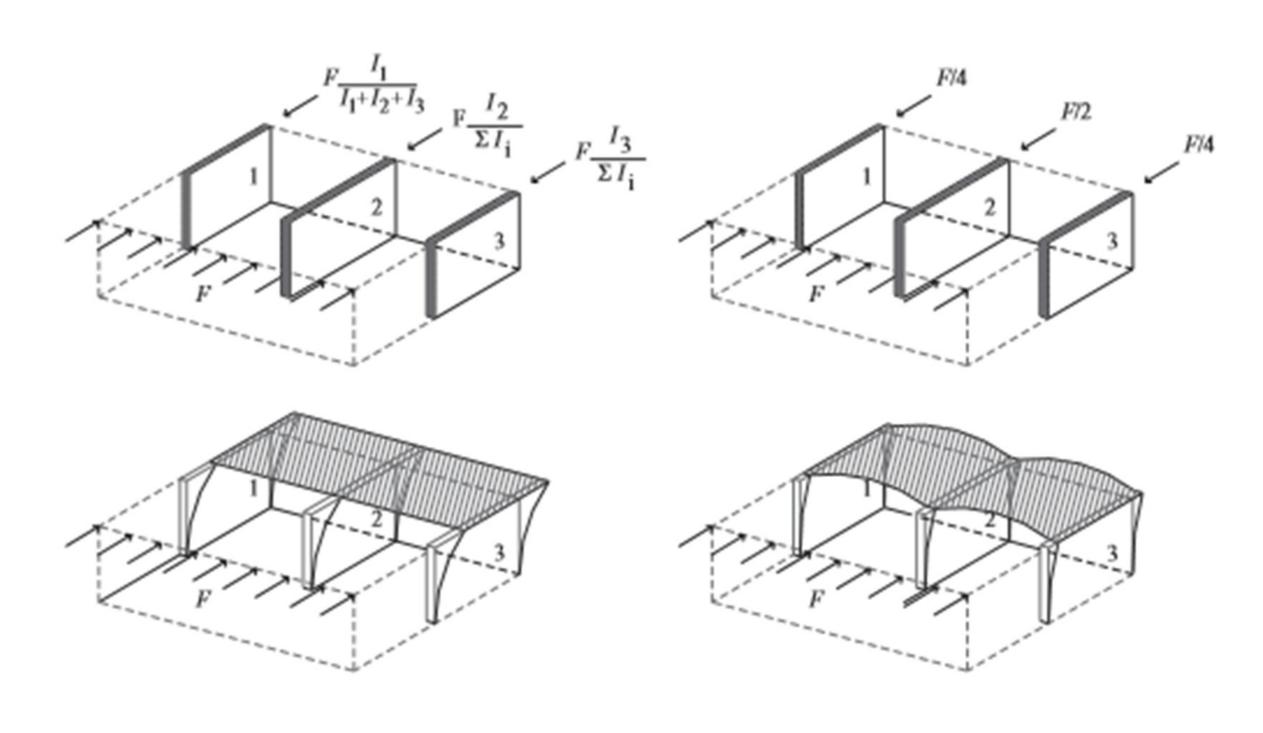
Facts



Theoretical Comparisons Earthquakes



Theoretical Comparisons Earthquake Loads



Theoretical Comparisons مقارنات نظریهٔ

	Waffle with beams	Ribbed with beams	Solid with beams	Solid without beams	Voided slab with beams
Vertical M	LV	LV	LV	LV	LV
Vertical V	HV	HV	LV	V	HV
Vertical δ	HV	HV	LV	V	V
Lateral M	LV	LV	LV	LV	LV
Lateral V	HV	HV	LV	V	HV
Lateral Δ	HV	HV	LV	V	V
weight	V	V	HV	HV	LV
assumptions	HV	HV	LV	LV	V

v=vulnarable, L=least, H=high

Types of Voided Slabs

-Forms can take any shape to fit the particular

need: spherical, cubic, ...

-Material of form: disposal for environment

protection

Examples

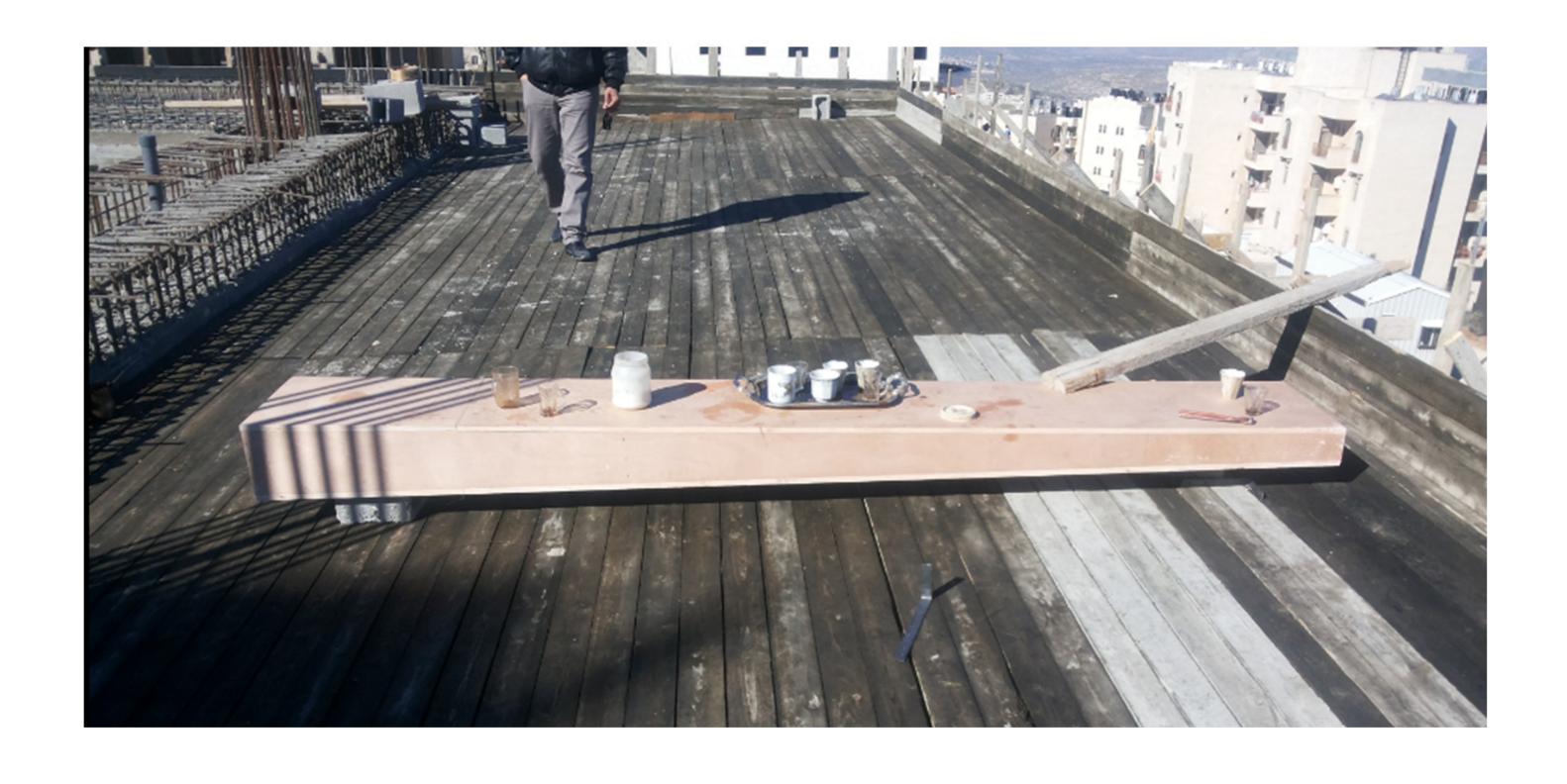
أمثلة

-Imitating new entry:

تصميم مظلة الحاج طاهر المصري/الدوار

-Enhancing new entry:

فيلا في نابلس











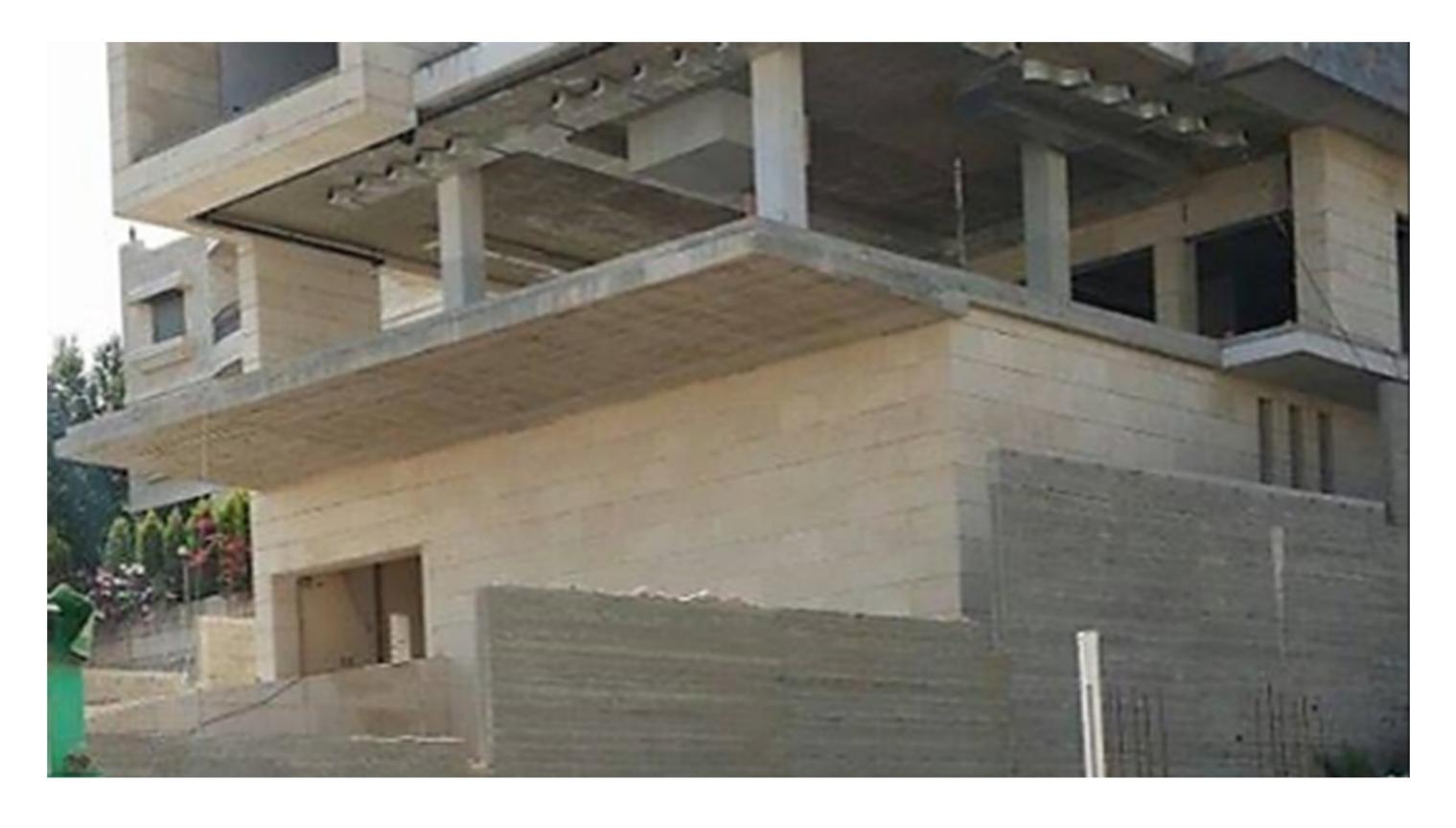












Conclusion s

- -First duty: safety
- -Be careful in shear
- -Use voided for long spans
- -better than ribbed slabs for earthquake resistance
- -Use false ceiling

تذکیر Reminder

قَدْ مَكَرَ الْذِينَ مِنْ قَبْلِهِمْ فَأَتَى اللَّهُ بُنْيَانَهُمْ مِنَ الْقُوَاعِدِ فَخَرَّ عَلَيْهِمُ السَّقْفُ مِنْ فَوْقِهِمْ وَأَتَاهُمُ الْعَذَابُ مِنْ حَيْثُ لَا يَشْعُرُونَ (26)النحل

أَأْنَتُمْ أَشَدُّ خَلْقًا أَمِ السَّمَاءُ بَنَاهَا (27) رَفَعَ سَمْكَهَا فَسَوَّاهَا (27) أَنْتُمْ أَشَدُّ خَلْقًا أَمِ السَّمَاءُ بَنَاهَا (27) رَفَعَ سَمْكَهَا فَسَوَّاهَا (28) أَلْنَازُ عات

اللَّهُ الَّذِي رَفَعَ السَّمَاوَاتِ بِغَيْرِ عَمَدٍ تَرَوْنَهَا ...(2)الرعد



شكرا لحسن استماعكم





الأسئلة