



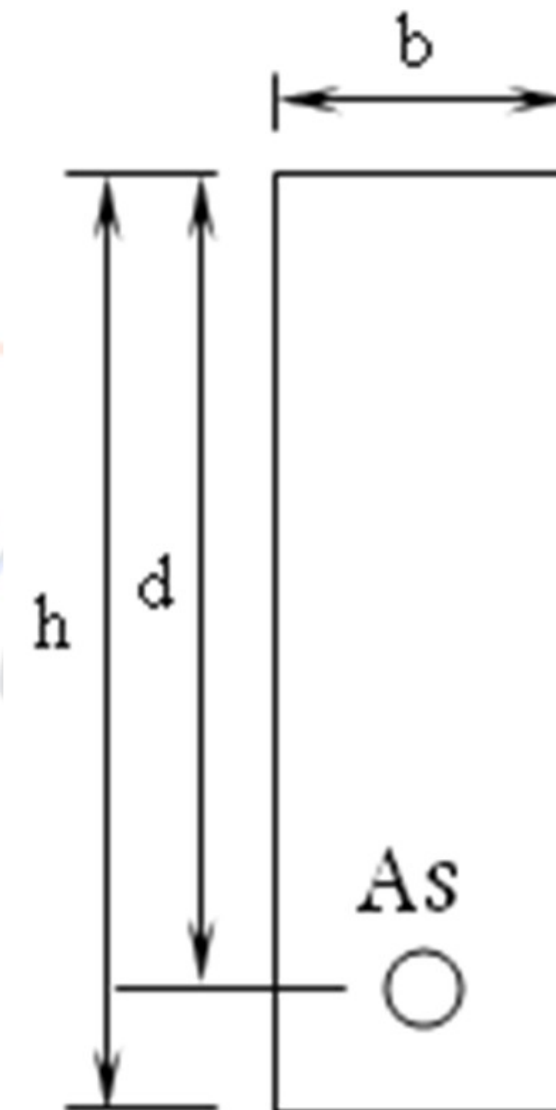
# System Design Fundamentals

Abdul Razzaq Touqan

Civil Engineering

## Objectives:

- to introduce the building construction determinant
- to analyze different systems by finite element method and analogical methods
- to build conceptual abilities in designing reinforced concrete elements.



- Most of the education and research is concentrated in analytical and anatomical skills and very little in creativity skills (analogical skills) which is fundamental in design.
- Creativity is the ability to conceive, generate design alternatives and preserve environment. It requires compositional ability.
- Compositional ability requires conceptual understanding which is based on both: “a feeling” for behavior and “approximate” analysis\design skills

- System design addresses the need for conceptual design skills.
- A design project provides opportunity for teams of students to create conceptual designs and make representations to a design “jury”.
- It provides opportunity to concentrate on the structure as a whole and very little on the element behaviour.
- The conceptual design is based on a systematical approach

- Introduction to systems
- Purpose
- System determinants
- Standards versus codes
- Fundamentals of thinking

- A system can be defined as a group of related parts that move or work together.
- A system is a necessary part of life. It occurs at any level, ranging from the molecular structure of material to laws of universe.
- As **order**, it relates all the parts of a whole reflecting some pattern of **organization**.
- Everything has system, even if we have not yet recognized it. Societies are a form of structural systems to properly function- language has system, the interrelationship of plants and animals with their **environment** represents equilibrium in nature which is a system by itself.

- The purpose of a system is to combine global understanding with local details.
  - Discuss face of human being and how systematically it combines architectural, structural, mechanical and electrical systems
  - Analogy between a mosque and shape of human raising his hands.

# System determinants:

Engineering systems must develop:

- **Support system (structure\science):**
- It holds the structure up so that it does not collapse. A need for **strength** to achieve this.
- It prevents elements to deform or crack excessively. A need for **serviceability** to achieve this.
- It makes the structure withstands severe events (like earthquakes, wind storms, ...). A **special\stable** design is needed to achieve this (**savings** in materials: smaller sections + larger strength).

- **Faith system (facts\faith):**

It Defines

- space configuration based on **functional** needs (social, economical),
- The capacity of adaptation based on **freedom** needs (legal, environmental)
- geometrical shape based on **form** needs (culture, esthetics)

# Standards versus codes

- Standard means an approved model or level of quality
- Code means a set of rules
- Minimum standards are controlled by design codes.
- Design codes are based on model codes which often specify a particular industry standard.
- Municipal and state governments adopt the model codes (or develop their own codes) and thus provide legally enforceable laws with which the engineer must comply.
- The intent of the code is not to limit engineering creativity, but to provide minimum standards to safeguard the health and safety of the public.

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Input: decompose problem into components

know degree of components

**draw** a mathematical model

Processing: define laws governing mechanics

provide **details** needed to solve problem

**design** methodology to solve problem (manual, computer)

Output: deliver solution in a nice way

enhance solution to values (dean)

**develop** capability to solve problems



- Architectural
- Structural
- Mechanical
- Electrical
- ....
- Earthquake:
  - Geology
  - Seismology
  - Geotechnical: soil+foundation
  - Structural

- Structure first before architectural
- Scalar, vector, stress,...., elasticity constants





# draw a mathematical model

- 1D models
- 2D models
- 3D models
- ....



- **Laws:** conceptual according to degree
  - constitutive relationships: stress-strain relationships
  - Counter-balance: equilibrium equations
  - compatibility equations: kinematics
- **Theories:**
  - Based on:
  - Assumptions based on:
  - Available knowledge is constrained with:



## Details needed: definitions

- *Conceptual is needed at first to save time:  
“what an engineer can do on a back of an envelope cannot  
tons of computer output do”*



## Input

1. Problem to be solved
2. Physics of problem
3. Mathematical model

## Processing

1. Propose theory
2. Formulate equations
3. Solve equations

## Output

1. Verify laws
2. Build engineering sense
3. Start a new cycle

- Start with present worked examples (get advantage of other thoughts-how Japan builds up quickly).
  1. See (a good engineer is a good observer),
  2. Read (plans of others),
  3. Ask (learn how to gather hidden information making sure you are satisfied with the answer, if not then argue but be careful not to go more than one round for each point (learn how to express yourself in words))

- Try to solve the problem by:
    1. Study your subject first of all.
    2. Get an overview about all tasks needed for solution.
    3. Select members of your team based on qualifications: capability to do the work + commitment.
- Choose a qualified team leader.
1. Divide the tasks between the team members.
  2. Put a study plan (allocate time for each task + plan alternatives).
  3. Think how to do your part of the work on paper (learn how to express yourself in writing).

- Systematical management of tasks
  1. Survey literature of the subject (system determinants). Be careful to cover all sides of the problem.
  2. Put a plan how to cover general principles before particular ones
  3. Make sure to stress the important issues and basic principles (support your work by scientific proof)
- Put contents of your final report
  1. Unify with your team members all symbols, wording, software ...etc to be used to present the final report.
  2. Perform your study plan and see how well it is.
  3. Get feed back from all your team members about the whole project to decide to continue or go to alternatives

**End of chapter 1**

Let Learning Continue

- **Limit States Design**
  - **Strength Limit State**
  - **Serviceability Limit State**
  - **Special Limit State**
- **Limit States Design**
  - **Design Philosophy**
  - **Strength Design Method**
  - **Safety Provisions**
    - **Variability in Resistance**
    - **Variability in Loading**
    - **Consequences of Failure**
    - **Margin of Safety**

# Limit State Design

## Limit State:

*Condition in which a structure or structural element is no longer acceptable for its intended use.*

Major groups for RC structural limit states

- Strength
- Serviceability
- Special

- Structural collapse of all or part of the structure (very low probability of occurrence) and loss of life can occur (a structure will not fail as long as there is a safe load path to the foundation). Major limit states are:
  - (a) Loss of equilibrium of a part or all of a structure as a rigid body (tipping, sliding of structure...: reaction could not be developed).
  - (b) Rupture of critical components causing partial or complete collapse. (flexural, shear failure...).

## (c) Progressive Collapse

- Minor local failure overloads causing adjacent members to fail until entire structure collapses.
- Structural integrity is provided by tying the structure together with correct detailing of reinforcement which provides alternative load paths to prevent localized failure.

- Functional use of structure is disrupted, but collapse is not expected. More often tolerated than a strength limit state since less danger of loss of life. Major limit states are:
  - (a) Excessive crack width leads to leakage which causes corrosion of reinforcement resulting in gradual deterioration of structure.
  - (b) Excessive deflections for normal service
    - malfunction of machinery
    - visually unacceptable
    - damage of nonstructural elements
    - changes in force distributions (no compatibility)
    - ponding on roofs leading to collapse of roof

## (c ) Undesirable vibrations

- Vertical: floors/ bridges
- Lateral\torsional: tall buildings

Damage/failure caused by abnormal conditions or loading.

These could be due to:

- (a) Extreme earthquakes: damage/collapse
- (b) Floods: damage/collapse
- (c) Effects of fire, explosions, or vehicular collisions.
- (d) Effects of corrosion, deterioration
- (e) Long-term physical or chemical instability

- Identify all potential modes of failure.
- Determine acceptable safety levels for normal structures building codes → load combination factors.

- Consider the significant limit states.
  - Members are designed for strength limit states
  - Serviceability is checked.

Exceptions may include

- water tanks (crack width)
- monorails (deflection)
- Noise in auditoriums

Two philosophies of design have long prevalent.

(a) Working stress method focusing on conditions at service loads.

(b) Strength design method focusing on conditions at loads greater than the service loads when failure may be imminent.

The strength design method is deemed conceptually more realistic to establish structural safety.

In the strength method, the service loads are increased sufficiently by factors to obtain the load at which failure is considered to be “imminent”. This load is called the *factored load* or *factored service load*.

$$\text{strength provided} \geq \left[ \begin{array}{l} \text{strength required to} \\ \text{carry factored loads} \end{array} \right]$$

Strength provided is computed in accordance with rules and assumptions of behavior prescribed by the building code and the strength required is obtained by performing a structural analysis using factored loads.

The “*strength provided*” has commonly referred to (wrongly) as “*ultimate strength*”. However, it is a code defined value for strength and not necessarily “*ultimate*”. The ACI Code uses a conservative definition of strength.

Structures and structural members must always be designed to carry some reserve load above what is expected under normal use.

There are three main reasons why some sorts of safety factor are necessary in structural design.

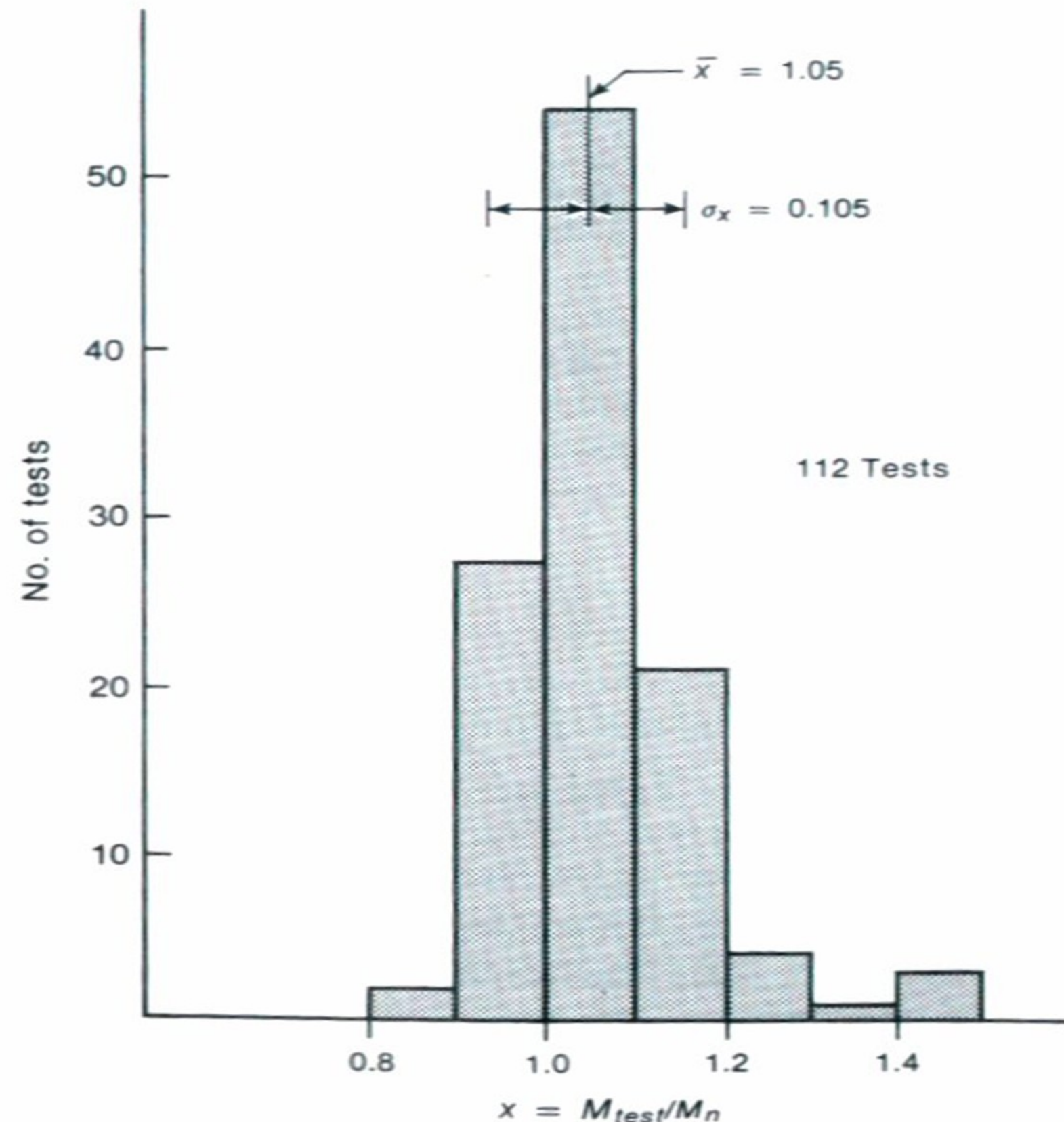
- [1] Variability in resistance.
- [2] Variability in loading.
- [3] Consequences of failure.

## *Variability in Resistance: R*

- Variability of the strengths of concrete and reinforcement.
- Differences between the as-built dimensions and those found in structural drawings.
- Effects of simplification made in the derivation of the members resistance (i.e. simplifying assumptions).

Comparison of measured and computed failure moments based on all data for reinforced concrete beams with  $f_c > 14\text{MPa}$

The variability shown is due largely to simplifying assumptions.



Frequency distribution of sustained component of live loads in offices.

In small areas:

Average =  $0.65 \text{ kN/m}^2$

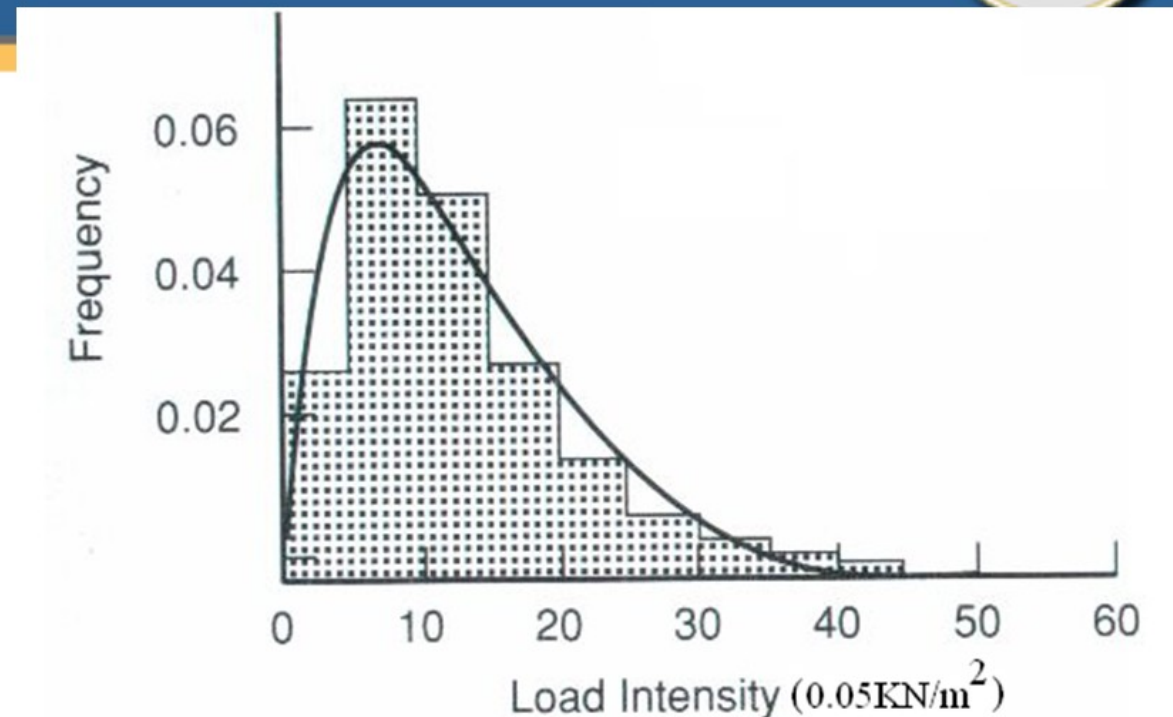
1% exceeded =  $2.2 \text{ kN/m}^2$

Code use  $2.5 \text{ kN/m}^2$

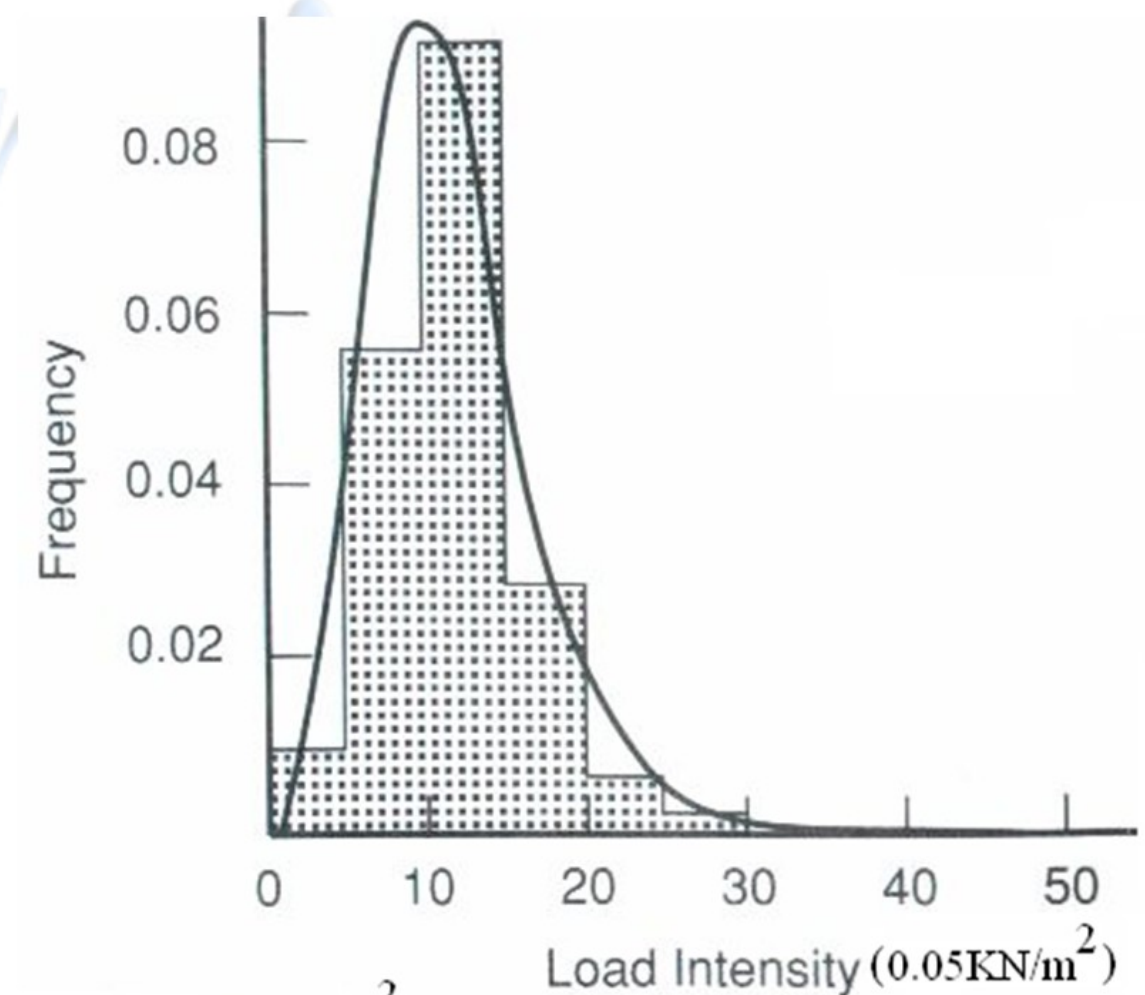
In large areas:

average almost the same, but variability decreases.

(notice that large areas can be used for parties, temporary storage...etc, thus larger LL is needed)



(a) Area =  $14 \text{ m}^2$



(a) Area =  $190 \text{ m}^2$

A number of subjective factors must be considered in determining an acceptable level of safety.

- Potential loss of life: larger SF for auditorium than a storage building.
- Cost of clearing the debris and replacement of the structure and its contents.
- Cost to society: collapse of a major road.
- Type of failure, warning of failure, existence of alternative load paths.

The term

$$Y = R - S$$

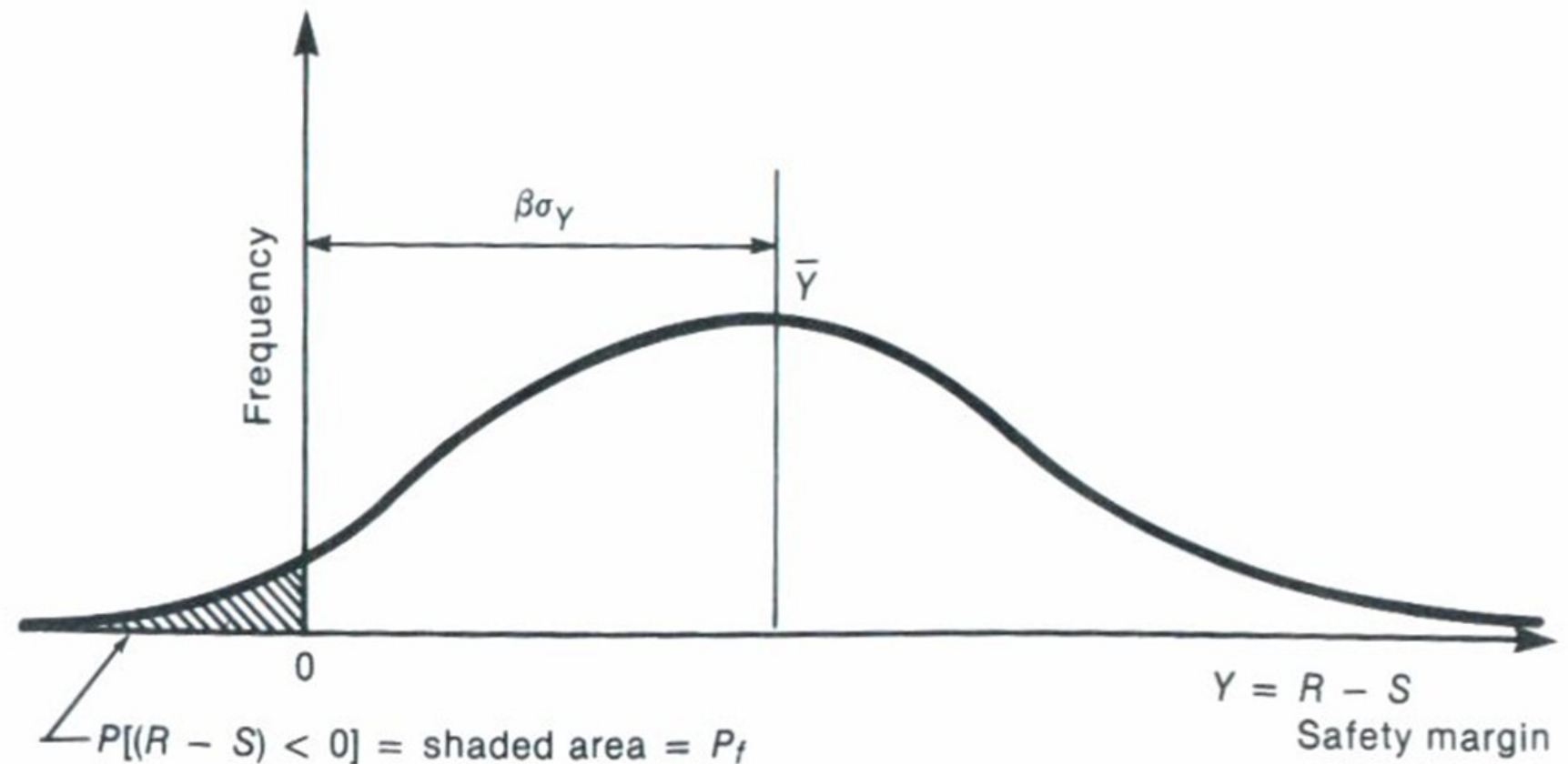
is called the safety margin.

The probability of failure is defined as:

$$P_f = \text{Probability of } [Y < 0]$$

and the safety index is

$$\beta = \frac{\bar{Y}}{\sigma_Y}$$



- Types of design can be classified as:
  - Creative
  - Development
  - Copy
- Analyze previous types showing advantages and disadvantages of each type in view of what you learned from previous two chapters.

**End of chapter 2**

Let Learning Continue

- Loading Specifications
- Dead Loads
- Live Loads
- Environmental Loads
- Classification of Buildings for Wind, Snow and Earthquake Loads
  - Snow Loads
  - Earthquake Loads
- Roof Loads
- Construction Loads
- Load factors

# Building Codes

Cities in the U.S. generally base their building code on one of the three model codes:

- Uniform Building Code
- Basic Building Code (BOCA)
- Standard Building Code

These codes have been consolidated in the 2000 *International Building Code*.

Loadings in these codes are mainly based on  
*ASCE Minimum Design Loads for Buildings  
and Other Structures ASCE 7-10.*

- Weight of all permanent construction
- Constant magnitude and fixed location

## *Examples:*

- Weight of the Structure  
(Walls, Floors, Roofs, Ceilings, Stairways)
- Fixed Service Equipment  
(HVAC, Piping Weights, Cable Tray, etc.

- Loads produced by use and occupancy of the structure.
- Maximum loads likely to be produced by the intended use.
- Not less than the minimum uniformly distributed load given by Code.

See Table 4-1 from *ASCE 7-05*

Stairs and exitways:  $4.8 \text{ kN/m}^2$ .

Storage warehouses:  $6 \text{ kN/m}^2$  (light)  
 $12 \text{ kN/m}^2$  (heavy)

Minimum concentrated loads are also given in the codes.

ASCE 7-05 allows reduced live loads for members with influence area ( $K_{LL} A_T$ ) of 38m<sup>2</sup> or more (not applied for roof):

$$L = L_o \left( 0.25 + \frac{4.6}{\sqrt{K_{LL} A_T}} \right)$$

where  $L \geq 0.50 L_o$  for members  
supporting one floor  
 $\geq 0.40 L_o$  otherwise

$K_{LL}$  = live load element factor (Table 4.2)

=2 for beams

=4 for columns

- Snow Loads
- Earthquake
- Wind
- Soil Pressure
- Roof Loads
- Temperature Differentials
- ...etc

## *Based on Use Categories (I through IV)*

- I** Buildings and other structures that represent a low hazard to human life in the event of a failure (such as agricultural facilities),  $I=1$
- II** Buildings/structures not in categories I, III, and IV,  $I=1$

**III** Buildings/structures that represent a substantial hazard to human life in the event of a failure (assembly halls, schools, colleges, jails, buildings containing toxic/explosive substances),  $I=1.25$

**IV** Buildings/structures designated essential facilities (hospitals, fire and police stations, communication centers, power-generating stations),  $I=1.5$

## Ground Snow Loads:

- Based on historical data (not always the maximum values)
- Basic equation in codes is for flat roof snow loads
- Additional equations for drifting effects, sloped roofs, etc.
- Use ACI live load factor
- No LL reduction factor allowed
- Use  $1\text{KN/m}^2$  as minimum snow load, multiply it by I (importance factor)

Inertia forces caused by earthquake motion

$$\mathbf{F} = \mathbf{m} * \mathbf{a}$$

- Distribution of forces can be found using equivalent static force procedure (code, not allowed for every building) or using dynamic analysis procedures (computer applications).

- Ponding of rainwater
  - Roof must be able to support all rainwater that could accumulate in an area if primary drains were blocked.
  - Ponding Failure (steel structures):
    - Rain water ponds in area of maximum deflection
    - increases deflection
    - allows more accumulation of water → cycle continues... → potential failure
- Roof loads (like storage tanks) in addition to snow loads
- Minimum loads for workers and construction materials during erection and repair

# Construction Loads

- Construction materials
- Weight of formwork supporting weight of fresh concrete
- Basement walls
- Water tanks

The loading variations are taken into consideration by using a series of “load factors” to determine the ultimate load,  $U$ .

$$U = 1.4D$$

$$U = 1.2D + 1.6L$$

$$U = 1.2D + 1.6W + 1.0L$$

$$U = 1.2D + 1.0E + 1.0L$$

$$U = 0.9D + E; \dots \text{etc.}$$

The equations come from ACI code 9.2

D – Dead Load

L – Live Load

E – Earthquake Load

W – Wind Load

The most general equation for the ultimate load,  $U$  ( $M_u$ ) that you will see is going to be:

$$U = 1.2D + 1.6L$$

- Ribbed slab construction is common in Palestine. Construct an allowable load table and an ultimate load table for common sizes of rib-construction. The table should include block (density  $12\text{KN/m}^3$  ) and eitong (density  $5.5\text{KN/m}^3$  ) of different sizes against different values of superimposed loads (1 to  $4\text{KN/m}^2$  in 0.5 increments).

**End of chapter 3**

Let Learning Continue

## 4.1 Short Columns

## 4.2 Beams:

### 4.2.1 Flexure

### 4.2.2 Serviceability

### 4.2.3 Shear

### 4.2.4 Bar development

### 4.2.5 Bar splices in tension

## 4.3 Footings

## 4.1 Short Columns

### General Information

**Columns:** Vertical Structural members

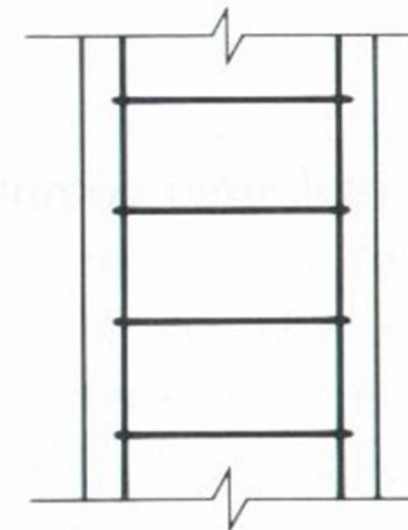
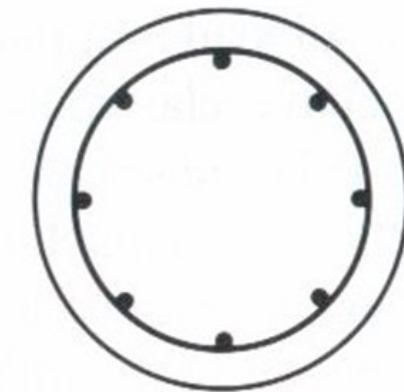
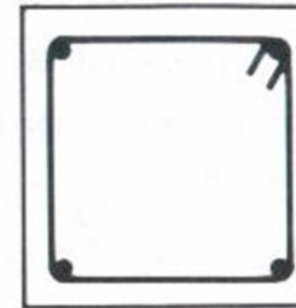
Transmits axial compressive loads with or without moment

transmit loads from the floor & roof to the foundation

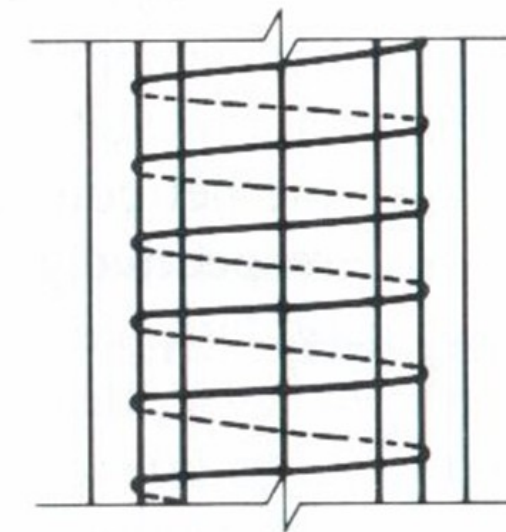
## General Information

### Column Types:

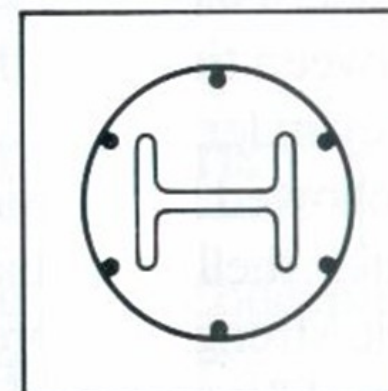
1. Tied
2. Spiral
3. Composite
4. Combination
5. Steel pipe



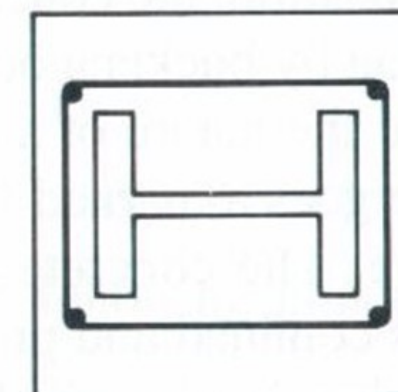
Tied



Spiral



Composite



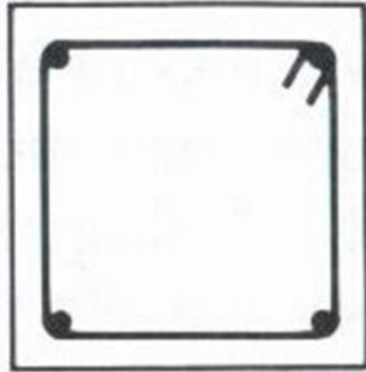
Combination



Steel pipe

# Short Columns: revision

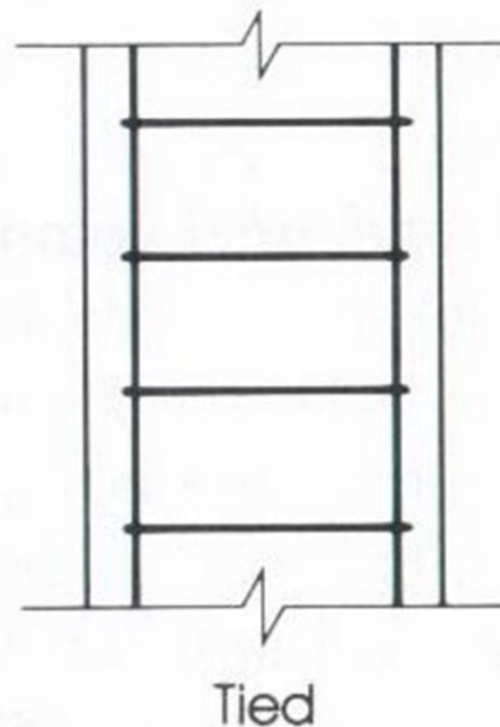
**Tied Columns** - 95% of all columns in buildings in nonseismic regions are tied



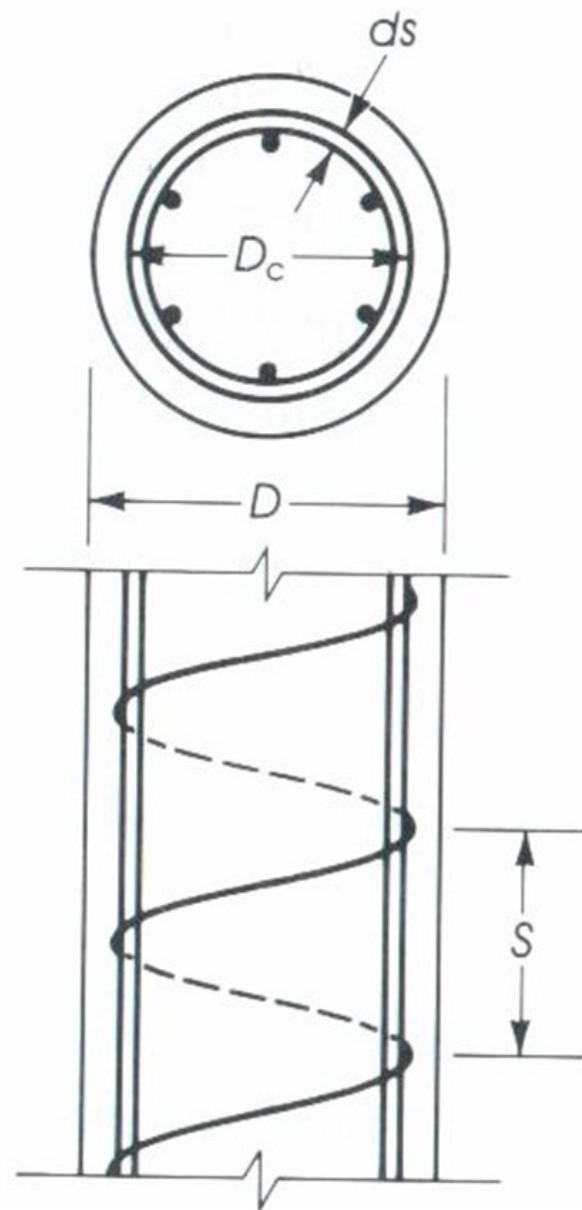
Tie spacing  $\approx b$  (except for seismic)

tie supports long bars (reduces buckling)

ties provide negligible restraint to lateral expose of core



## Spiral Columns



Pitch = 2.5cm to 7.5cm

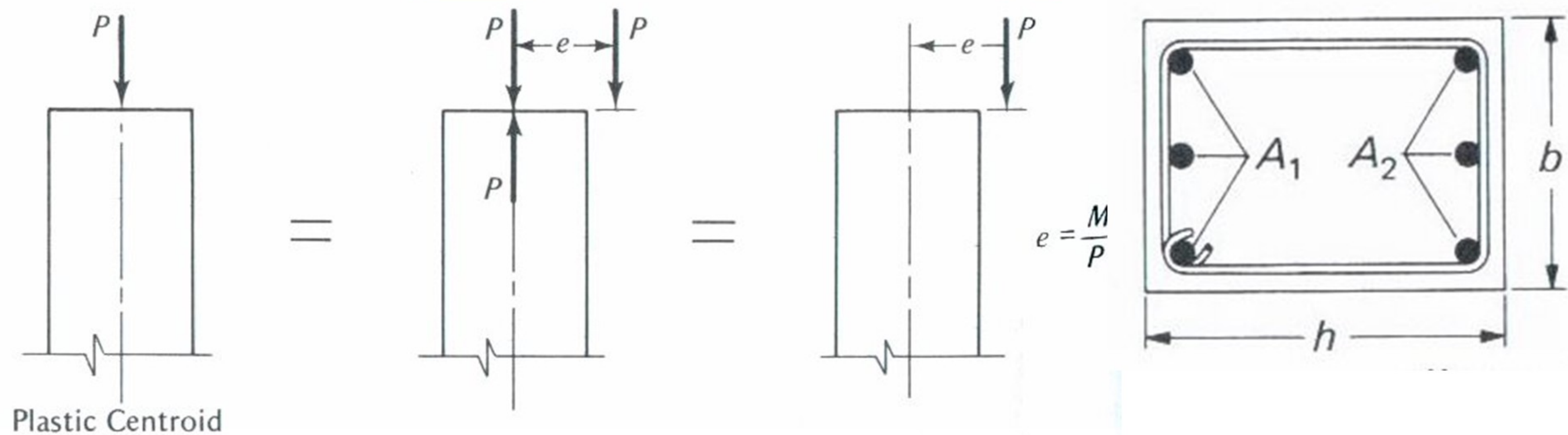
spiral restrains lateral (Poisson's effect)

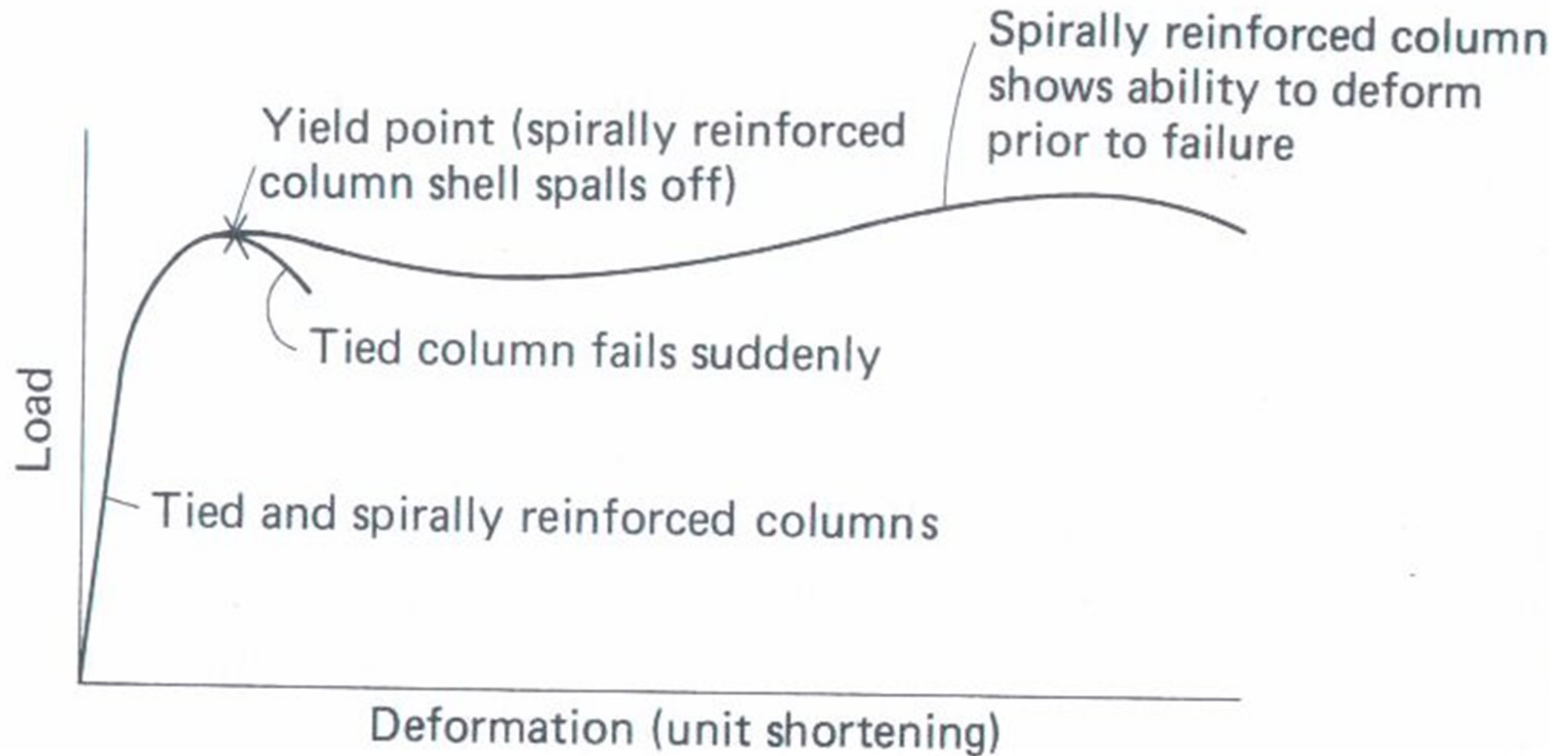
axial load  $\rightarrow$  delays failure (ductile)

## **Behavior**

An “allowable stress” design procedure using an elastic analysis was found to be unacceptable. Reinforced concrete columns have been designed by a “strength” method since the 1940’s.

# 1. Initial Behavior up to Nominal Load - Tied and spiral columns.





- Use of tributary area: area of floor or roof which supports all of the loads whose load path leads to the column.
- Use load path: slab reactions carried by beams. Beam reactions carried by columns.

$$P_0 = 0.85 f_c * (A_g - A_{st}) + f_y A_{st}$$

Let

$A_g$  = Gross Area =  $b * h$        $A_{st}$  = area of long steel

$f_c$  = concrete compressive strength

$f_y$  = steel yield strength

Factor due to less than ideal consolidation and curing conditions for column as compared to a cylinder. It is **not** related to *Whitney's* stress block.

2. Maximum Nominal Capacity for Design  $P_{n(max)} \Rightarrow$

$$P_{n(max)} = 0.8P_0 \rightarrow \textit{tied}$$

$$P_{n(max)} = 0.85P_0 \rightarrow \textit{spiral}$$

ACI 10.3.6.1-2

### 3. Reinforcement Requirements (Longitudinal Steel $A_{st}$ )

Let 
$$\rho_g = \frac{A_{st}}{A_g}$$

- ACI Code requires  $0.01 \leq \rho_g \leq 0.08$
- ACI 10.8.4 use half  $A_g$  if column section is much larger than loads.
- Minimum # of Bars (ACI Code 10.9.2): 6 in circular arrangement and 4 in rectangular arrangement

### 3. Reinforcement Requirements (Lateral Ties)

**Vertical spacing:** (ACI 7.10.5.1-3)

#10mm bars least dimension of tie

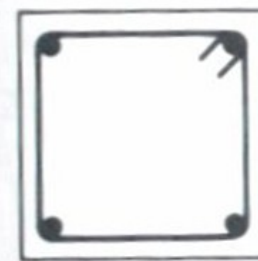
$$s \leq 16 d_b \quad (d_b \text{ for longitudinal bars})$$

$$s \leq 48 d_b \quad (d_b \text{ for tie bar})$$

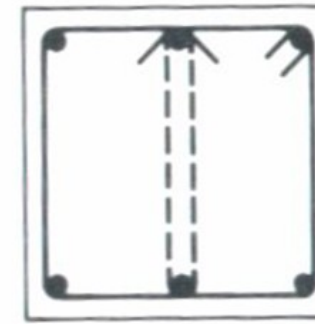
$$s \leq \text{least lateral dimension of column}$$

Every corner and alternate longitudinal bar shall have lateral support provided by the corner of a tie with an included angle not more than  $135^\circ$ , and no bar shall be more than 15cm clear on either side from “support” bar.

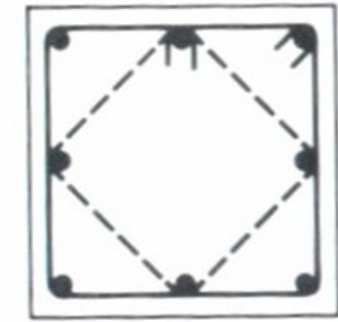
Examples of lateral ties.



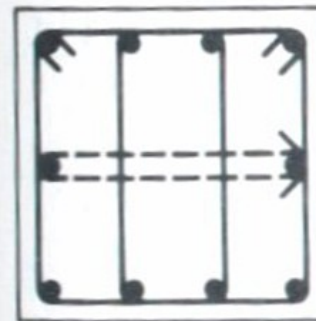
4 bars



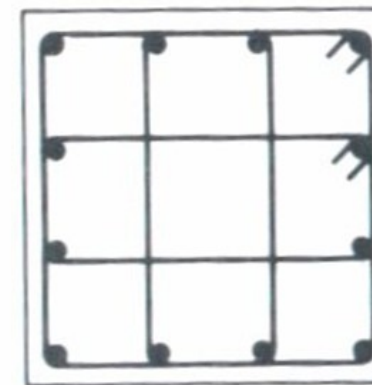
6 bars



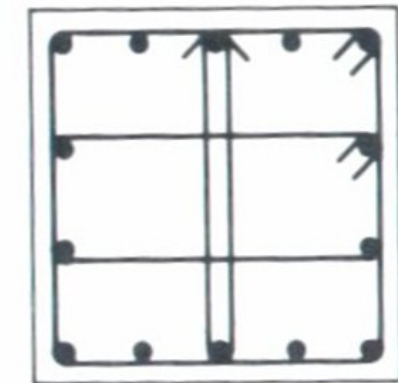
8 bars



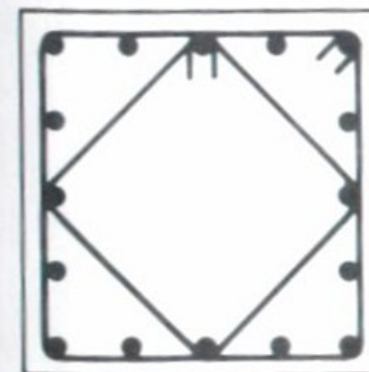
10 bars



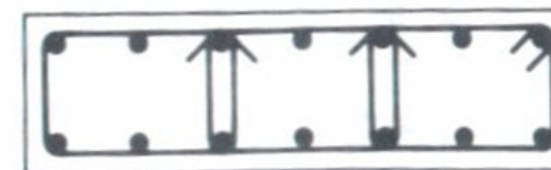
12 bars



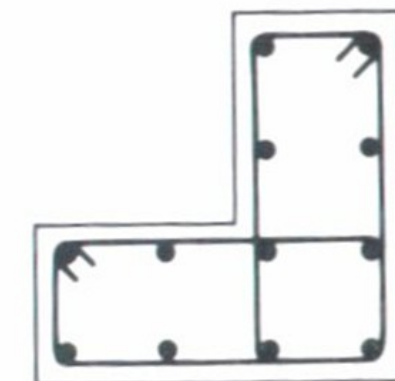
14 bars



16 bars



Wall column



Corner column

### 3. Reinforcement Requirements (Spirals )

ACI Code 7.10.4

size  $\geq$  10mm “ dia.

2.5cm  $\leq$  clear spacing between spirals  $\leq$  7.5cm ACI 7.10.4.3

## 4. Design for Concentric Axial Loads

### (a) General Strength Requirement

$$\phi P_n \geq P_u$$

where,  $\phi = 0.65$  for tied columns

$\phi = 0.75$  for spiral columns (ACI 08)

## 4. Design for Concentric Axial Loads

### (b) Expression for Design

defined:

$$\rho_g = \frac{A_{st}}{A_g} \quad \text{ACI Code } (0.01 \leq \rho_g \leq 0.08)$$

# Design of Tied Short Columns

$$\phi P_n = \phi 0.8 \left[ A_g (0.85 f_c) + A_{st} (f_y - 0.85 f_c) \right] \geq P_u$$

$$\phi P_n = \phi 0.8 A_g \left[ 0.85 f_c + \rho_g (f_y - 0.85 f_c) \right] \geq P_u$$

- The ultimate load is found using tributary area and number of stories

The design load can be approximated as follows:

# Approximate Design of Short Columns

- For a tied column with 1% steel reinforcement

$$\phi P_n = 0.65 * 0.8 A_g \left[ 0.85 f_c + 0.01 (f_y - 0.85 f_c) \right]$$

$$\phi P_n = A_g \left[ 0.438 f_c + 0.0052 f_y \right] \geq P_u$$

For 20MPa concrete strength and 420MPa yield strength and representing gross area in cm<sup>2</sup> and column capacity in kN

$$\phi P_n = 1.1 \times 10^4 (A_g \times 10^{-4}) \approx A_g$$

Thus the area of column in square cm represents approximately its capacity in kN

- Condition for short columns: braced

$$\frac{KL}{r} \leq 34 - 12 \frac{M_1}{M_2} = 34$$

$$0.5 \leq K \leq 1, r \approx 0.3b$$

$$\frac{KL}{0.3b} \leq 34 \rightarrow \frac{L}{b} \leq \frac{34 * 0.3}{K} \rightarrow \frac{L}{b} \leq 10, 20$$

- Thus if the height to width ratio is less than 15 (the mean value) the column is classified as short

- Common practice is to build four stories with 4m span dimensions. What is the size of the column needed to support a common 25cm rib construction (17cm height blocks, 15cm ribs).
- Common practice in the last 50 years is to use 6#14mm bars in columns 25cmX50cm, thus a use of 0.72% instead of 1% minimum. Comment!
- In the nineties trying to build columns with 2% reinforcement using common technology at that time yields to honeycombing, comment!
- Is it wise to design columns according to minimum design requirements, comment!

# End of 4.1

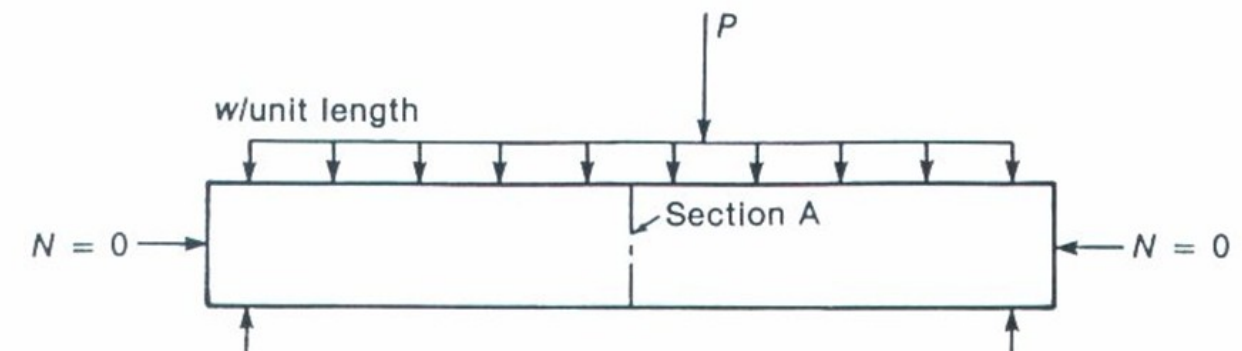
## Let Learning Continue

The beam is a structural member used to support the internal moments and shears. It would be called a beam-column if a compressive force existed.

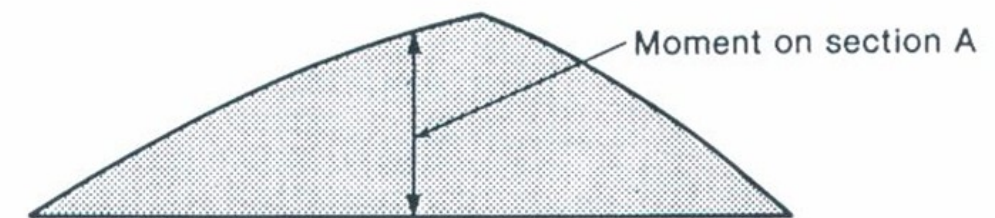
$$C = T$$

$$M = C * (jd)$$

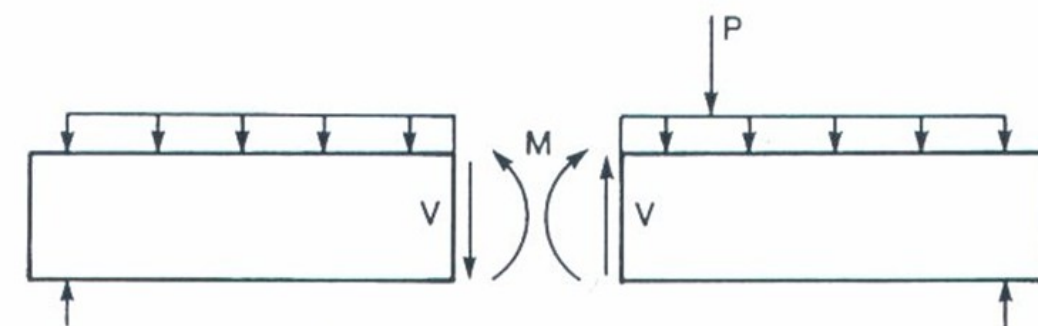
$$= T * (jd)$$



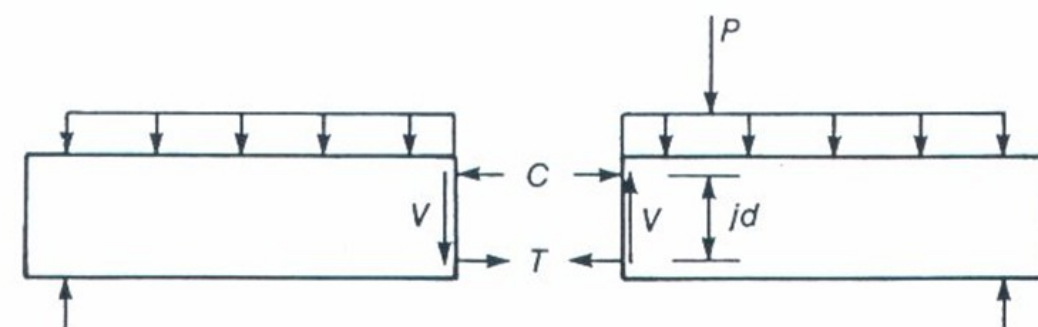
(a) Beam.



(b) Bending moment diagram.

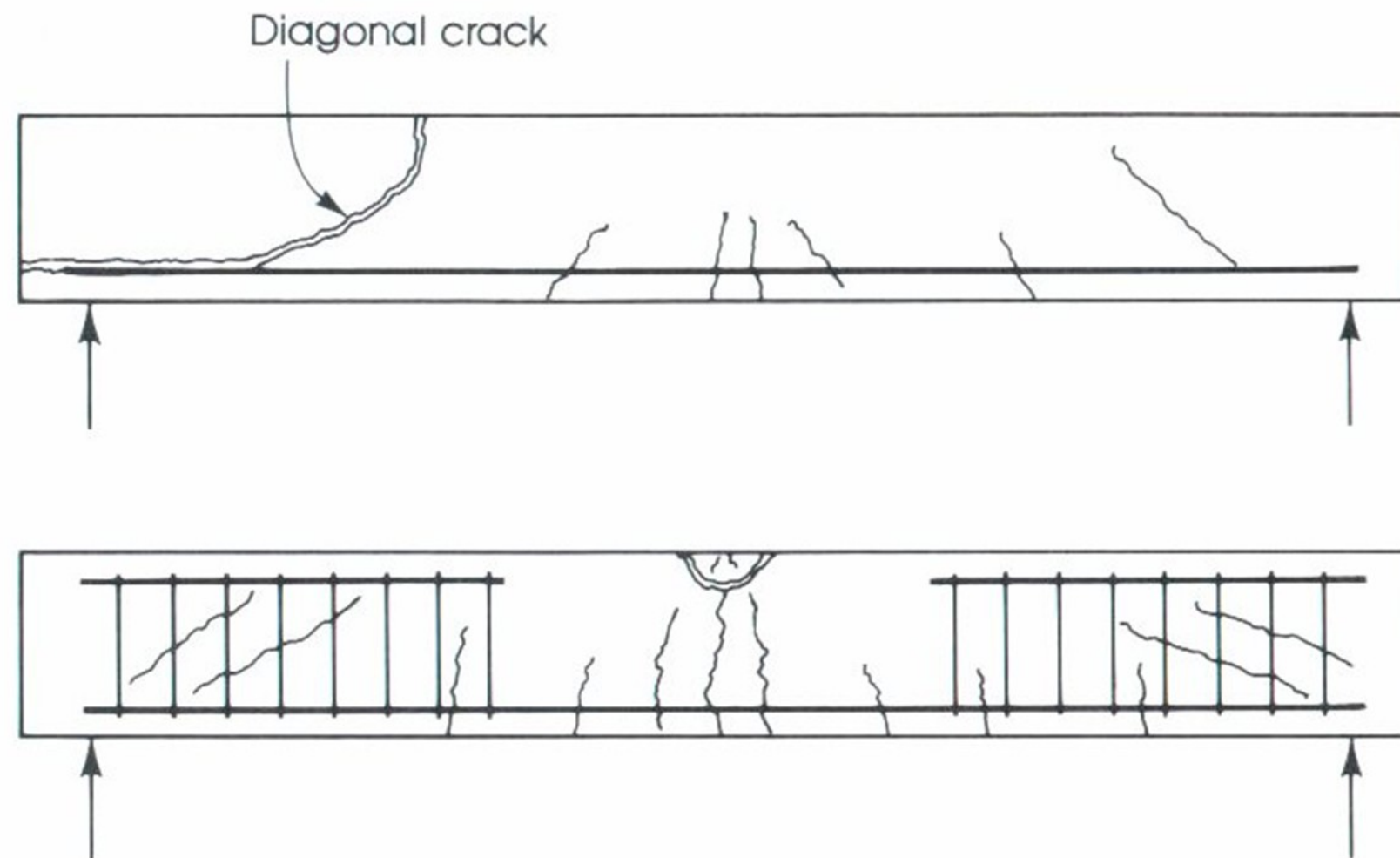


(c) Free body diagrams showing internal moment and shear force.



(d) Free body diagrams showing internal moment as a compression-tension force couple.

The first beam fails in shear, the second fails in bending moment.

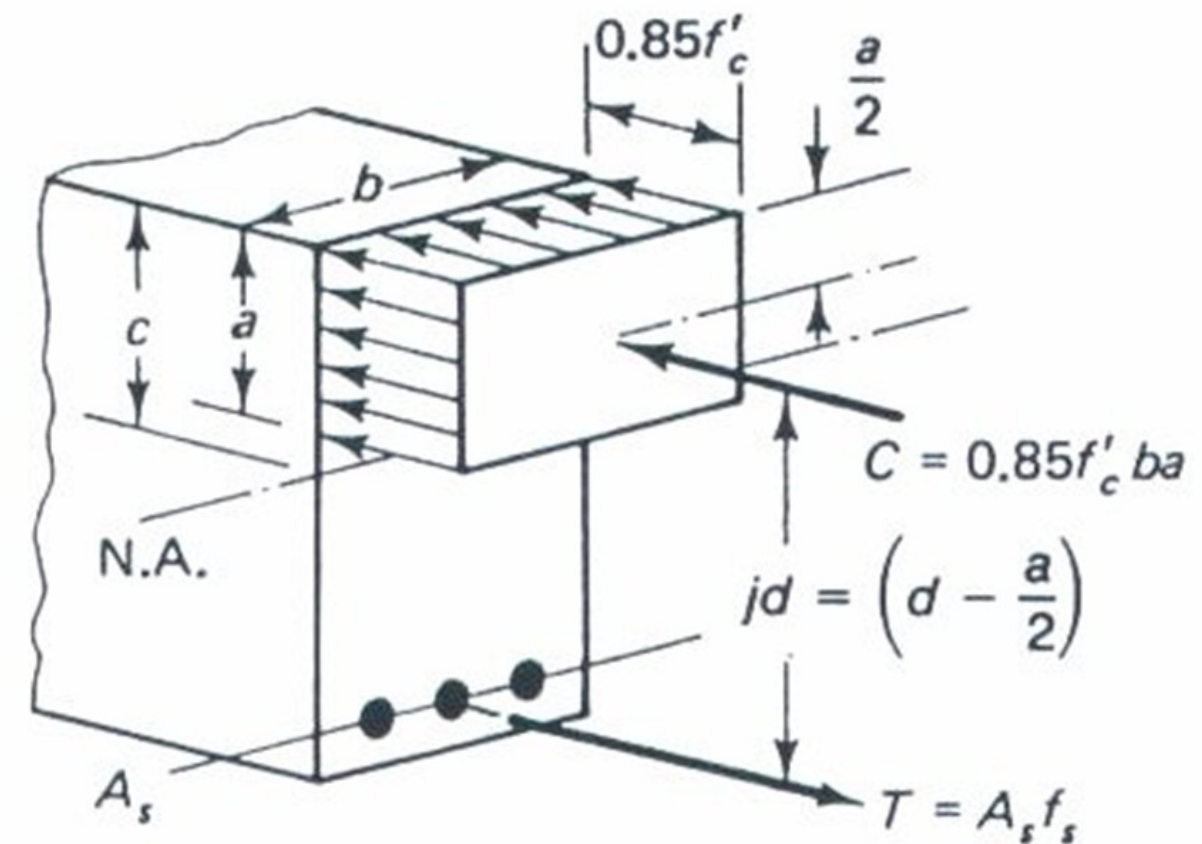
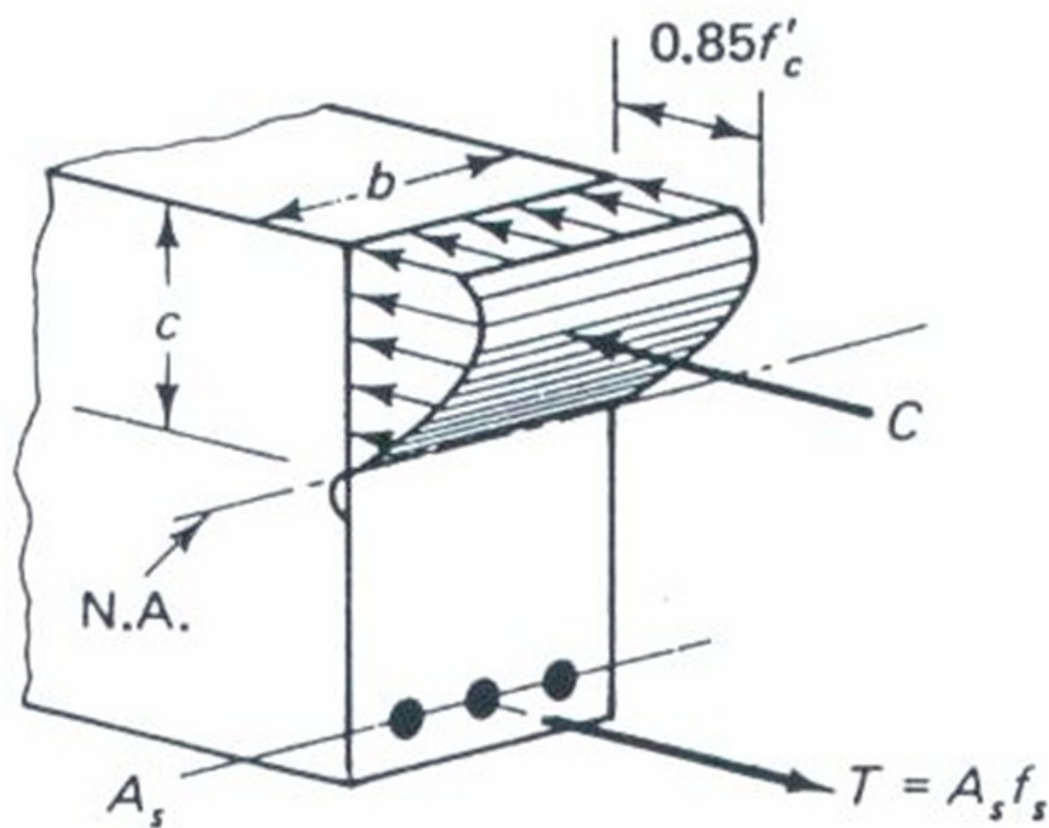


- Use of tributary area (area of floor or roof which supports all of the loads whose load path leads to the beam) determines the beam load.
- Perform approximate analysis through:
  - Approximate deflected shape to locate points of inflection, hence transform to determinate beam and analyze using statics.
  - Use analysis coefficients (e.g. ACI coefficients)
  - Use finite element programs

## *Basic Assumptions in Flexure Theory*

- Plane sections remain plane ( not true for deep beams  $h > 4b$ )
- The strain in the reinforcement is equal to the strain in the concrete at the same level, i.e.  $\varepsilon_s = \varepsilon_c$ .
- Stress in concrete & reinforcement may be calculated from the strains using  $f$ - $\varepsilon$  curves for concrete & steel.
- Tensile strength of concrete is neglected.
- Concrete is assumed to fail in compression, when  $\varepsilon_c = 0.003$
- Compressive  $f$ - $\varepsilon$  relationship for concrete may be assumed to be any shape that results in an acceptable prediction of strength.

The compressive zone is modeled with an equivalent stress block.



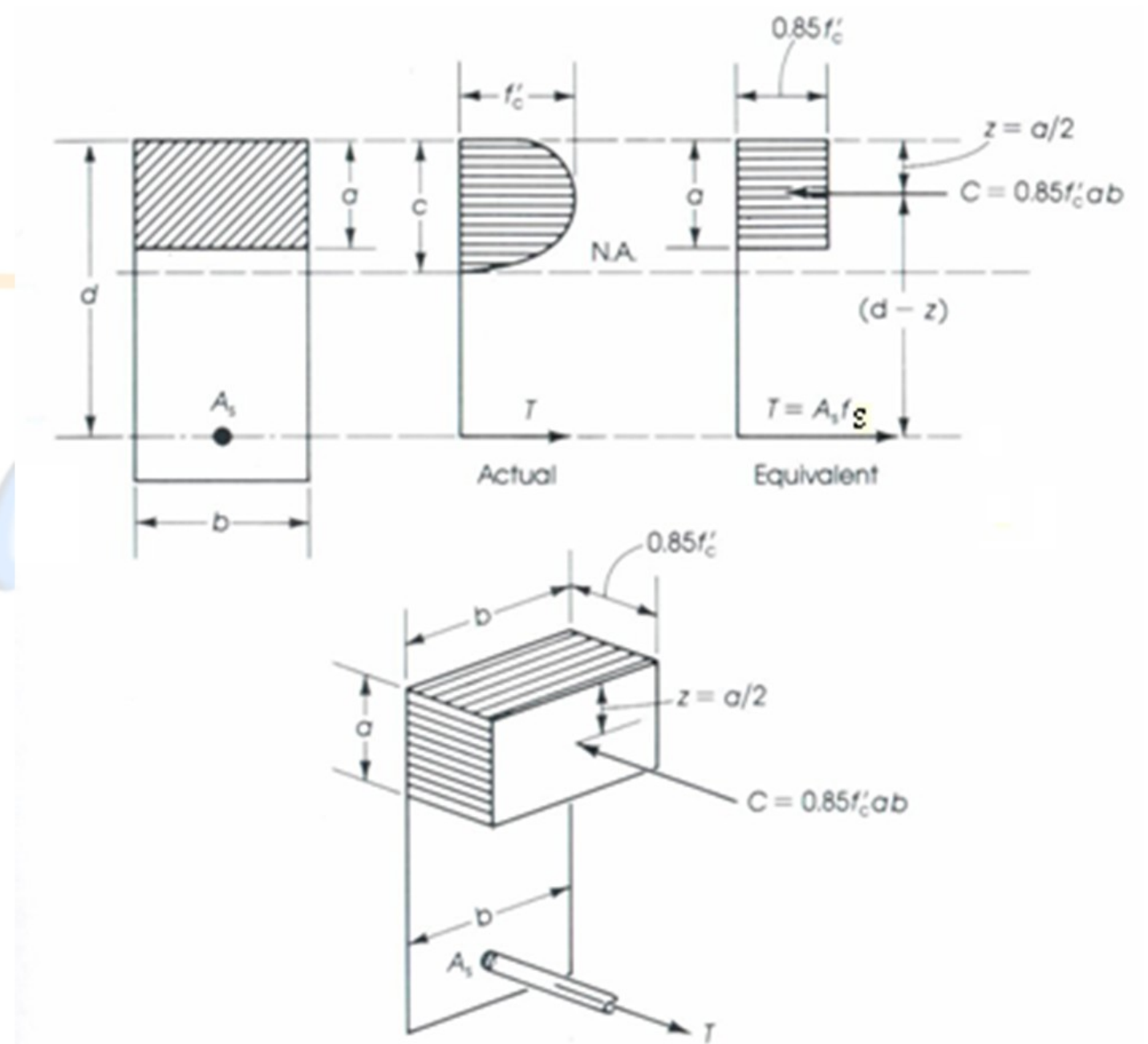
## Example of rectangular reinforced concrete beam.

Setup equilibrium.

$$\sum F_x = 0 \Rightarrow T = C$$

$$A_s f_s = 0.85 f_c' a b$$

$$\sum M = 0 \Rightarrow T \left( d - \frac{a}{2} \right) = M_n$$



The ultimate load, which is used in the design and analysis of the structural member is:

$$M_u = \phi M_n$$

$M_u$  – Ultimate Moment

$M_n$  – Nominal Moment

$\Phi$  – Strength Reduction Factor

The strength reduction factor,  $\Phi$ , varies depending on the tensile strain in steel in tension. Three possibilities:

Compression Failure - (over-reinforced beam)

Tension Failure - (under-reinforced beam)

Balanced Failure - (balanced reinforcement)

## Which type of failure is the most desirable?

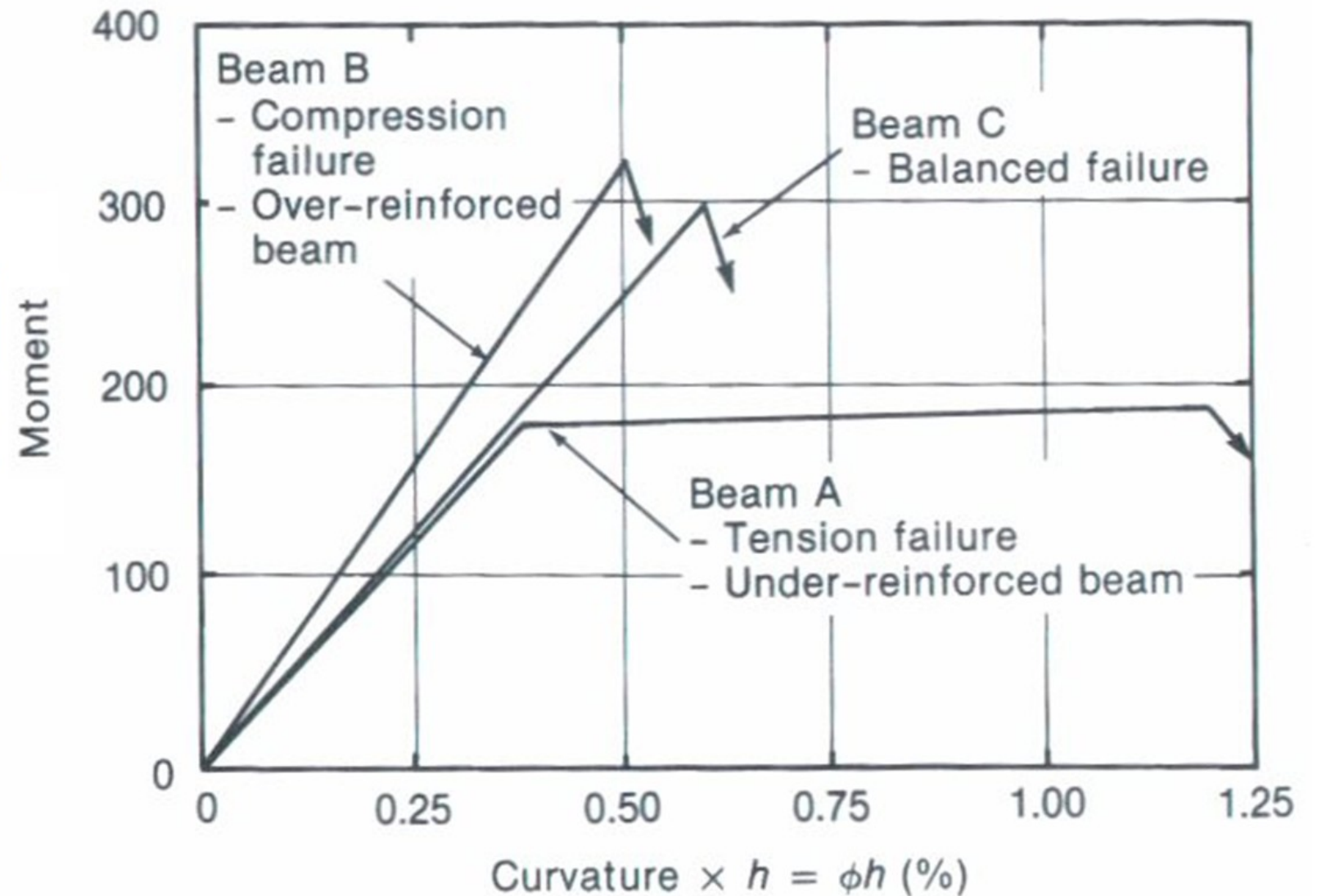
The *under-reinforced beam* is the most desirable.

$$f_s = f_y$$

$$\epsilon_s \gg \epsilon_y$$

You want ductility

system deflects and still carries load.



For under-reinforced, the equation can be rewritten as:

$$C = T \quad \Rightarrow \quad 0.85 f'_c b a = A_s f_y$$

$$a = \frac{f_y A_s}{0.85 f'_c b}$$

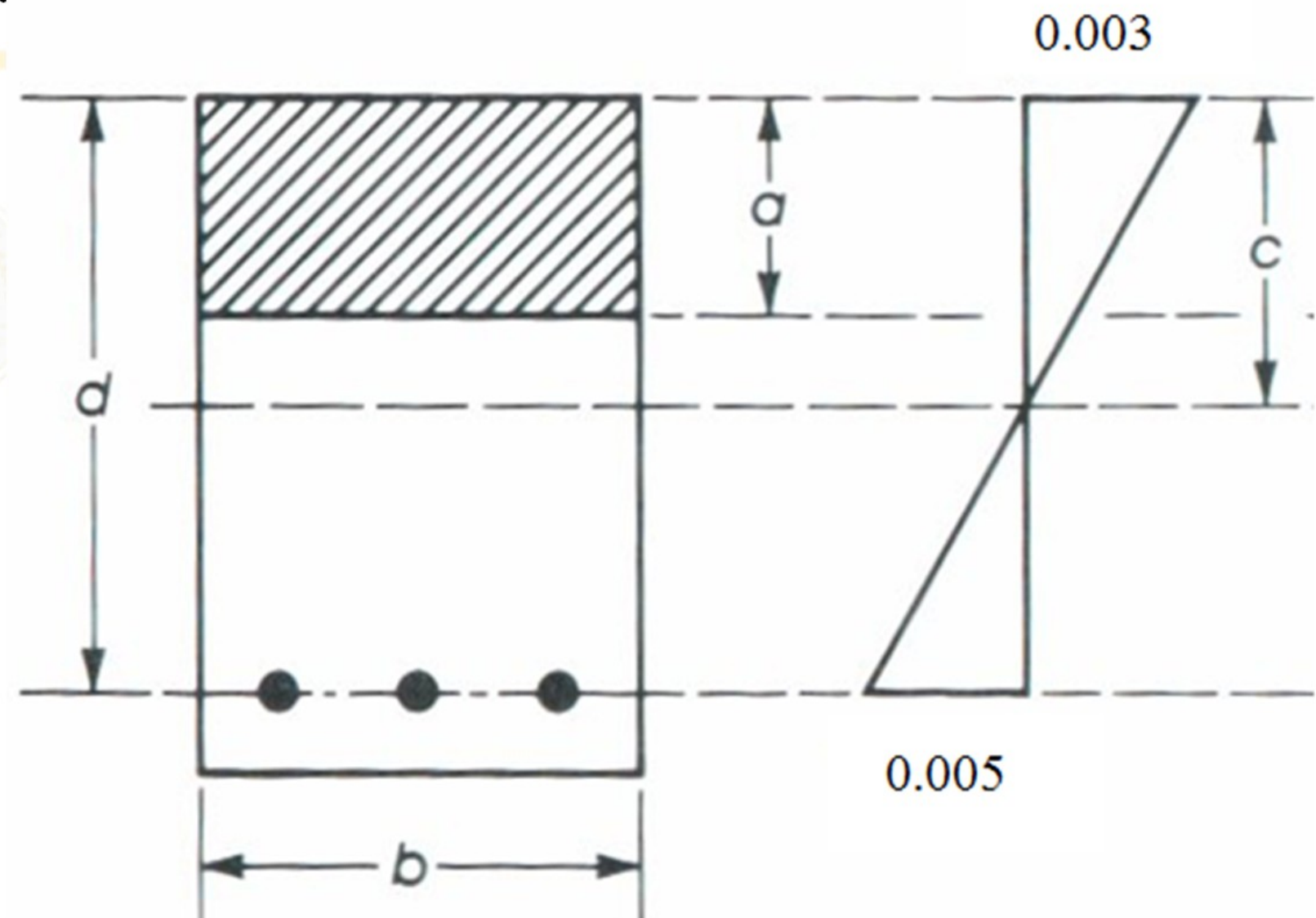
$$M_n = A_s f_y d \left( 1 - \frac{f_y A_s}{1.7 f'_c b d} \right)$$

$$M_d = \phi M_n = A_s d \phi f_y \left( 1 - \frac{\rho f_y}{1.7 f'_c} \right) = A_s d j$$

$\rho_{\max}$  = maximum  $\rho$  value recommended to get simultaneous  $\varepsilon_c = 0.003$  &  $\varepsilon_s = 0.005$

Use similar triangles:

$$\frac{0.003}{c} = \frac{0.005}{d - c}$$



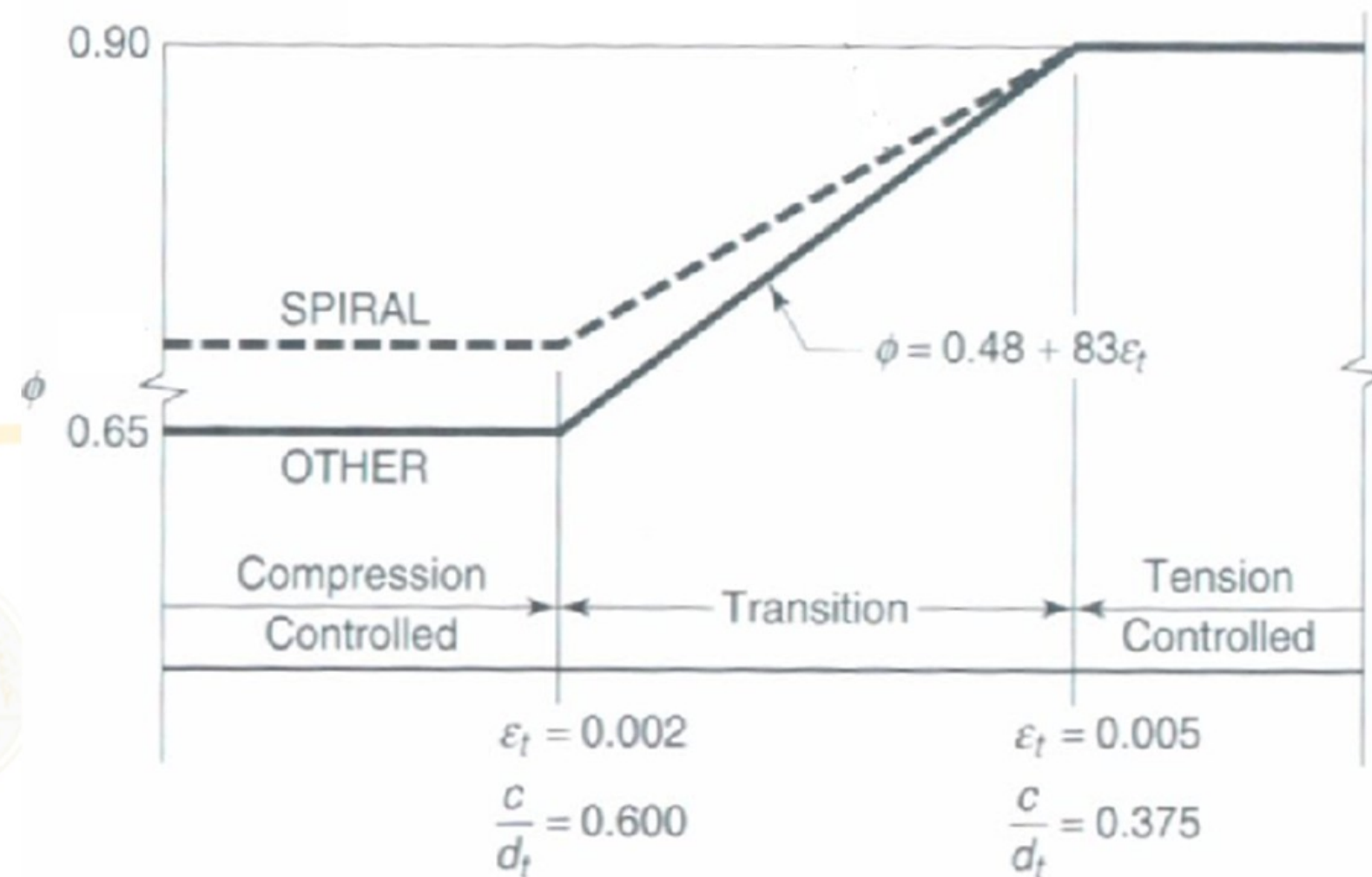
For a yield stress 420MPa, the equation can be rewritten to find  $c$  as

$$c = \frac{0.003d}{0.008} \Rightarrow c = 0.375d$$

$$a = 0.85c = 0.319d$$

$$\rho = 0.271f'_c/f_y$$

The strength reduction factor,  $\phi$ , will come into the calculation of the strength of the beam.



## The factor $J$ for large steel ratios

$$M_d = \phi M_n = A_s d \phi f_y \left( 1 - \frac{\rho f_y}{1.7 f'_c} \right) = A_s d j$$

$$j = \phi f_y \left( 1 - \frac{\rho f_y}{1.7 f'_c} \right)$$

- For concrete strength variation 20MPa to 42Mpa, the value of  $J$  for maximum recommended steel ratio varies is 0.317. Moment in kN.m, area of steel in square cm and depth in cm.

Lower Limit on  $\rho$

ACI 10.5.1

$$A_{s(\min)} = \frac{\sqrt{f'_c}}{4 f_y} * b_w d \geq \frac{1.4}{f_y} * b_w d \quad \text{ACI Eqn. (10-3)}$$

$f_c$  &  $f_y$  are in MPa

Lower limit used to avoid “Piano Wire” beams.

Very small  $A_s$  (  $M_n < M_{cr}$  )

Strain in steel is huge (large deflections)

when beam cracks (  $M_u / \Phi > M_{cr}$  ) beam fails right away because nominal capacity decreases drastically.

# The factor $J$ for minimum steel ratios

$$j = \phi f_y \left( 1 - \frac{\rho f_y}{1.7 f'_c} \right) = \phi f_y \left( 1 - \frac{1.4}{1.7 f'_c} \right)$$

- For concrete strength variation 20MPa to 42Mpa, the value of  $J$  for minimum steel varies from 0.36 to 0.37

- It is obvious that variation of J is not sensitive to changes in concrete strength. Thus a mean value of 0.33 is representative for all types of concrete used in Palestine (B250-B500)

$$M_d = \frac{A_s d}{3}$$

Temperature & Shrinkage reinforcement in structural slabs and footings (ACI 7.12) place perpendicular to direction of flexural reinforcement.

GR 40 or GR 50 Bars:  $A_s (T\&S) = 0.0020 A_g$

GR 60  $A_s (T\&S) = 0.0018 A_g$

$A_g$  - Gross area of the concrete

**End of 4.2.1**

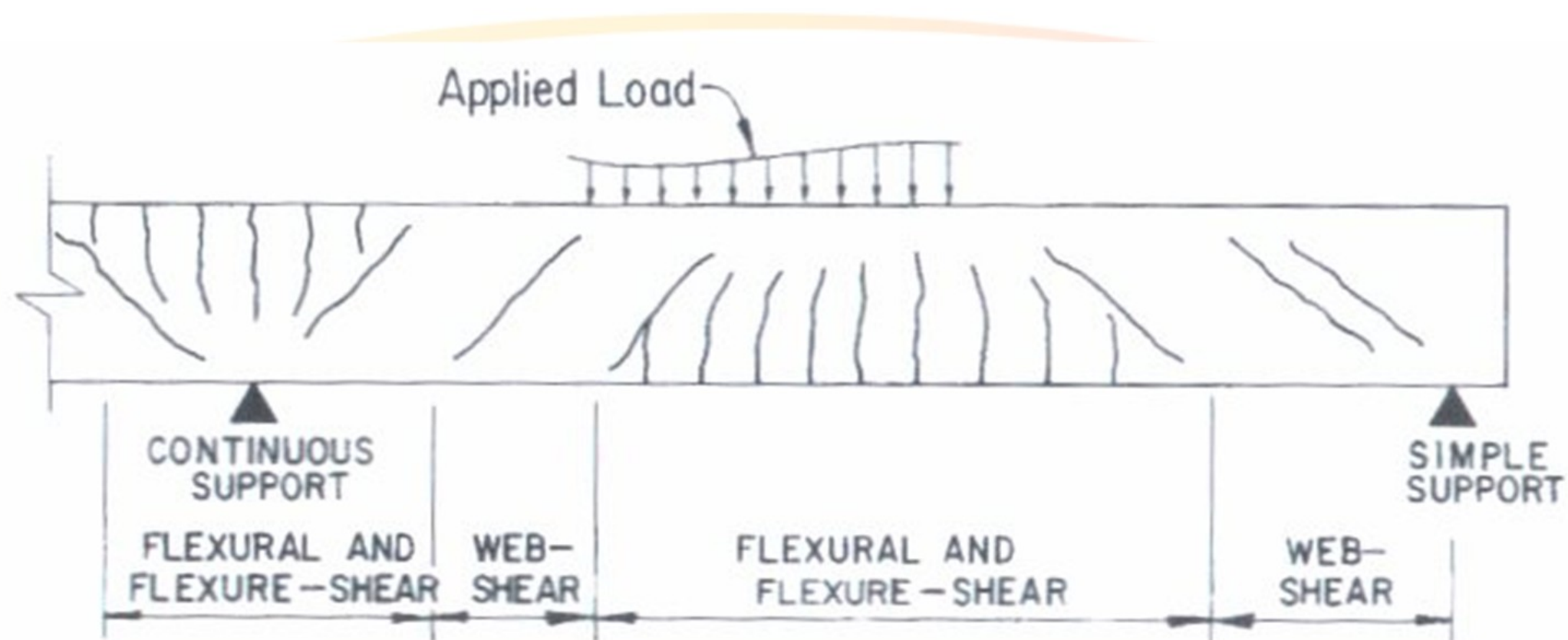
Let Learning Continue

### Beam Depths

- ACI 318 - Table 9.5(a) min.  $h$  based on span (slab & beams)
- Design for max. moment over a support to set depth of a continuous beam.

## 4.2.3 Shear

Typical Crack Patterns for a deep beam.



## Shear Strength (ACI 318 Sec 11.1)

$$\phi V_n \geq V_u$$

capacity  $\geq$  demand

$V_u$  = factored shear force at section  
 $V_n$  = Nominal Shear Strength  
 $\phi = 0.75$  (shear) – strength reduction factor

$$V_n = V_c + V_s$$

$$V_c = \frac{\sqrt{f'_c}}{6} b_w d = \text{Nominal shear resistance provided by concrete}$$

$$V_s = \text{Nominal shear resistance provided by the shear reinforcement}$$

**11.4.6.1** — A minimum area of shear reinforcement,  $A_{v,min}$ , shall be provided in all reinforced concrete flexural members (prestressed and nonprestressed) where  $V_u$  exceeds  $0.5\phi V_c$ , except in members satisfying one or more of (a) through (f):

- (a) Footings and solid slabs;
- (c) Concrete joist construction defined by 8.13;
- (d) Beams with  $h$  not greater than 250 mm;
- (e) Beam integral with slabs with  $h$  not greater than 600 mm and not greater than the larger of 2.5 times thickness of flange, and 0.5 times width of web;

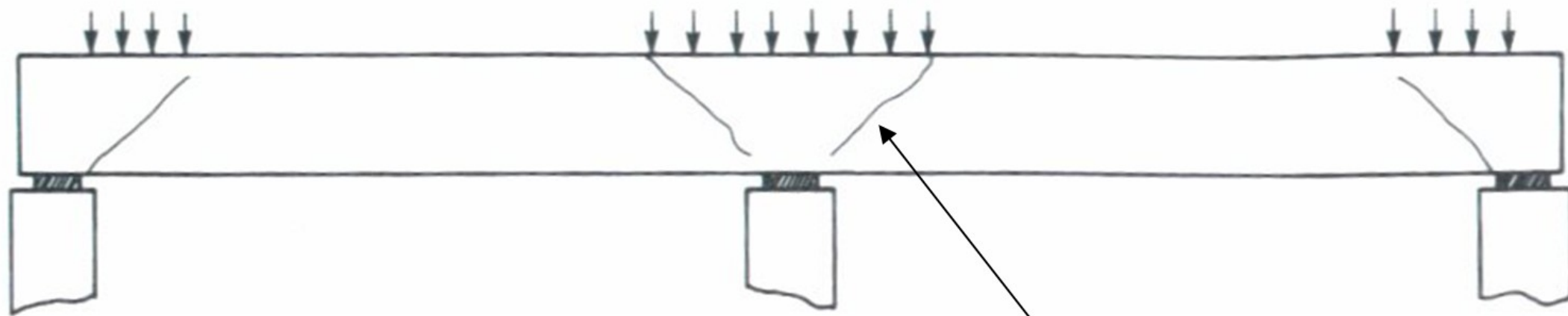
# Approximate design for shear

- Better to use

$$V_u < 0.5\phi\sqrt{f'_c} b_w d$$

- Hence

$$s_{\max} \leq \frac{d}{2} \leq 60cm$$



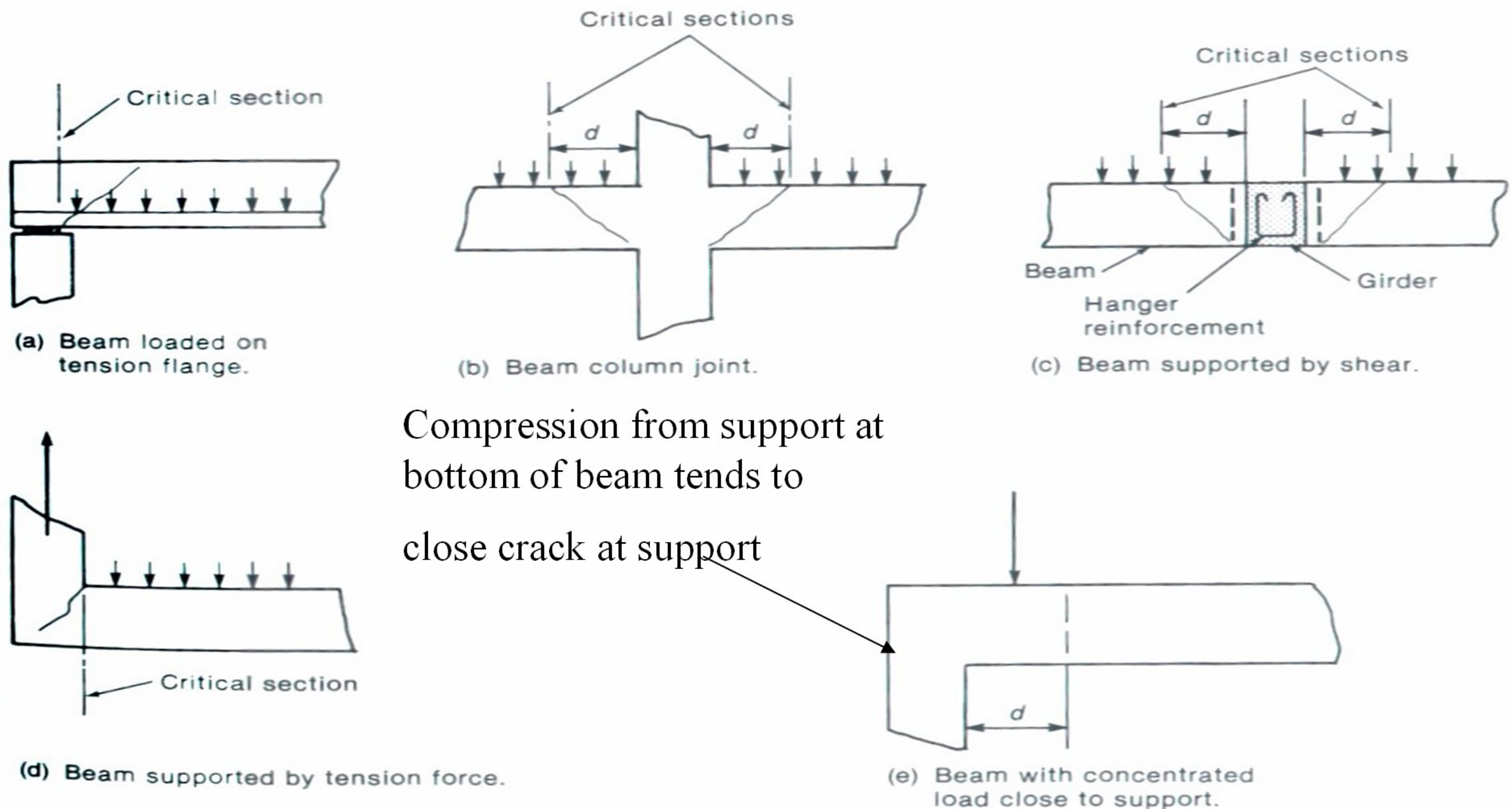
Non-pre-stressed members:

Compression fan carries  
load directly into support.

Sections located less than a distance  $d$  from face of support may be designed for same shear,  $V_u$ , as the computed at a distance  $d$ .

When:

1. The support reaction introduces compression into the end regions of the member.
2. The loads are applied at or near the top of the beam.
3. No concentrated load occurs within  $d$  from face of support .



Compression from support at bottom of beam tends to close crack at support

## 4.2.4 Development Length

**12.2.1** — Development length for deformed bars and deformed wire in tension,  $\ell_d$ , shall be determined from either 12.2.2 or 12.2.3 and applicable modification factors of 12.2.4 and 12.2.5, but  $\ell_d$  shall not be less than 300 mm.

**12.2.2** — For deformed bars or deformed wire,  $\ell_d$  shall be as follows:

Spacing and cover	No. 19 and smaller bars and deformed wires	No. 22 and larger bars
Clear spacing of bars or wires being developed or spliced not less than $d_b$ , clear cover not less than $d_b$ , and stirrups or ties throughout $\ell_d$ not less than the Code minimum or Clear spacing of bars or wires being developed or spliced not less than $2d_b$ and clear cover not less than $d_b$	$\left( \frac{f_y \psi_t \psi_e}{2.1 \lambda \sqrt{f'_c}} \right) d_b$	$\left( \frac{f_y \psi_t \psi_e}{1.7 \lambda \sqrt{f'_c}} \right) d_b$
Other cases	$\left( \frac{f_y \psi_t \psi_e}{1.4 \lambda \sqrt{f'_c}} \right) d_b$	$\left( \frac{f_y \psi_t \psi_e}{1.1 \lambda \sqrt{f'_c}} \right) d_b$

**12.2.3** — For deformed bars or deformed wire,  $\ell_d$  shall be

$$\ell_d = \left( \frac{f_y}{1.1 \lambda \sqrt{f'_c}} \frac{\psi_t \psi_e \psi_s}{\left( \frac{c_b + K_{tr}}{d_b} \right)} \right) d_b \quad (12-1)$$

in which the confinement term  $(c_b + K_{tr})/d_b$  shall not be taken greater than 2.5, and

$$K_{tr} = \frac{40 A_{tr}}{sn} \quad (12-2)$$


where  $n$  is the number of bars or wires being spliced or developed along the plane of splitting. It shall be permitted to use  $K_{tr} = 0$  as a design simplification

(a) Where horizontal reinforcement is placed such that more than 300 mm of fresh concrete is cast below the development length or splice,  $\psi_t = 1.3$ . For other situations,  $\psi_t = 1.0$ .

(c) For No. 19 and smaller bars and deformed wires,  $\psi_s = 0.8$ . For No. 22 and larger bars,  $\psi_s = 1.0$ .

Why do we need bar splices? -- for long spans

### Types of Splices

1. Butted & Welded
  2. Mechanical Connectors
  3. Lab Splices
- Must develop 125% of yield strength
- 

## Class A Splice

(ACI

12.15.2)

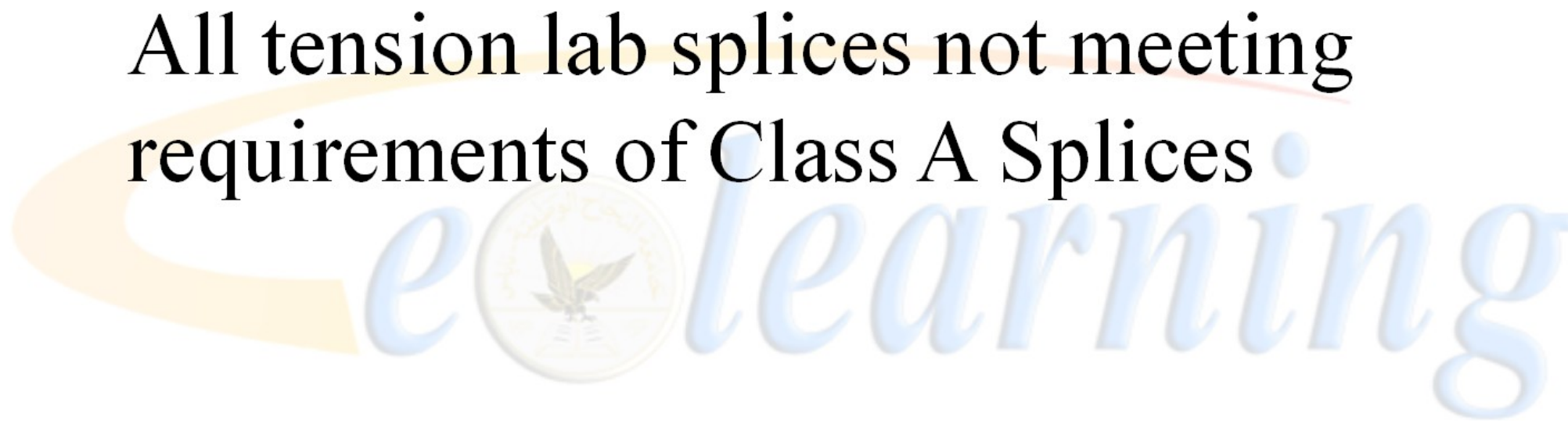
When  $\frac{A_{s(\text{provided})}}{A_{s(\text{req'd})}} \geq 2$  over entire splice length.

and 1/2 or less of total reinforcement is spliced within the req'd lap length.

## Class B Splice 12.15.2)

(ACI

All tension lap splices not meeting  
requirements of Class A Splices



# Tension Lap Splice (ACI 12.15)

As,prov/As,req'd	%As Spliced	Splice Class	Lap, req'd	Notes
$\geq 2.0$	$\leq 50$	A	$l_d$	Desirable
	$> 50$	B	$1.3 l_d$	ok
$< 2.0$	$\leq 50$	B	$1.3 l_d$	ok
	$> 50$	B	$1.3 l_d$	Avoid

where  $A_{s (req'd)}$  = determined for bending

$l_d$  = development length for bars (not allowed to use excess reinforcement modification factor)

$l_d$  must be greater than or equal to 30cm

Lab Splices should be placed in away from regions of high tensile stresses -locate near points of inflection (ACI R12.15.2)

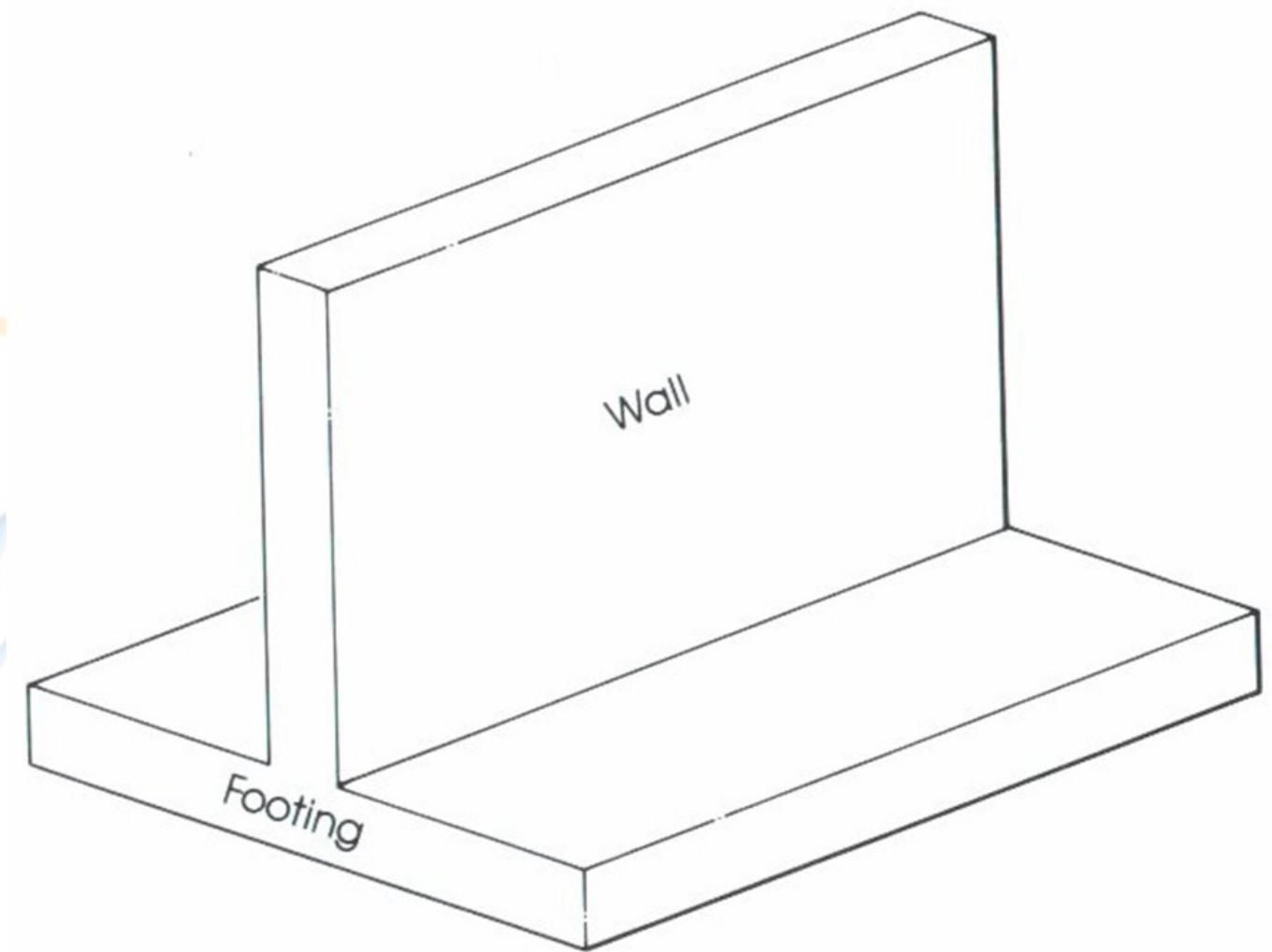
**End of 4.2.2-5**

Let Learning Continue

### Definition

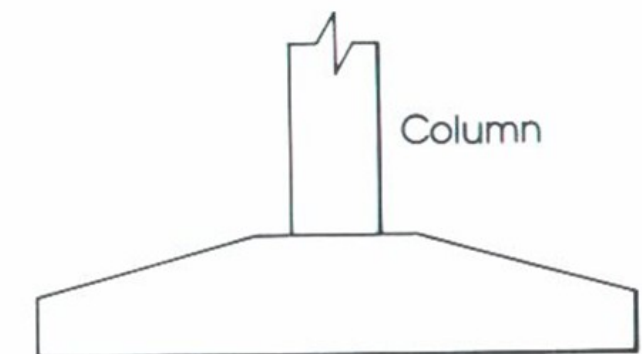
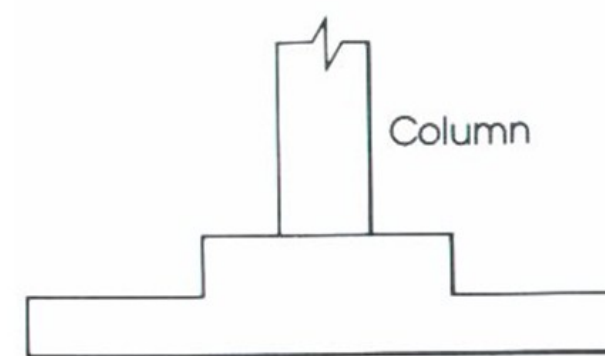
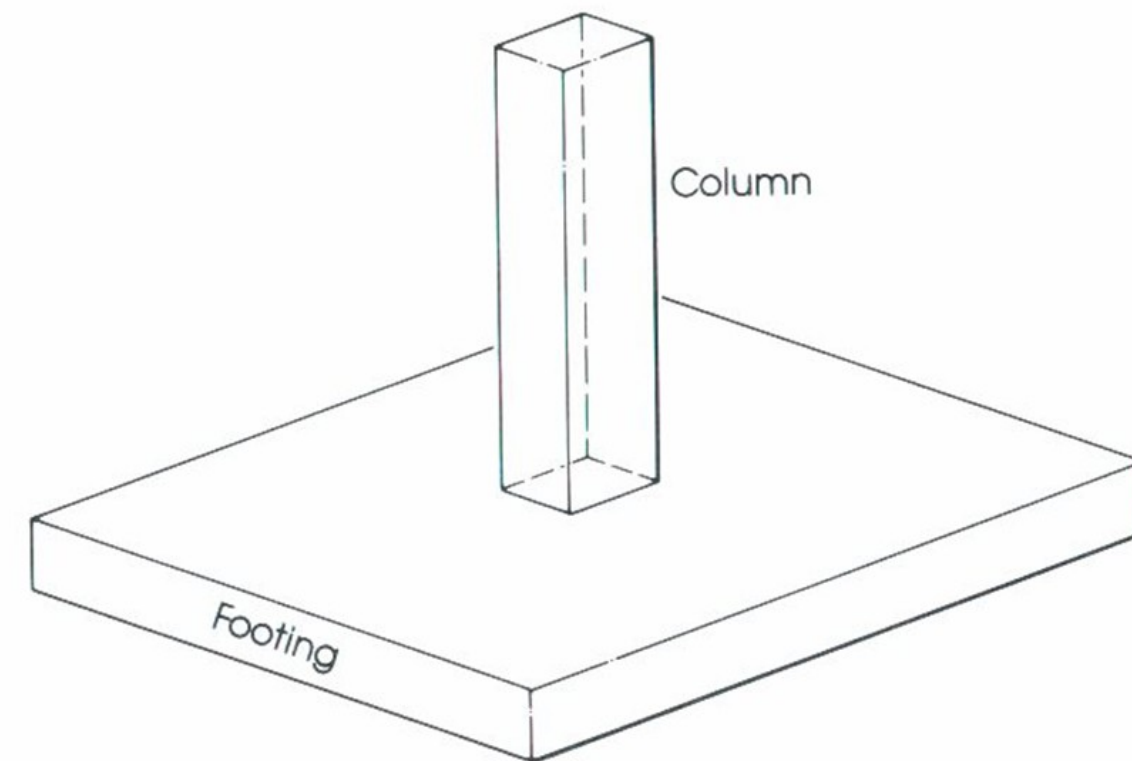
Footings are structural members used to support columns and walls and to transmit and distribute their loads to the soil in such a way that the load bearing capacity of the soil is not exceeded, excessive settlement, differential settlement, or rotation are prevented and adequate safety against overturning or sliding is maintained.

*Wall footings* are used to support structural walls that carry loads for other floors or to support nonstructural walls.



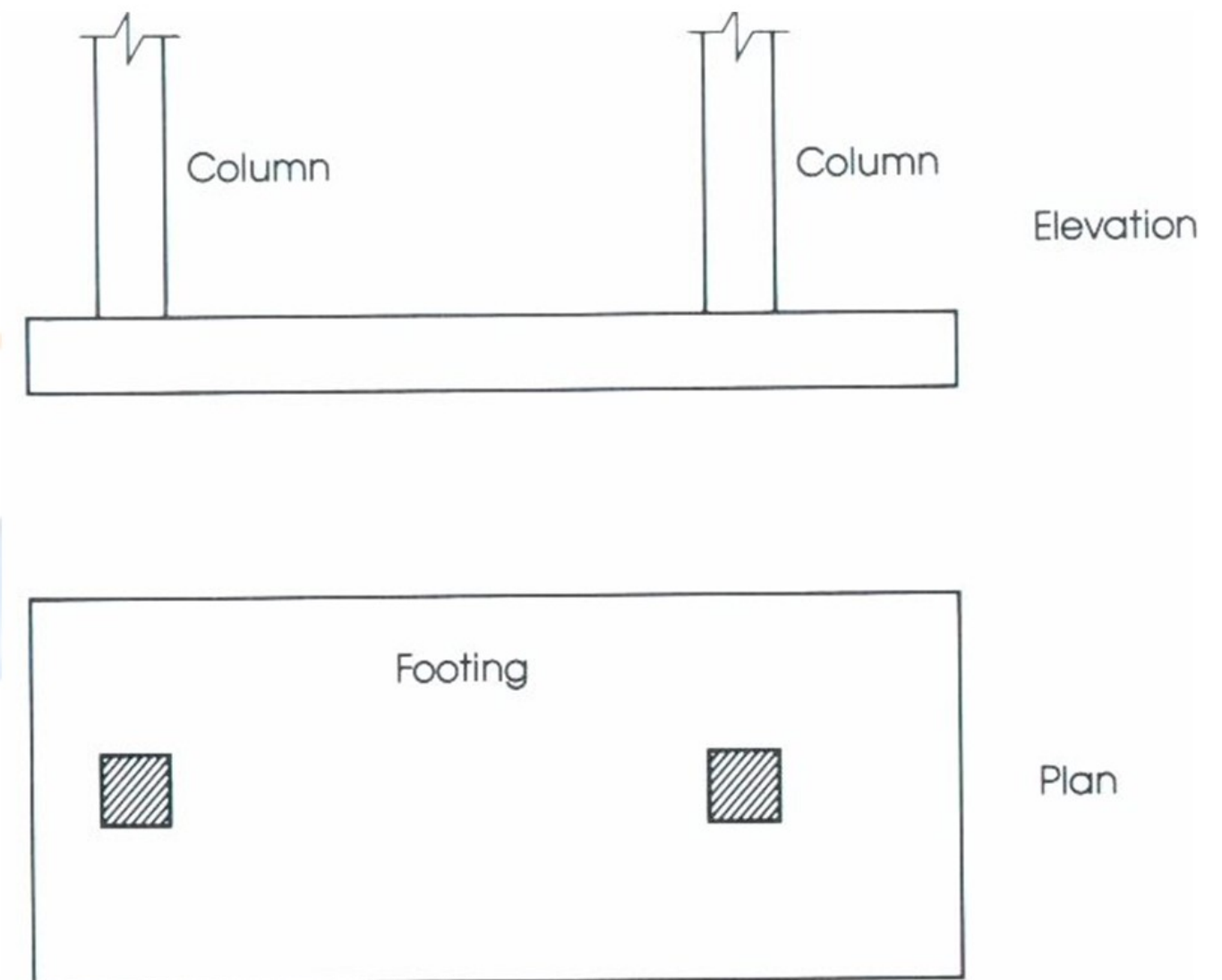
Wall footing.

*Isolated or single footings* are used to support single columns. This is one of the most economical types of footings and is used when columns are spaced at relatively long distances.

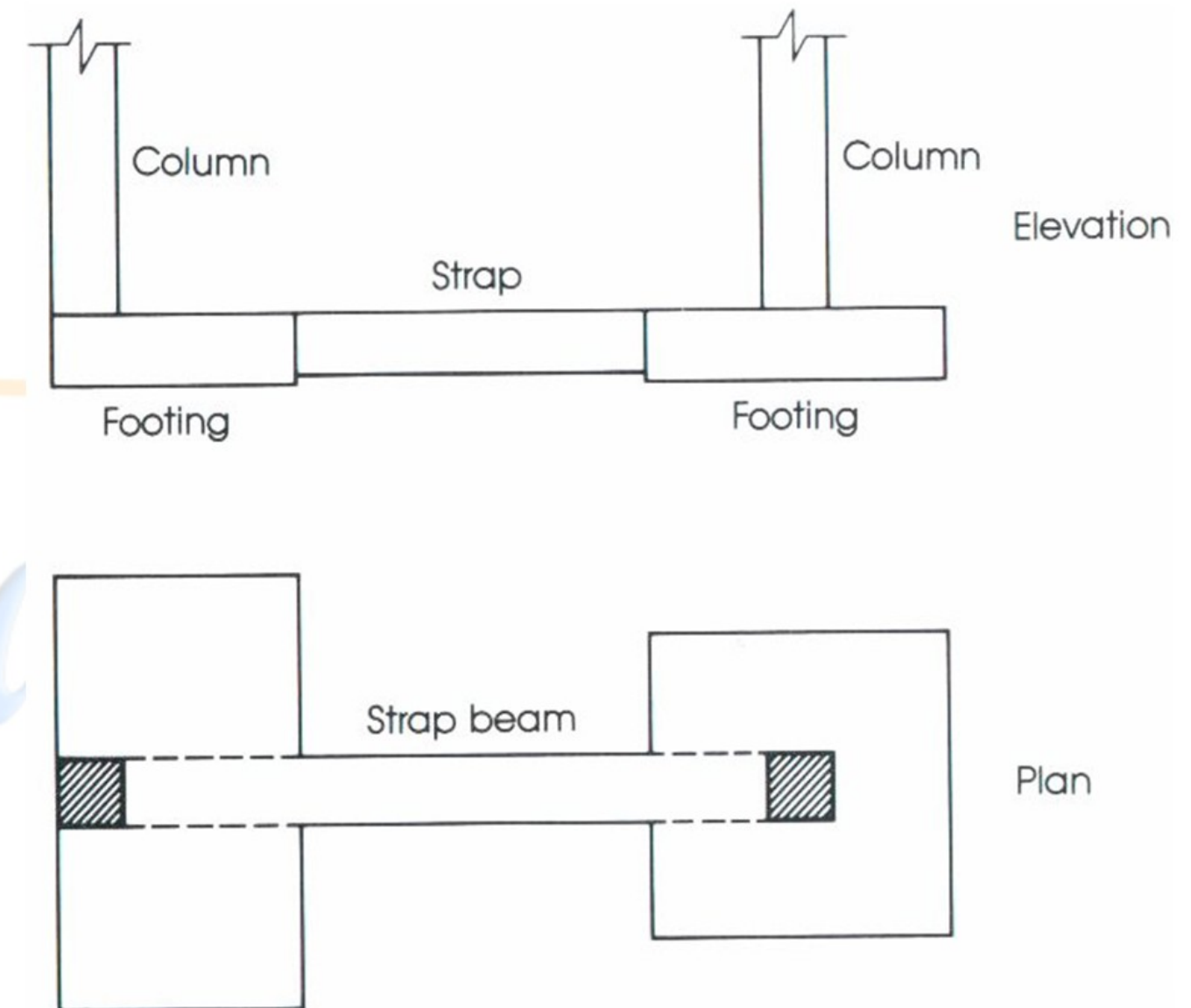


***Combined footings*** usually support two columns, or three columns not in a row.

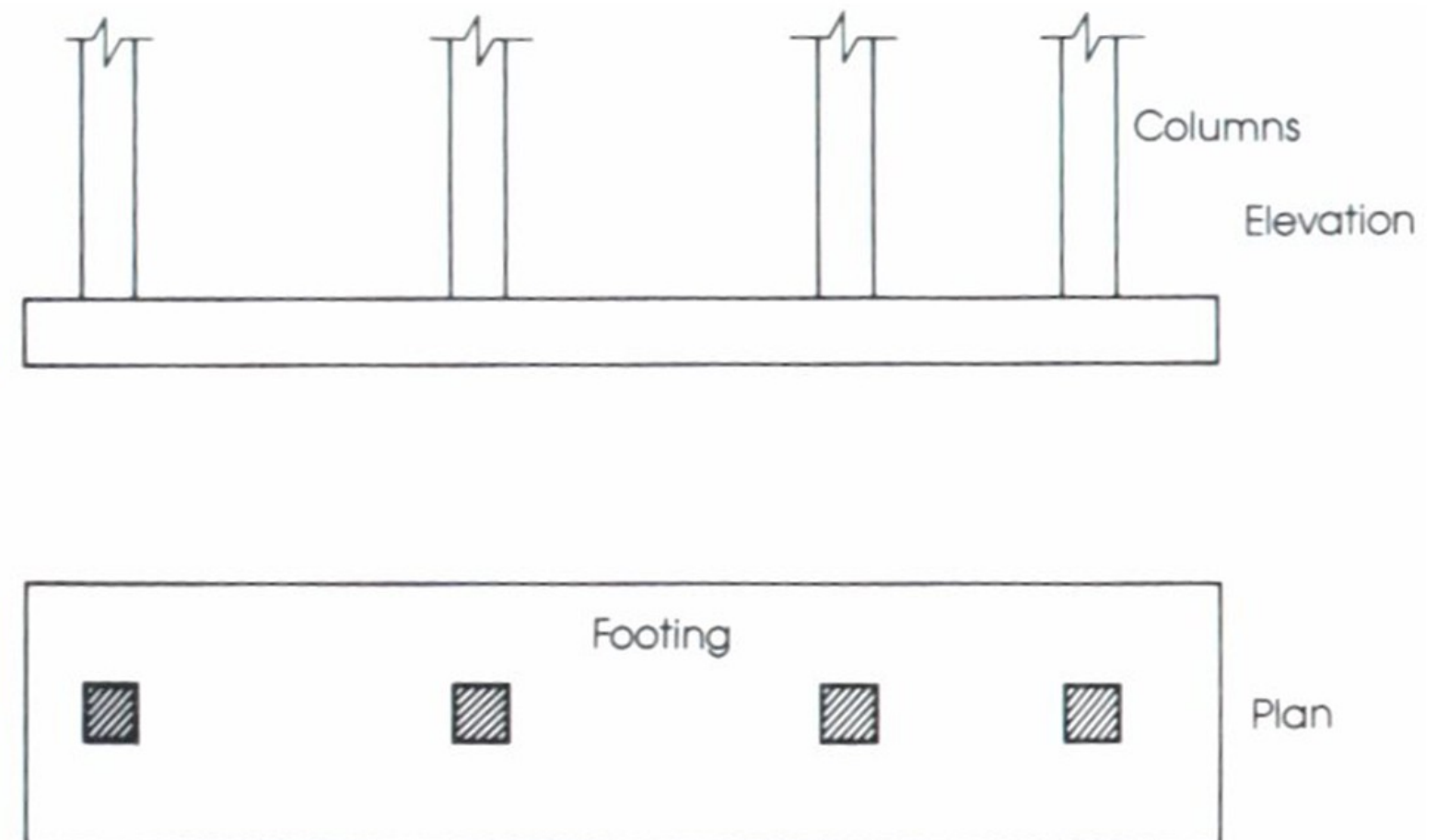
Combined footings are used when two columns are so close that single footings cannot be used or when one column is located at or near a property line.



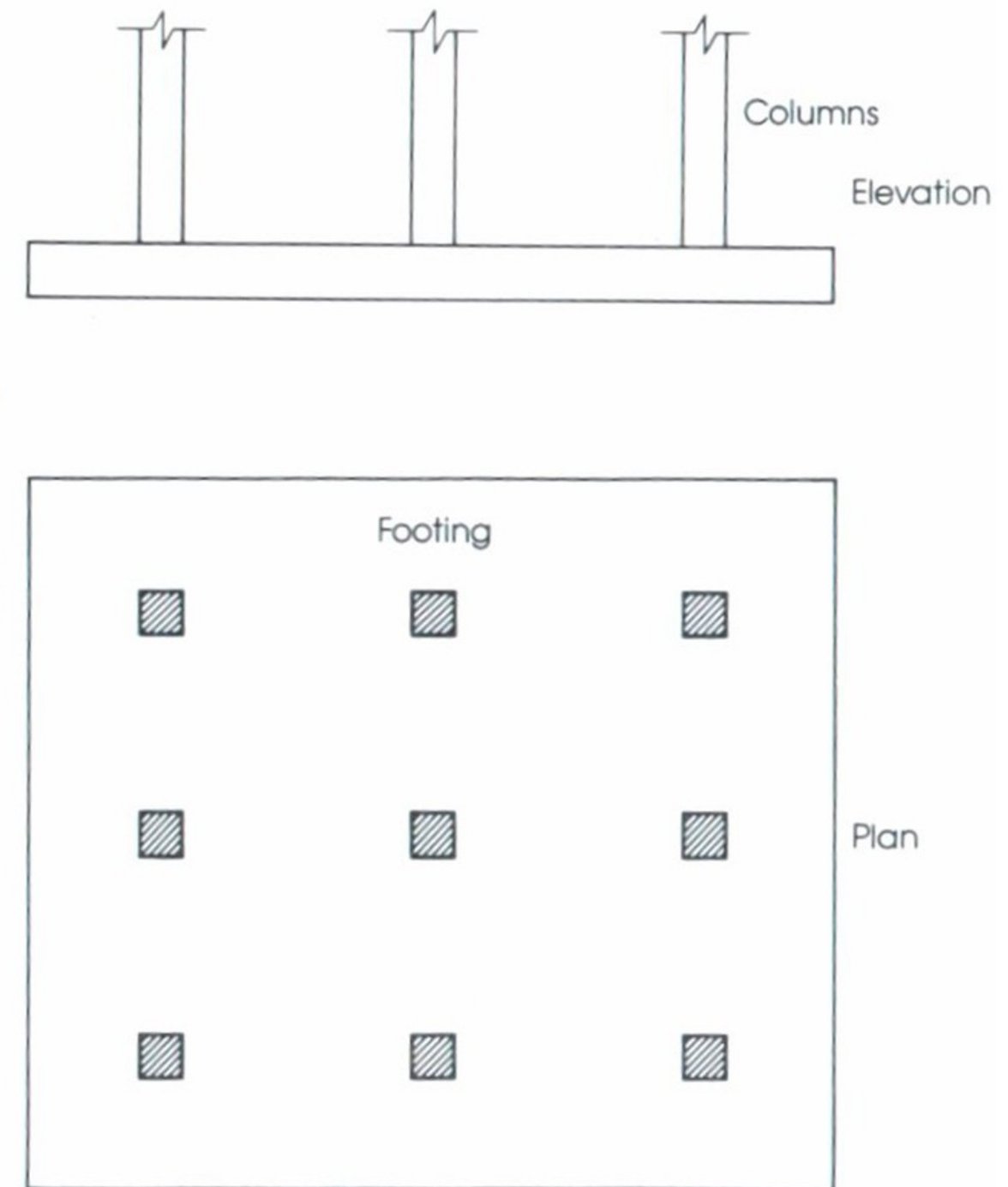
***Cantilever or strap footings*** consist of two single footings connected with a beam or a strap and support two single columns. This type replaces a combined footing and is more economical.



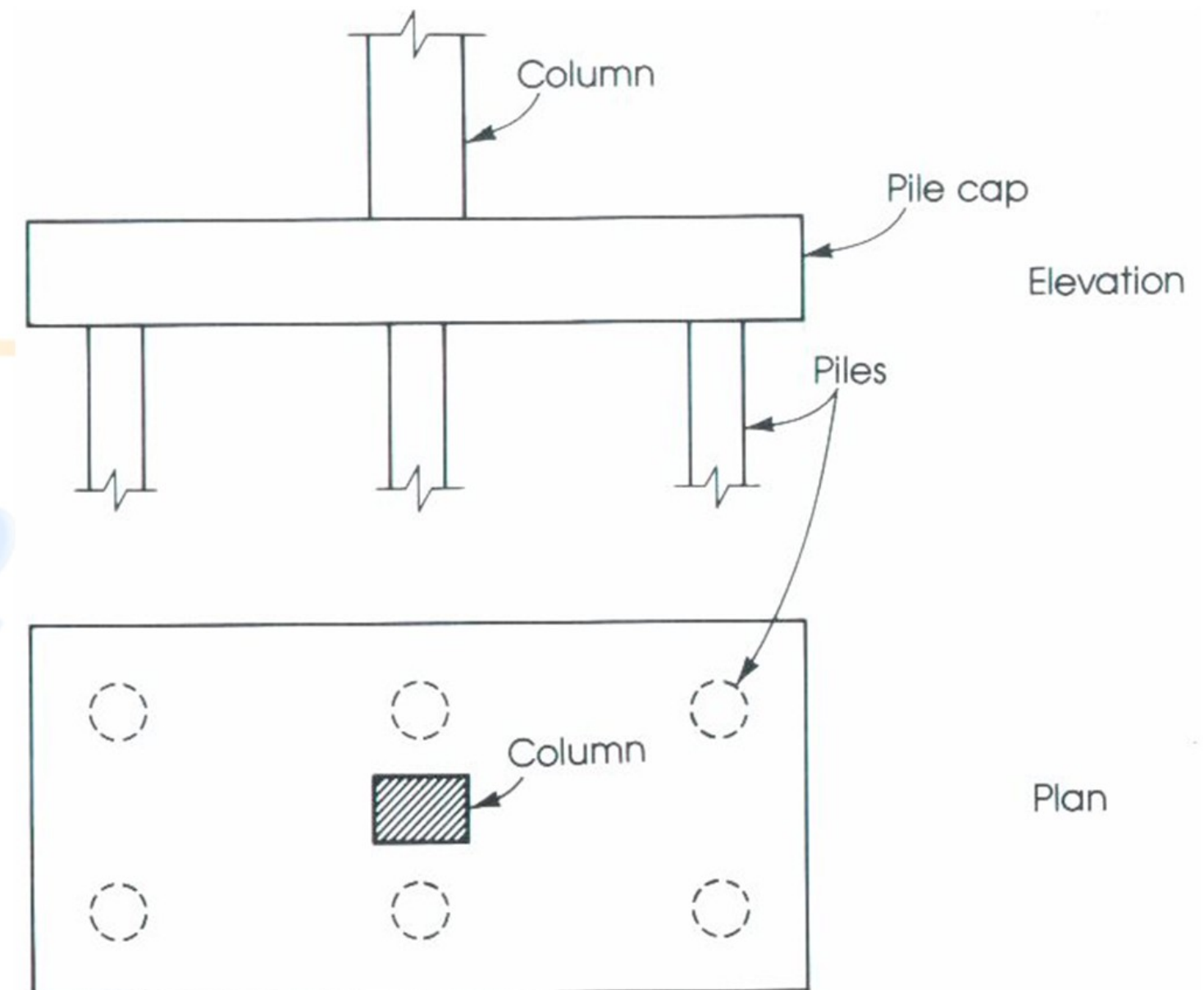
***Continuous footings*** support a row of three or more columns. They have limited width and continue under all columns.



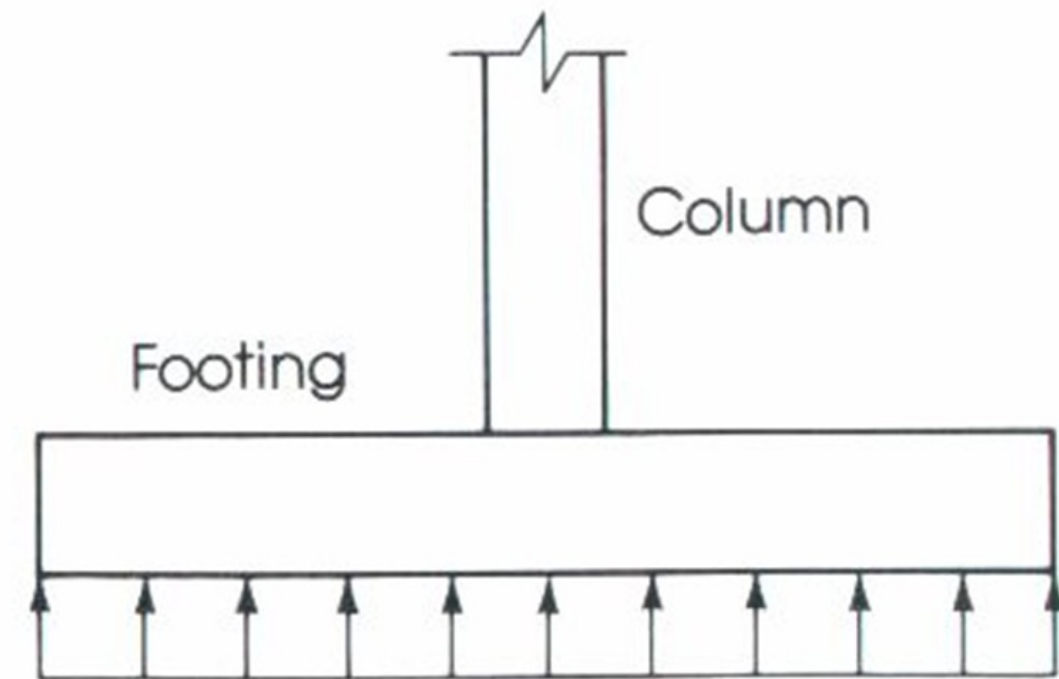
***Rafted or mat foundation*** consists of one footing usually placed under the entire building area. They are used, when soil bearing capacity is low, column loads are heavy, single footings cannot be used, piles are not used and differential settlement must be reduced.



***Pile caps*** are thick slabs used to tie a group of piles together to support and transmit column loads to the piles.



When the column load  $P$  is applied on the centroid of the footing, a uniform pressure is assumed to develop on the soil surface below the footing area.



However the actual distribution of the soil is not uniform, but depends on many factors especially the composition of the soil and degree of flexibility of the footing.

Footings must be designed to carry the column loads and transmit them to the soil safely while satisfying code limitations.

1. The area of the footing based on the allowable bearing soil capacity
2. Two-way shear or punch out shear.
3. One-way wide beam shear
4. Bending moment and steel reinforcement required

## Size of Footings

The area of footing can be determined from the actual external loads such that the allowable soil pressure is not exceeded.

$$\text{Area of footing} = \frac{\text{Total load (including self - weight)}}{\text{allowable soil pressure}}$$

Strength design requirements

$$q_u = \frac{P_u}{\text{area of footing}}$$

For two-way shear in slabs (& footings)  $V_c$  is smallest of

$$V_c = \left( 1 + \frac{2}{\beta_c} \right) \frac{\sqrt{f_c}}{6} b_0 d \quad \text{ACI 11-31}$$

where,  $\beta_c =$  long side/short side of column concentrated load or reaction area  $< 2$

$b_0 =$  length of critical perimeter around the column

When  $\beta_c > 2$  the allowable  $V_c$  is reduced.



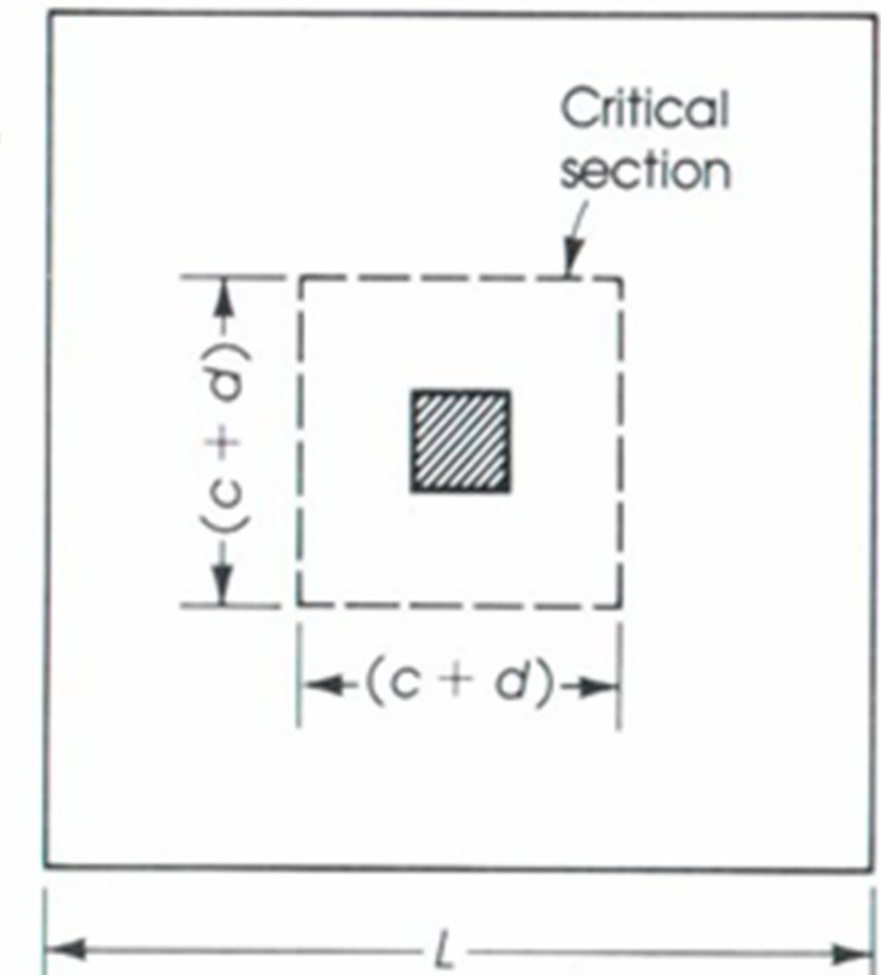
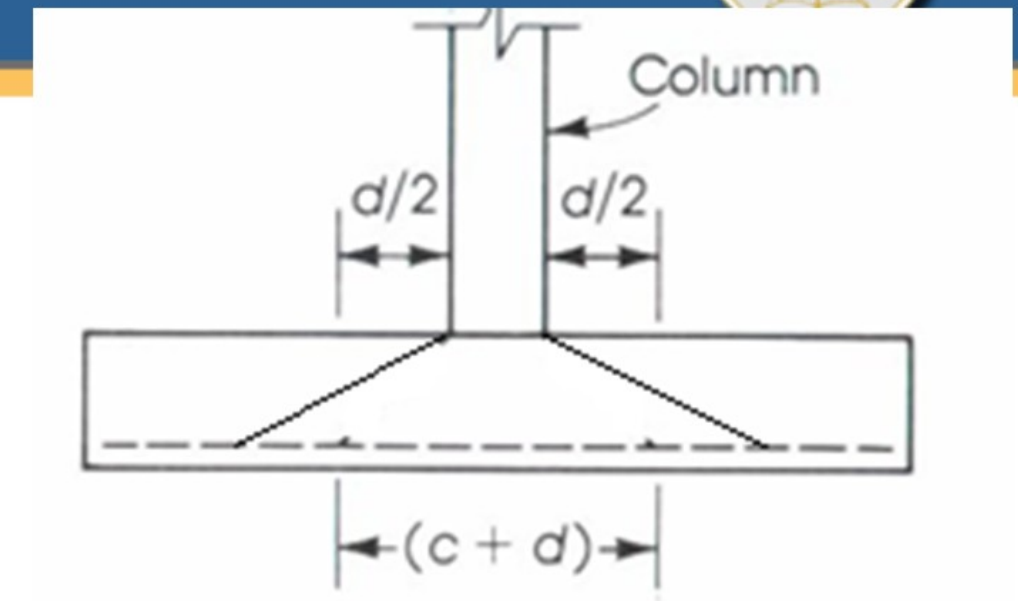
1. Assume  $d$ .
2. Determine  $b_0$ .

$$b_0 = 4(c+d)$$

for square columns  
where one side =  $c$

$$b_0 = 2(c_1+d) + 2(c_2+d)$$

for rectangular  
columns of sides  $c_1$   
and  $c_2$ .

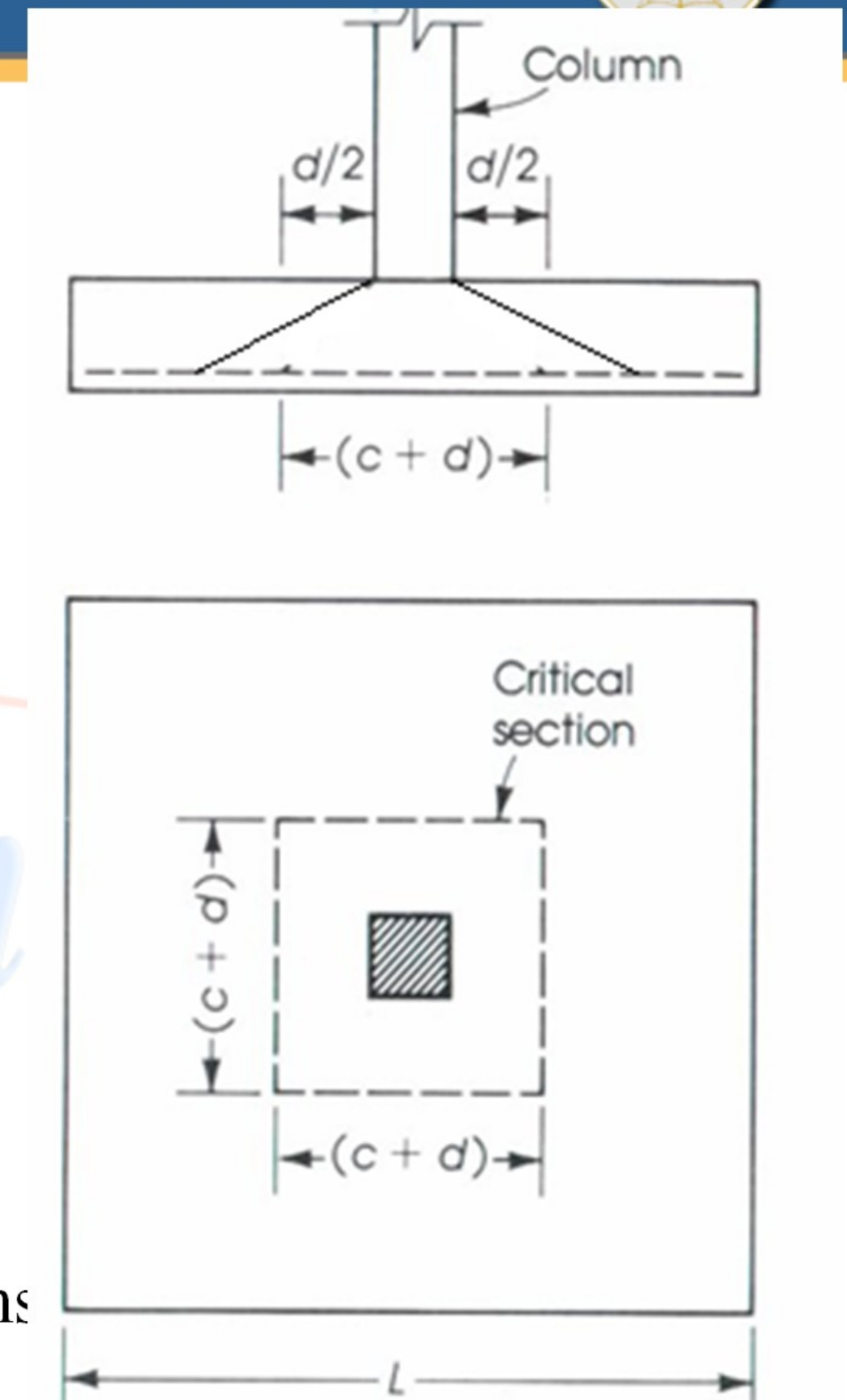




3. The shear force  $V_u$  acts at a section that has a length  $b_0 = 4(c+d)$  or  $2(c_1+d) + 2(c_2+d)$  and a depth  $d$ ; the section is subjected to a vertical downward load  $P_u$  and vertical upward pressure  $q_u$ .

$$V_u = P_u - q_u (c + d)^2 \text{ for square columns}$$

$$V_u = P_u - q_u (c_1 + d)(c_2 + d) \text{ for rectangular columns}$$



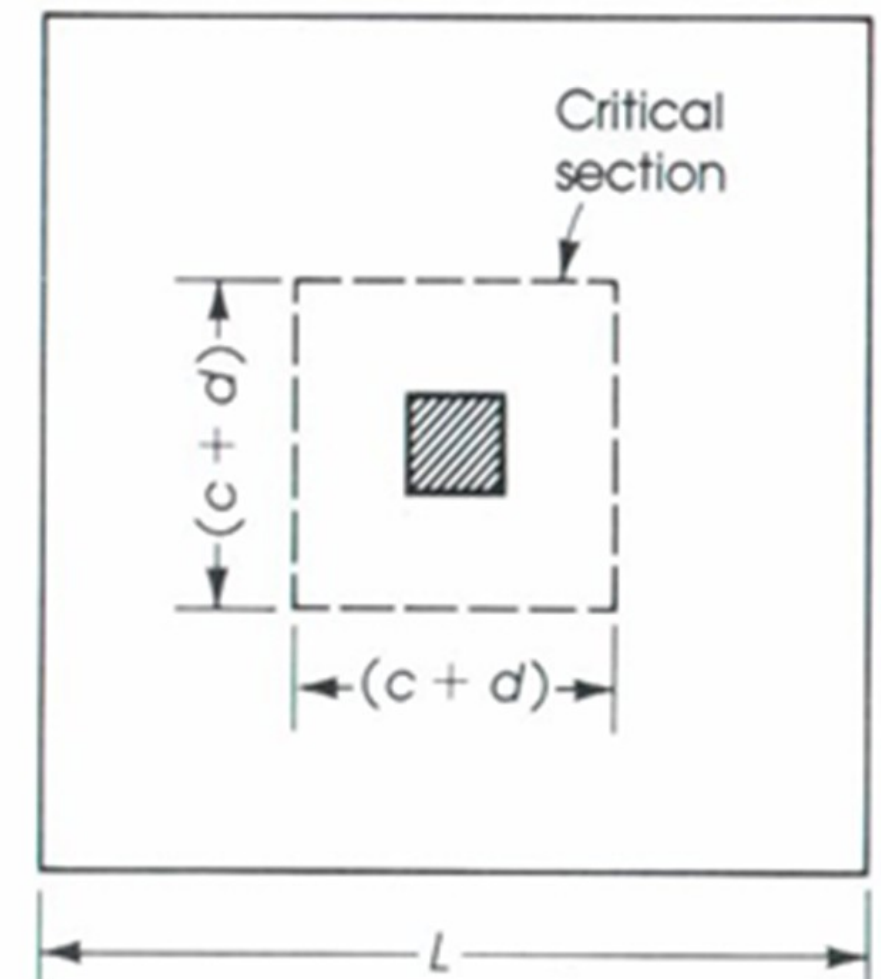
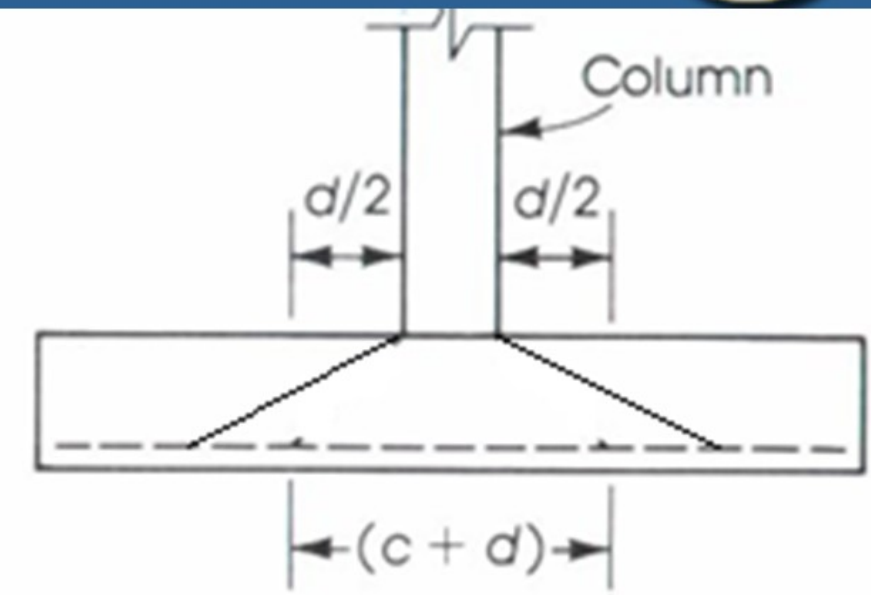


4. Allowable  $\phi V_c = \phi \frac{\sqrt{f_c}}{3} b_0 d$

Let  $V_u = \phi V_c$

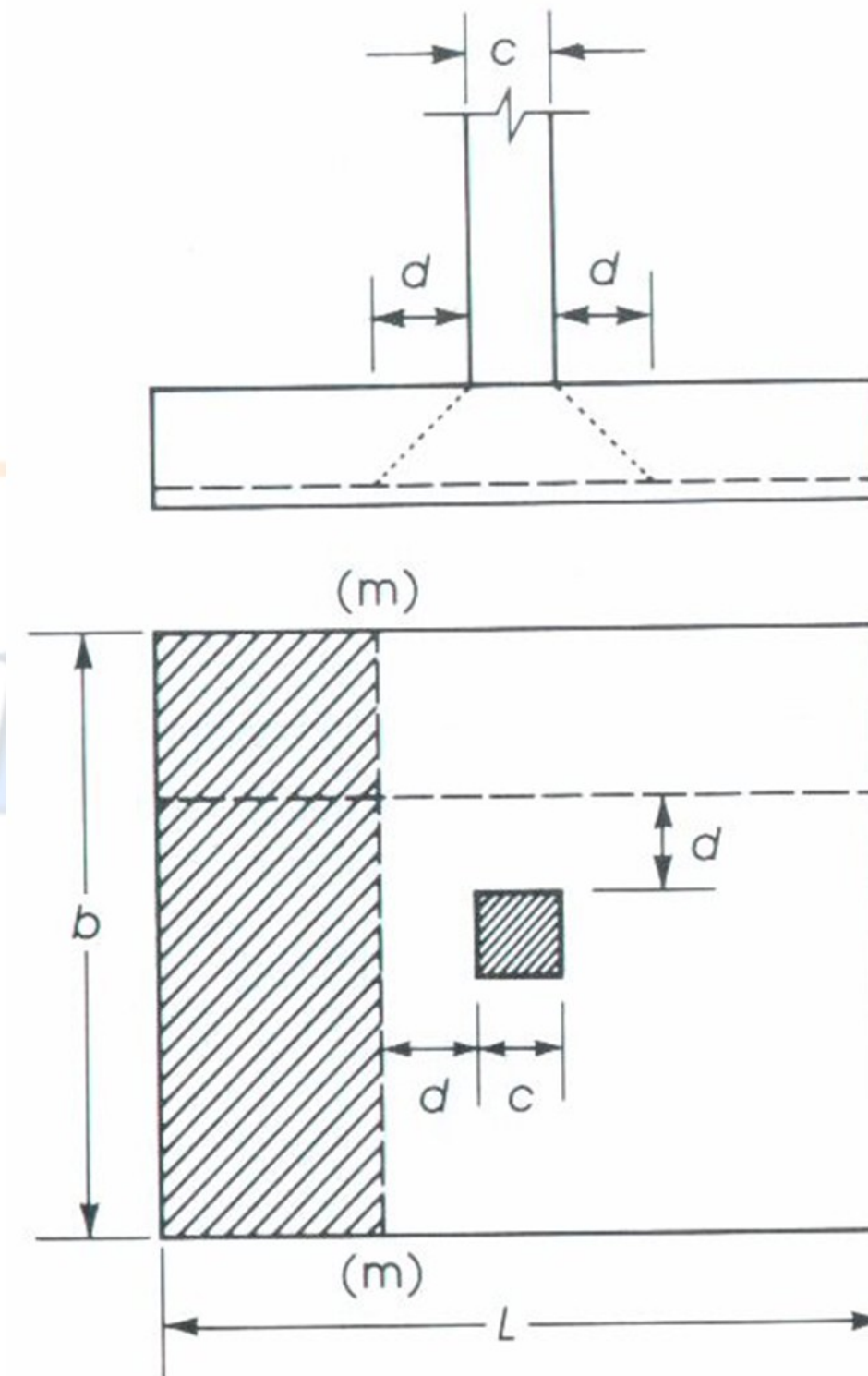
$$d = \frac{3V_u}{\phi \sqrt{f_c} b_0}$$

If  $d$  is not close to the assumed  $d$ ,  
revise your assumptions



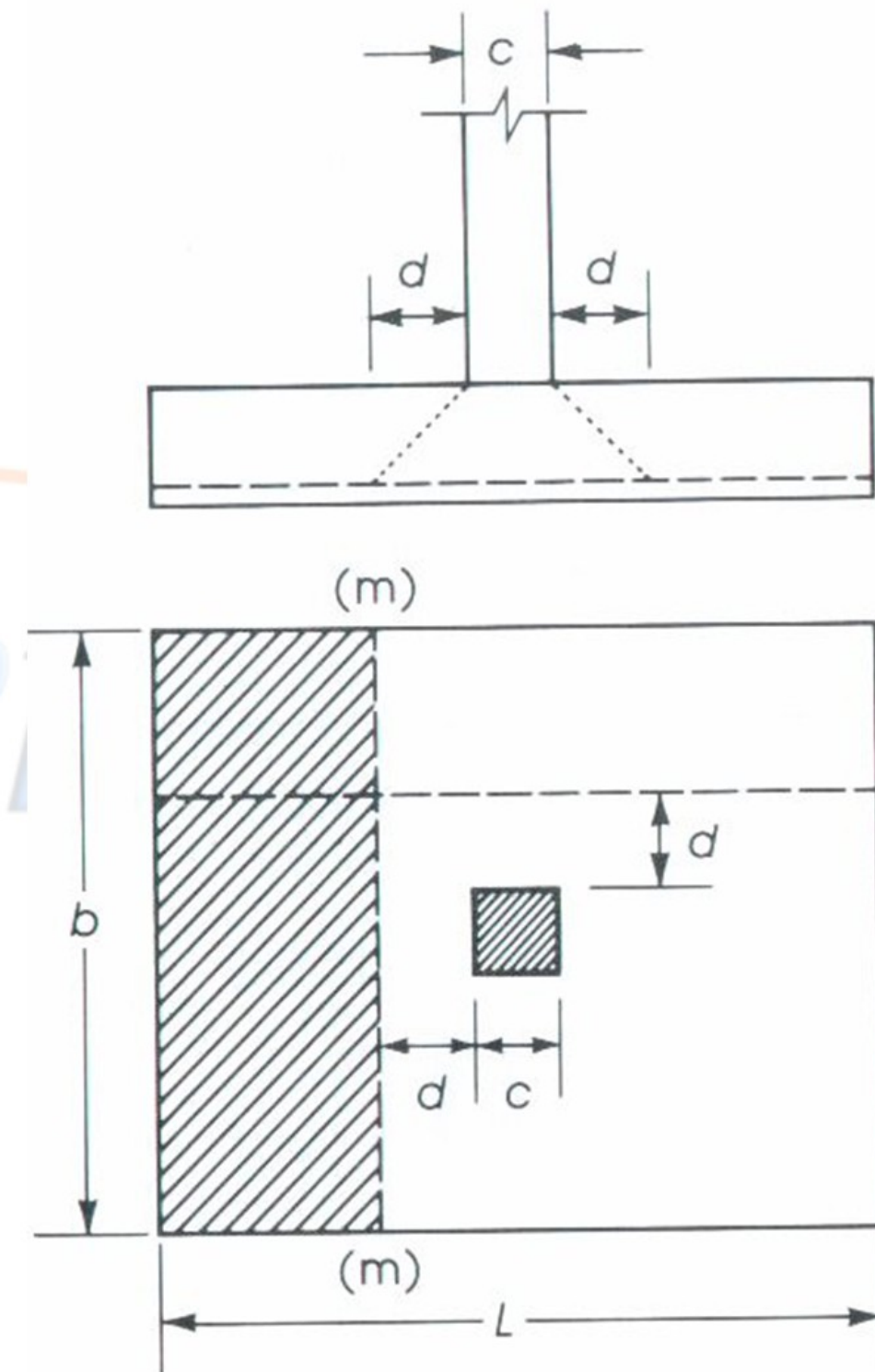
For footings with bending action in one direction the critical section is located a distance  $d$  from face of column

$$\phi V_c = \phi \frac{\sqrt{f_c}}{6} b d$$



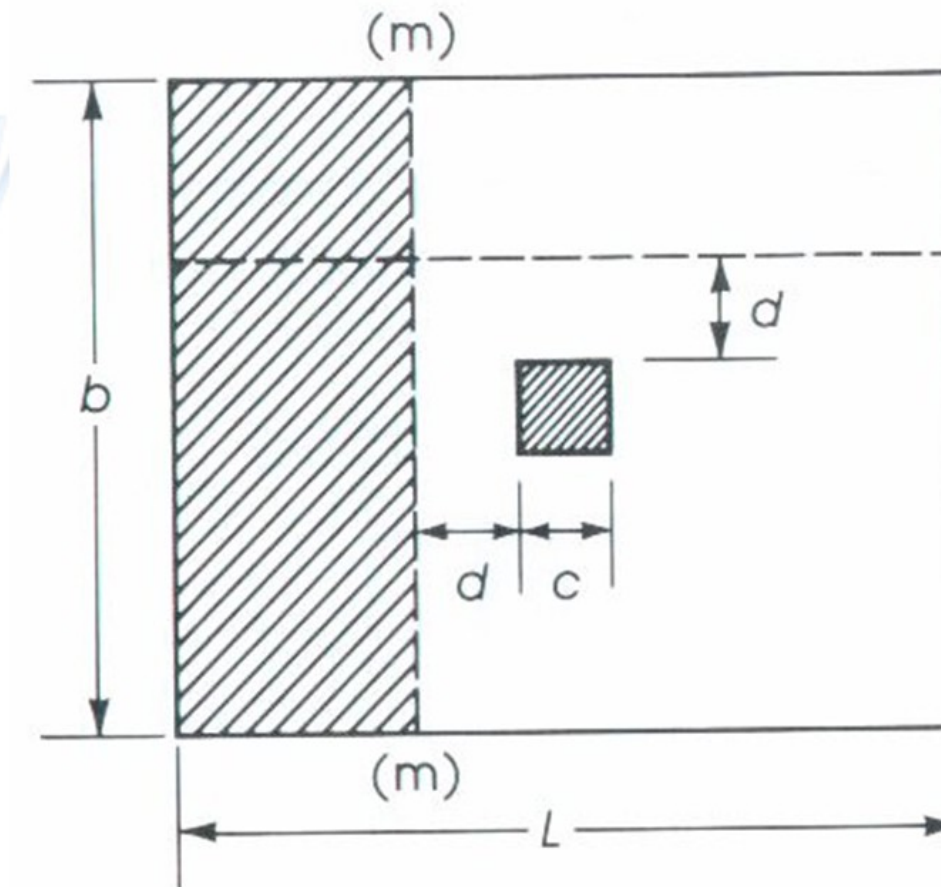
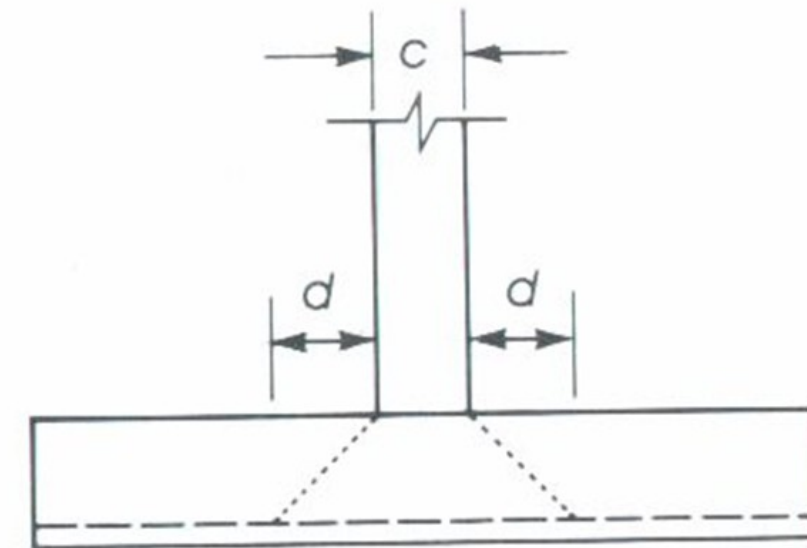
The ultimate shearing force at section m-m can be calculated

$$V_u = q_u b \left( \frac{L}{2} - \frac{c}{2} - d \right)$$



If no shear reinforcement is to be used, then  $d$  can be checked, assuming  $V_u = \phi V_c$

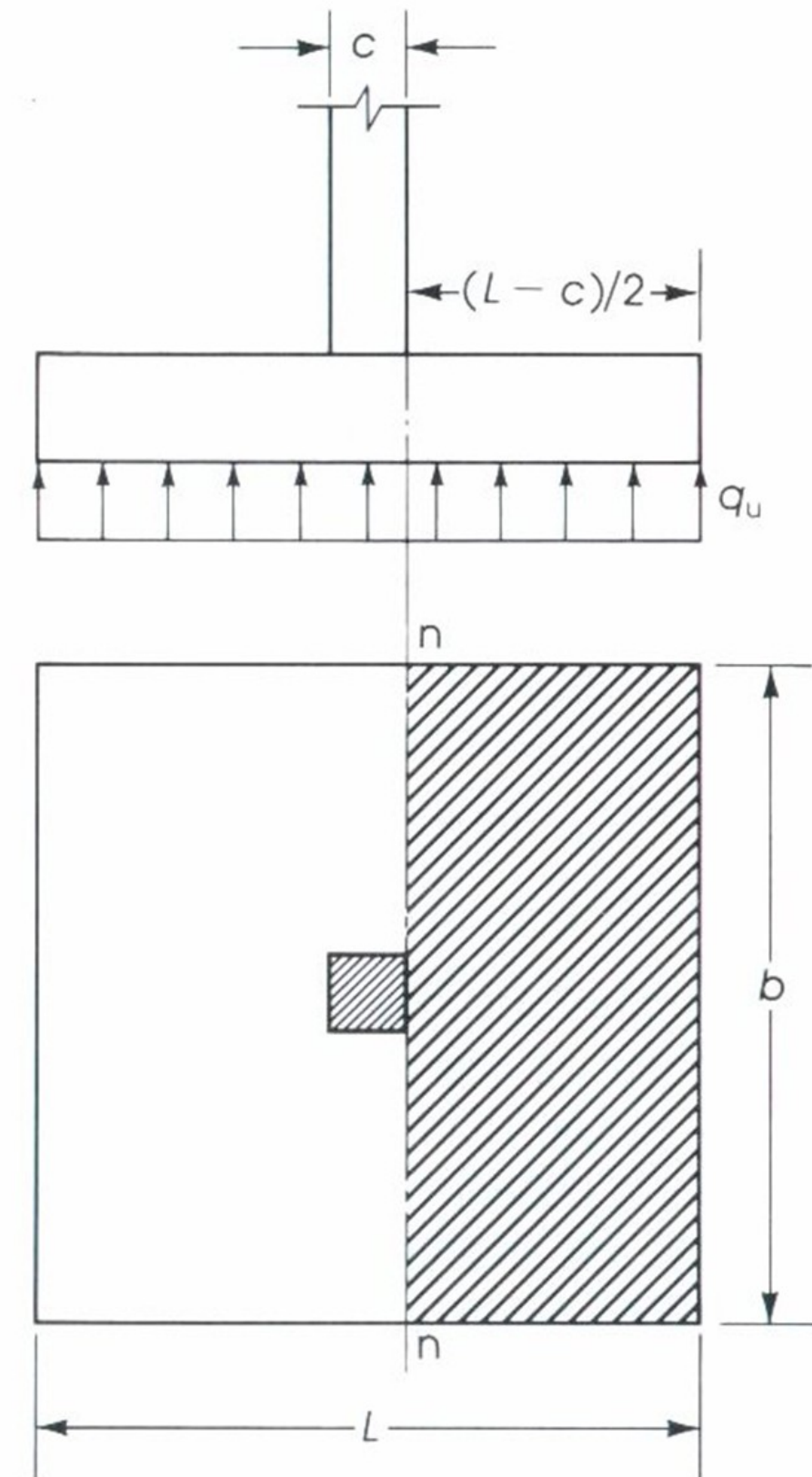
$$d = \frac{6V_u}{\phi \sqrt{f_c} b}$$





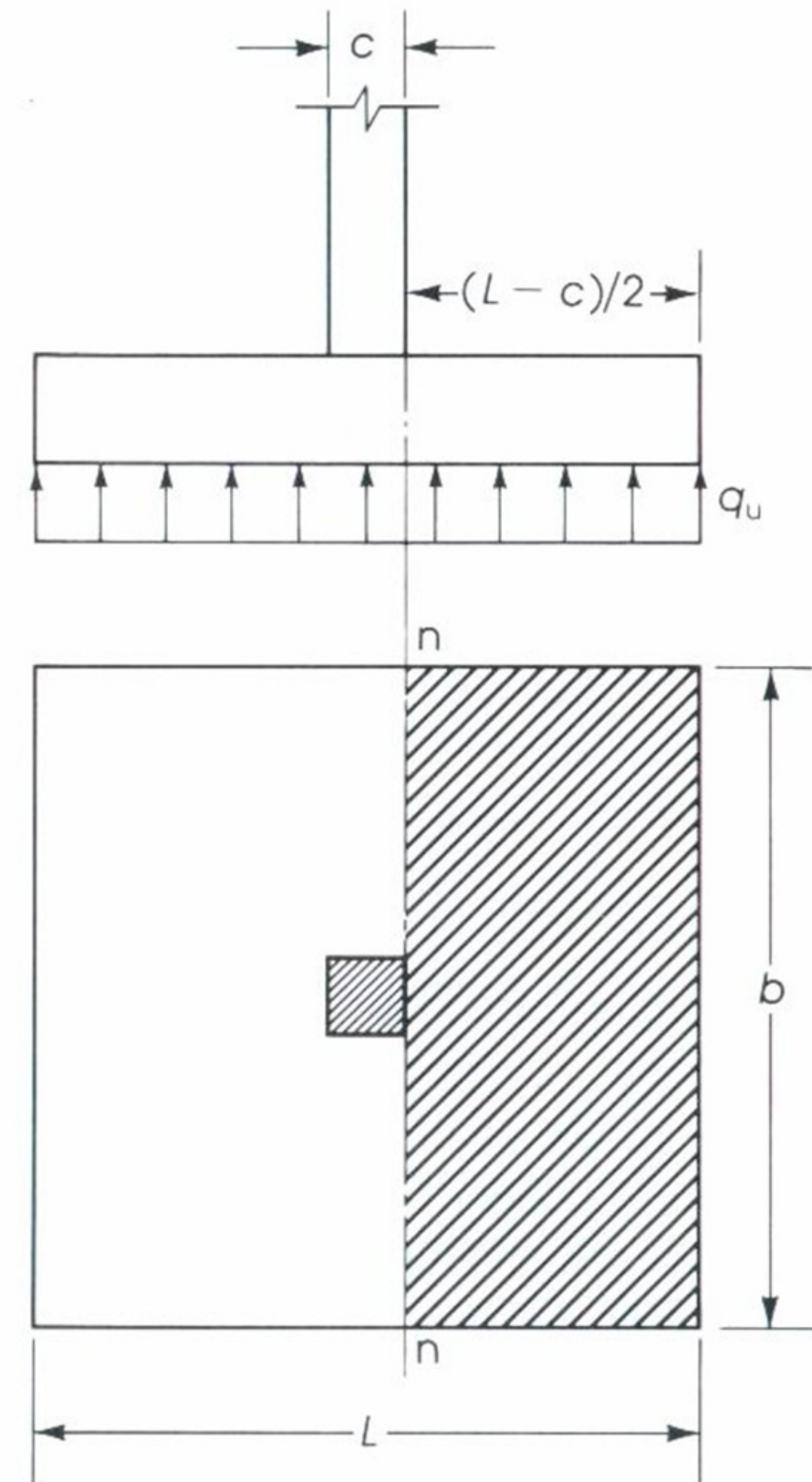
The bending moment in each direction of the footing must be checked and the appropriate reinforcement must be provided.

$$A_s = \frac{3M_u}{d}$$





The minimum steel percentage required shall be as required for shrinkage temperature reinforcement.



- Design a panel 4m by 5m supported on four columns.
  - Design the slab as one-way rib in the 4m direction. The superimposed load is  $3\text{kN/m}^2$ , the live load is  $3\text{kN/m}^2$
  - Design the beam, column and isolated footing to support four stories, concrete is B250 .
  - Soil allowable bearing capacity is  $350\text{kN/m}^2$

**End of chapter 4**

Let Learning Continue

5.1. Regular systems

5.2. Ribbed slab systems

5.3. Two way slab systems

If time permits

5.4. Systems without vertical continuity

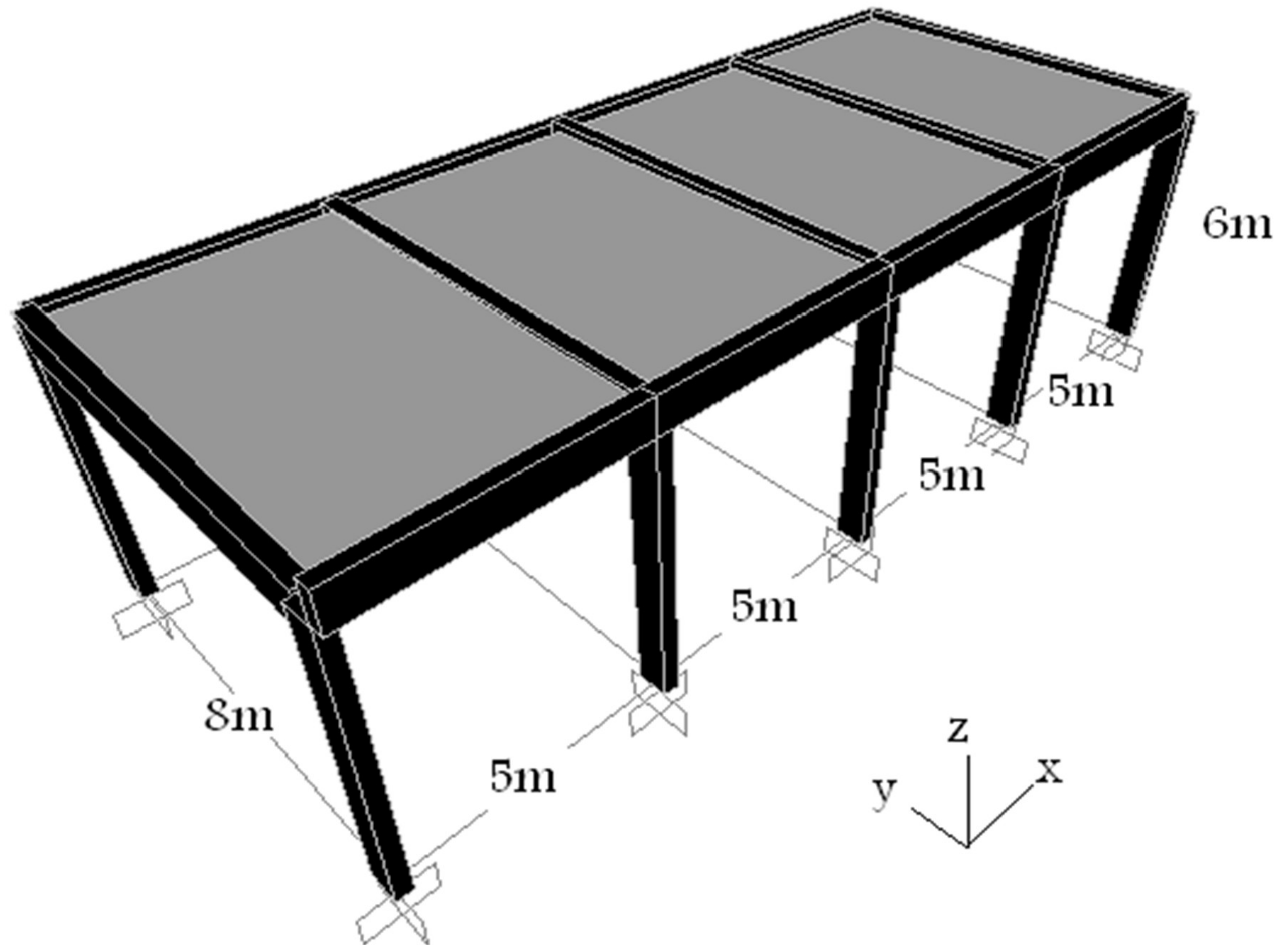
5.5. General shape building systems

## 5.1 Regular systems

Regular systems are those which have one way solid slab and vertical continuity; i.e. load of slab is transferred to beams, from beams to columns and then to footings.

Analysis of all systems are done using either 1D, 2D or 3D modeling.

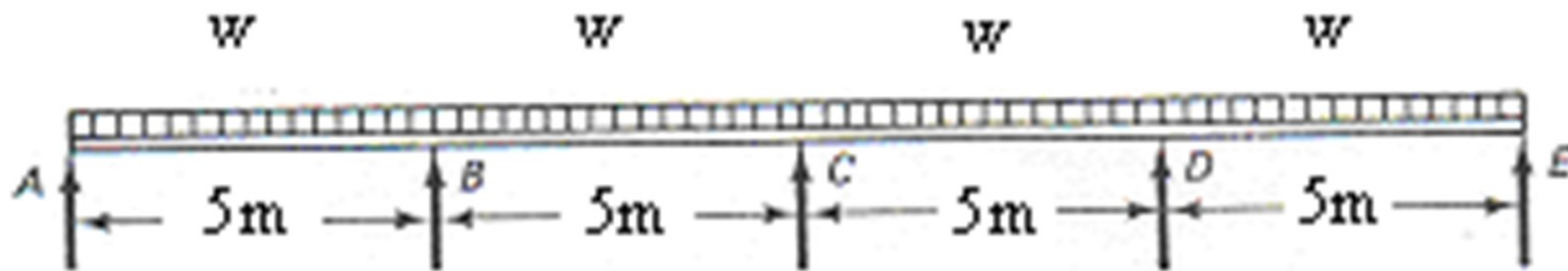
- 1-storey RC slab-beam factory structure shown next slide
- Fixed foundations, 4 spans 5m bays in x and a single 8m span in y, 6m elevation
- $E=24\text{GPa}$ ,  $\mu=0.2$ ,  $\rho=2.5\text{t/m}^3$
- Cylinder concrete strength=25MPa, steel yield=420MPa
- superimposed loads=5kN/m<sup>2</sup>, live load=9kN/m<sup>2</sup>



- Due to cracking of elements, use the following modifiers for gross inertia for 3D analysis (ACI R10.11.1):
  - Beam 0.35
  - Column 0.7
  - One way slab (0.35, 0.035)

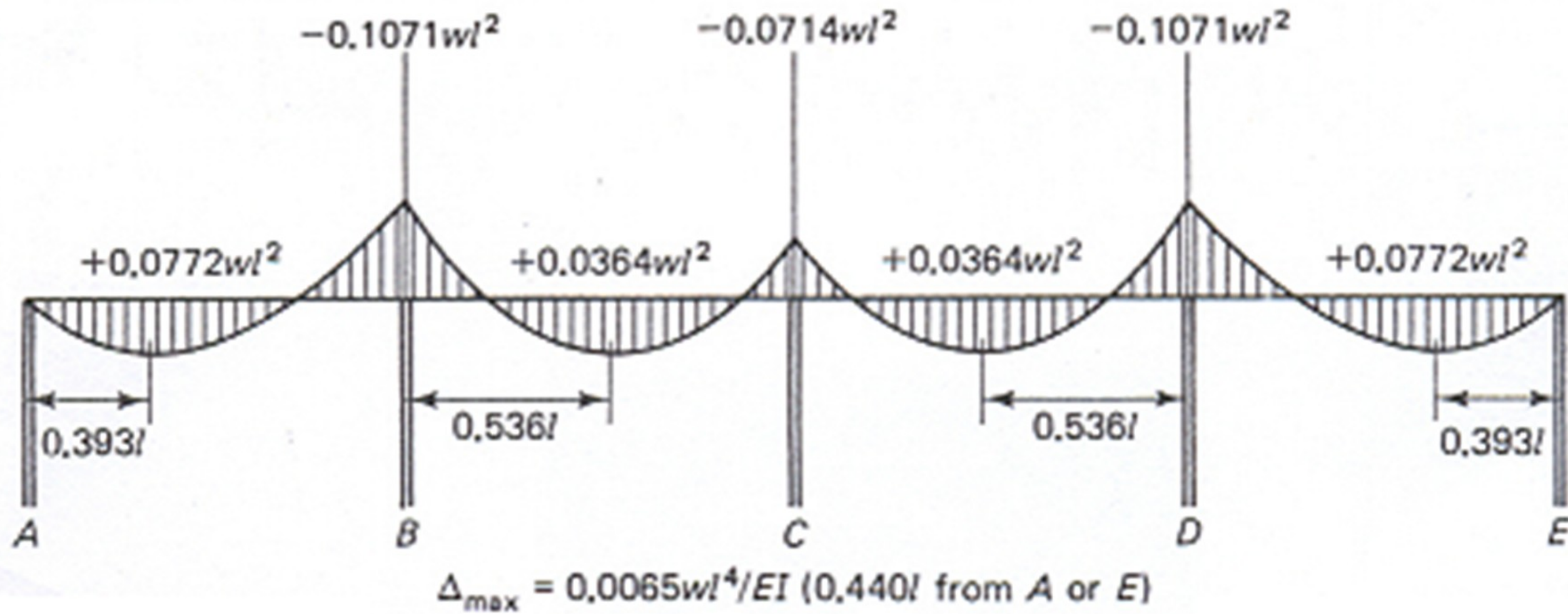
- Slab: According to ACI 9.5.2 thickness of slab= $500/24=20.83\text{cm}$ , but considering that concentrated loads might be placed at middle of slab, use 25cm thickness
- Beam:  $800/16=50\text{cm}$ , however beams fail by strength and not deflection, and because it is a factory use: drop beams 30cmX80cm (6cm cover)
- Columns: use 30X60cm reinforced on two faces (cover 4cm).

•





# 1D analysis and design: slab analysis

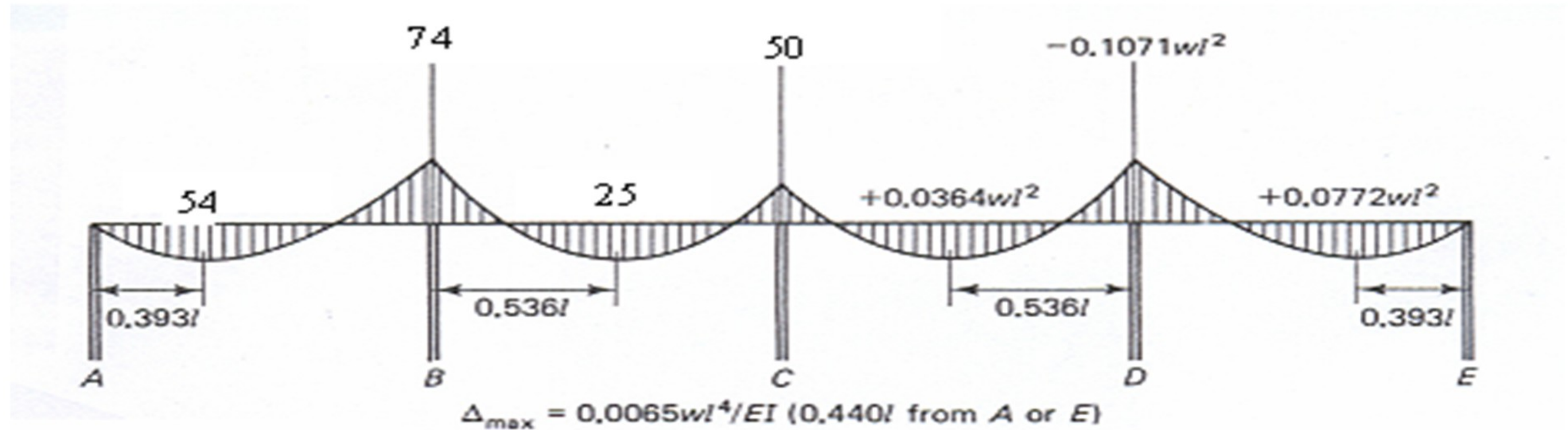


# 1D analysis and design: slab analysis

- $w_d = (.25 * 24.5 + 5) = 11.125 \text{ KN/m}$
- $w_l = 9 \text{ KN/m}$
- $w_u = 1.2 * 11.125 + 1.6 * 9 = 27.75 \text{ KN/m}$

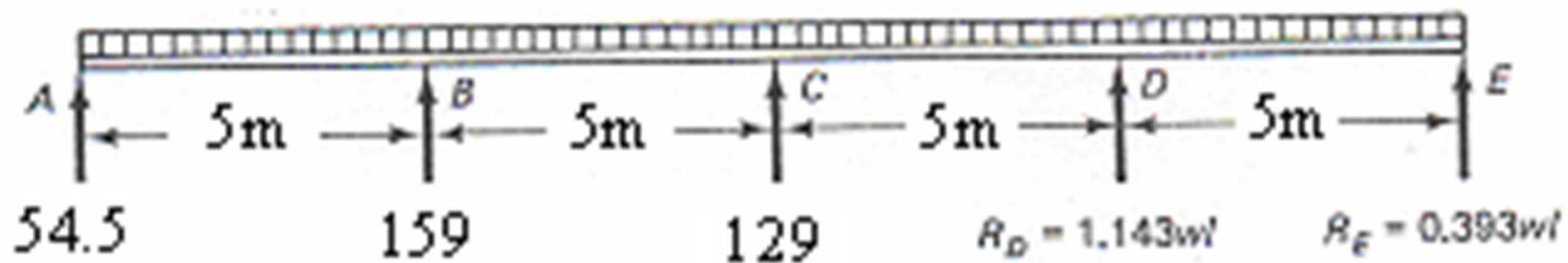
# 1D analysis and design: slab analysis, BM in KN.m

## As in square cm



$$A_s \approx \frac{3M_u}{20} = 0.15M_u \geq \frac{1.4}{420} (100 * 20) = 6.67$$

- Note: for slabs and footings of uniform thickness the minimum steel is that for temperature and shrinkage but with maximum spacing three times the thickness or 450mm. (ACI10.5.4)



# 1D analysis and design: beam analysis,

- Assume simply supported beam:
- Beam C,  $M_u = (129 + 1.2 * 0.3 * .8 * 24.5) * 8^2 / 8 = 1088$
- Beam B,  $M_u = (159 + 1.2 * 0.3 * .8 * 24.5) * 8^2 / 8 = 1328$
- Beam A,  $M_u = (54.5 + 1.2 * 0.3 * .8 * 24.5) * 8^2 / 8 = 492$

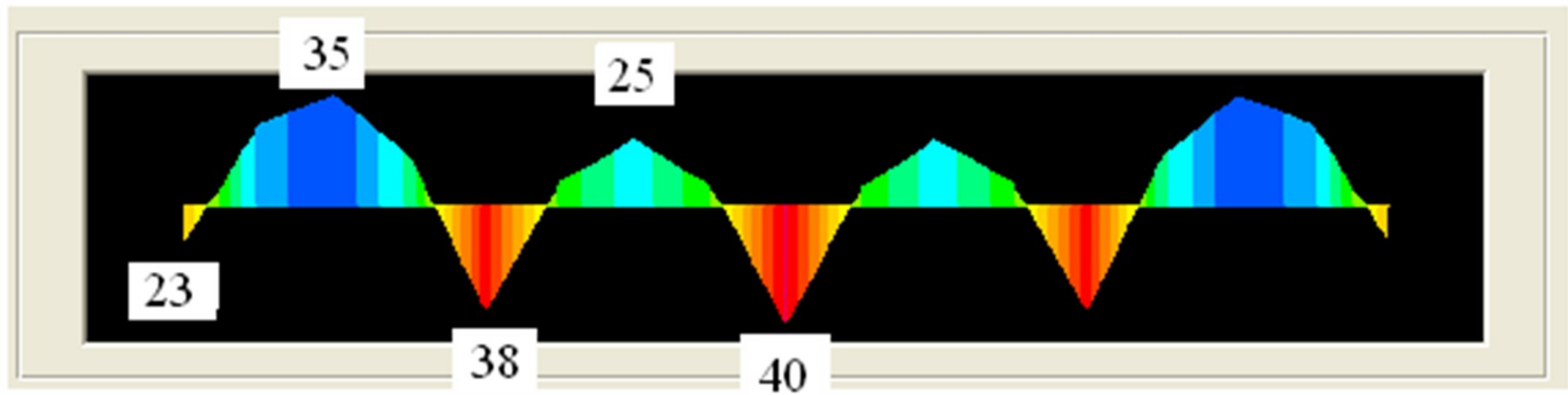
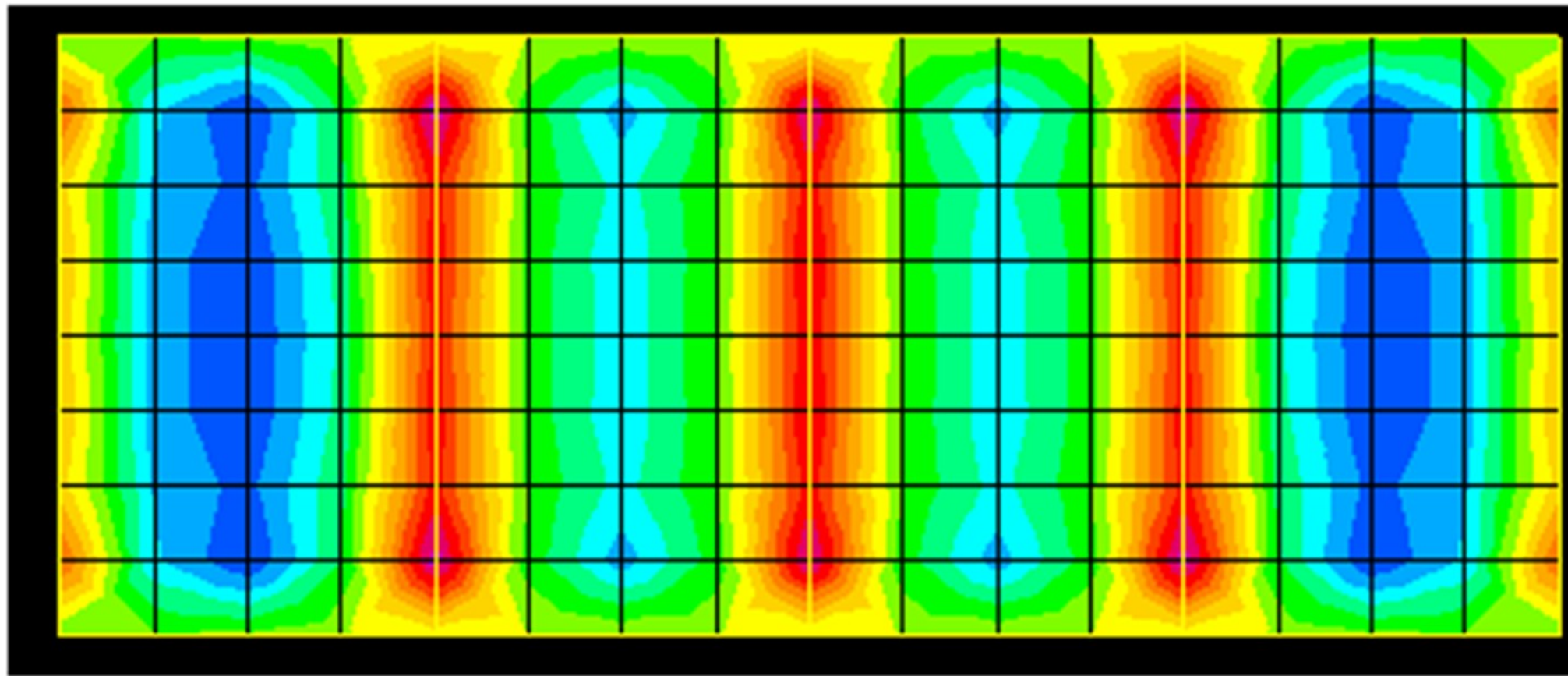
# 3D SAP: Gravity equilibrium checks



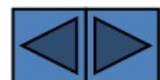
- D:
  - Slab= $20 \times 8 \times (0.25 \times 24.5 + 5) = 1780 \text{ KN}$
  - Beams= $(5 \times 8 + 2 \times 20) \times 8 \times 3 \times 24.5 = 470 \text{ KN}$
  - Columns= $10 \times 6 \times 3 \times 6 \times 24.5 = 264.6 \text{ KN}$
  - Sum= $2514.6 \text{ KN}$
- L:
  - R =  $20 \times 8 \times 9 = 1440 \text{ KN}$

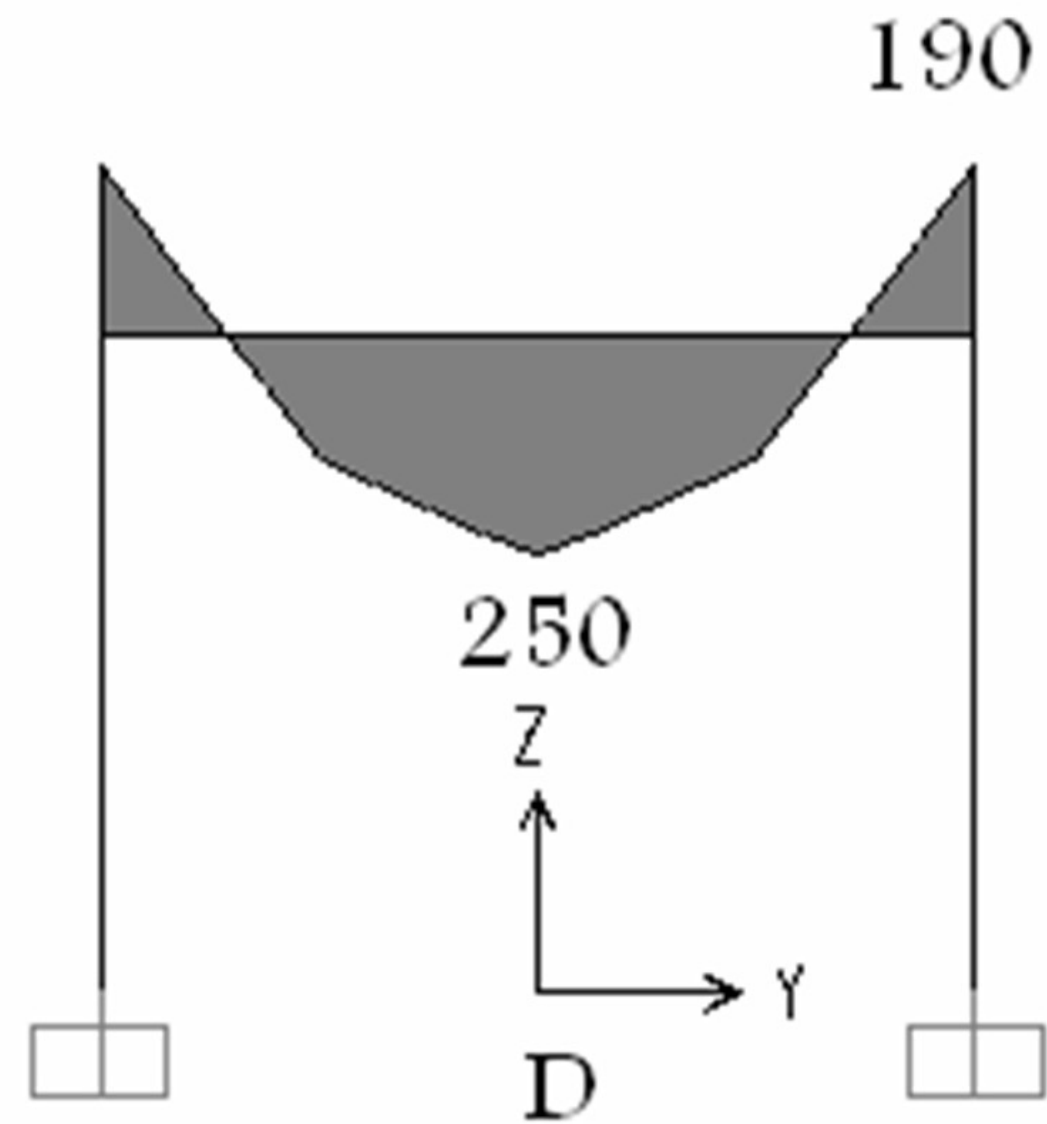
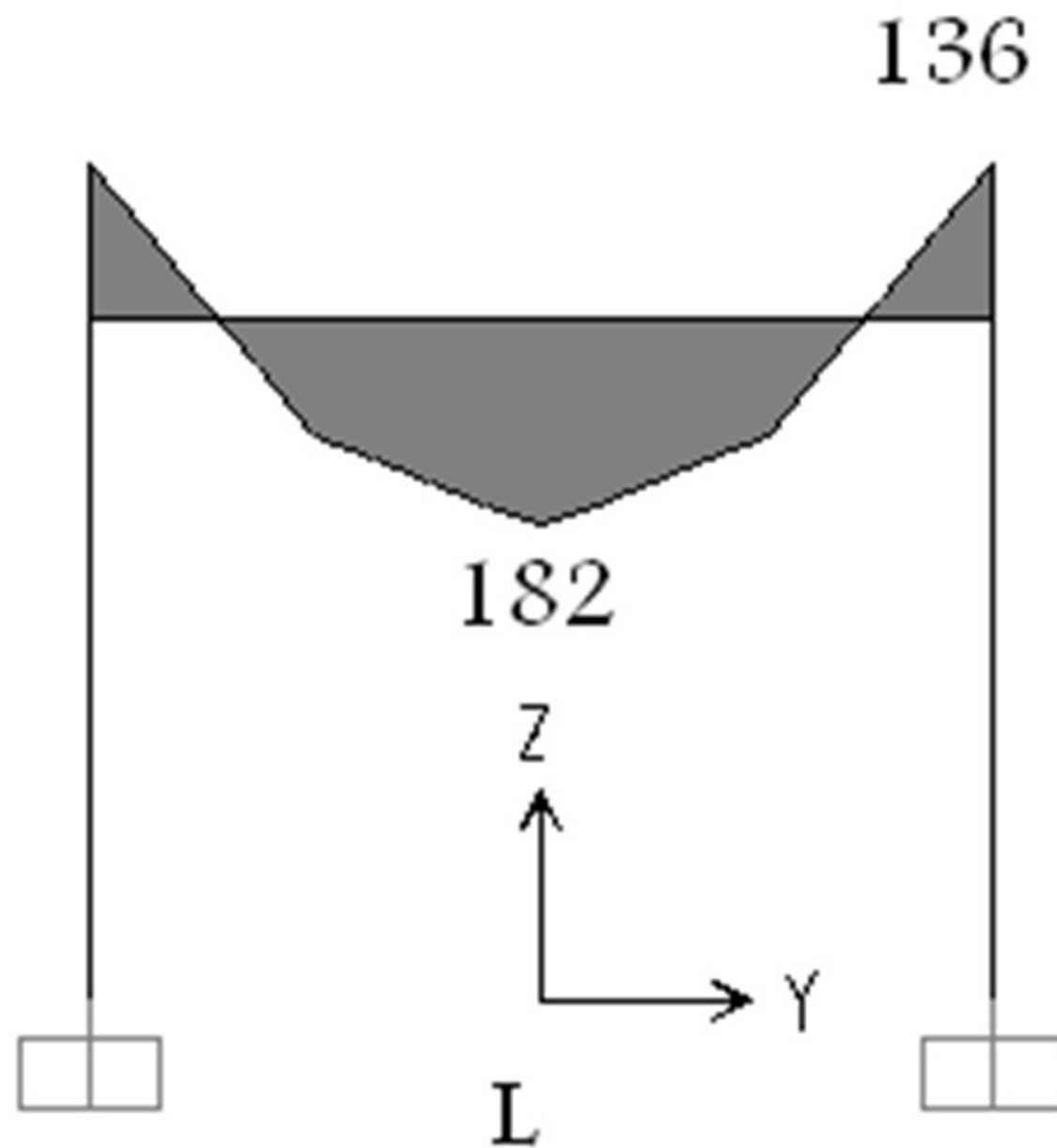
- SAP results:

	OutputCase Text	CaseType Text	GlobalFX KN	GlobalFY KN	GlobalFZ KN	GlobalMX KN-m	GlobalMY KN-m	GlobalMZ KN-m
►	DEAD	LinStatic	1.776E-15	0	2515	000000002615	000000004093	000000000151
	live	LinStatic	1.155E-14	-5.329E-14	1440	5.684E-14	000000008527	-5.658E-13

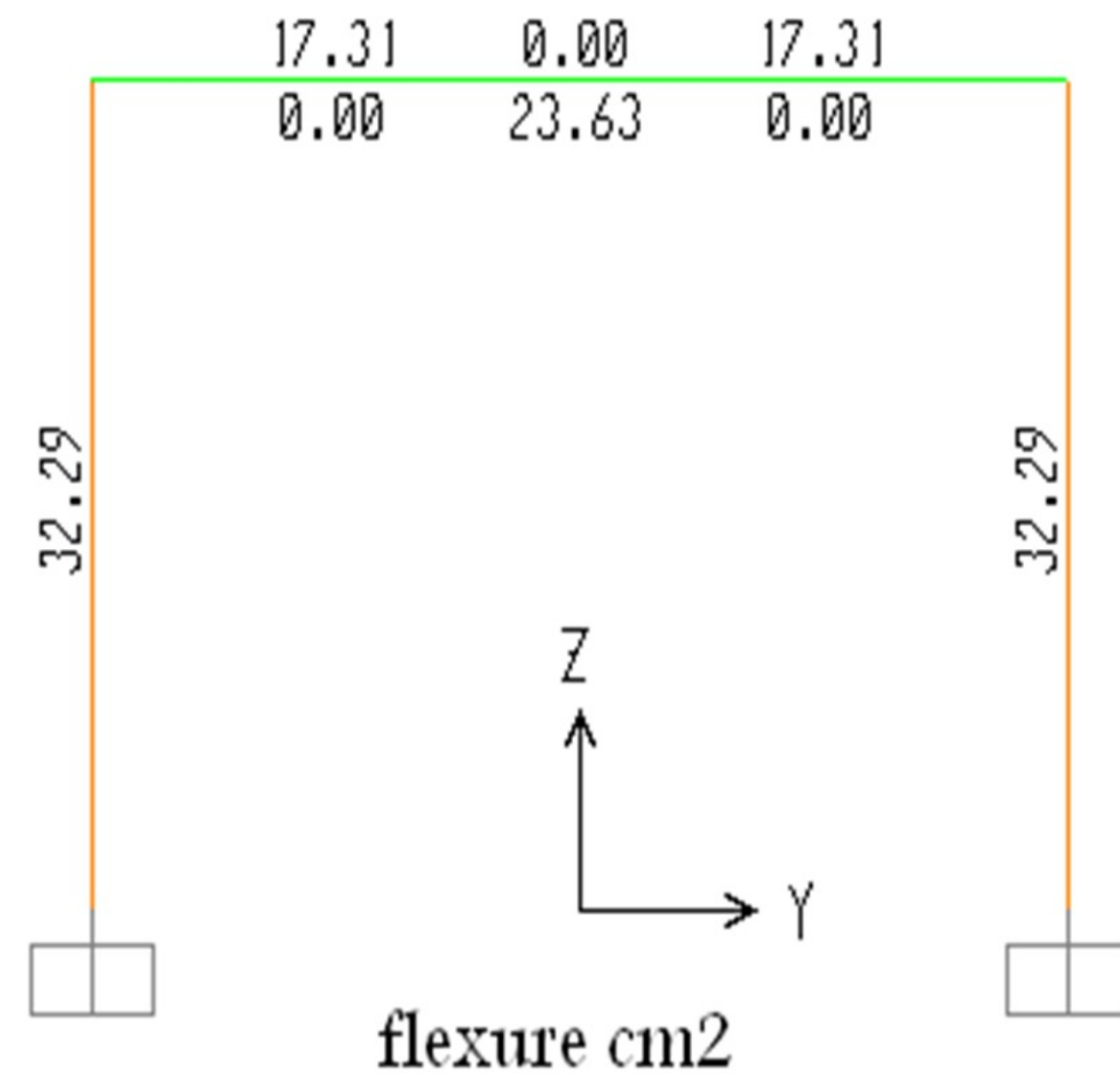
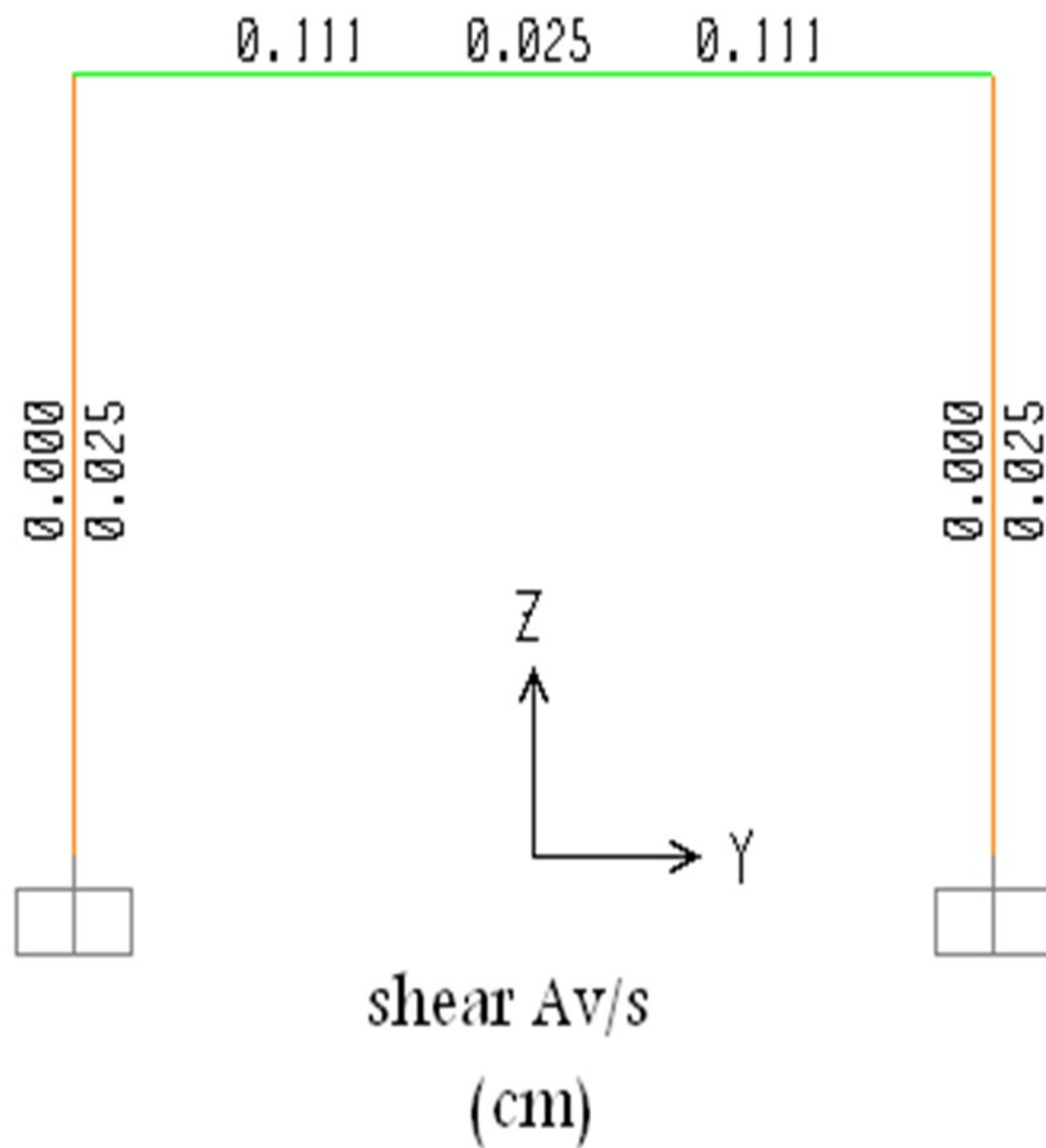


bending moment in slab KN.m



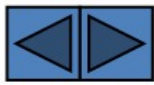
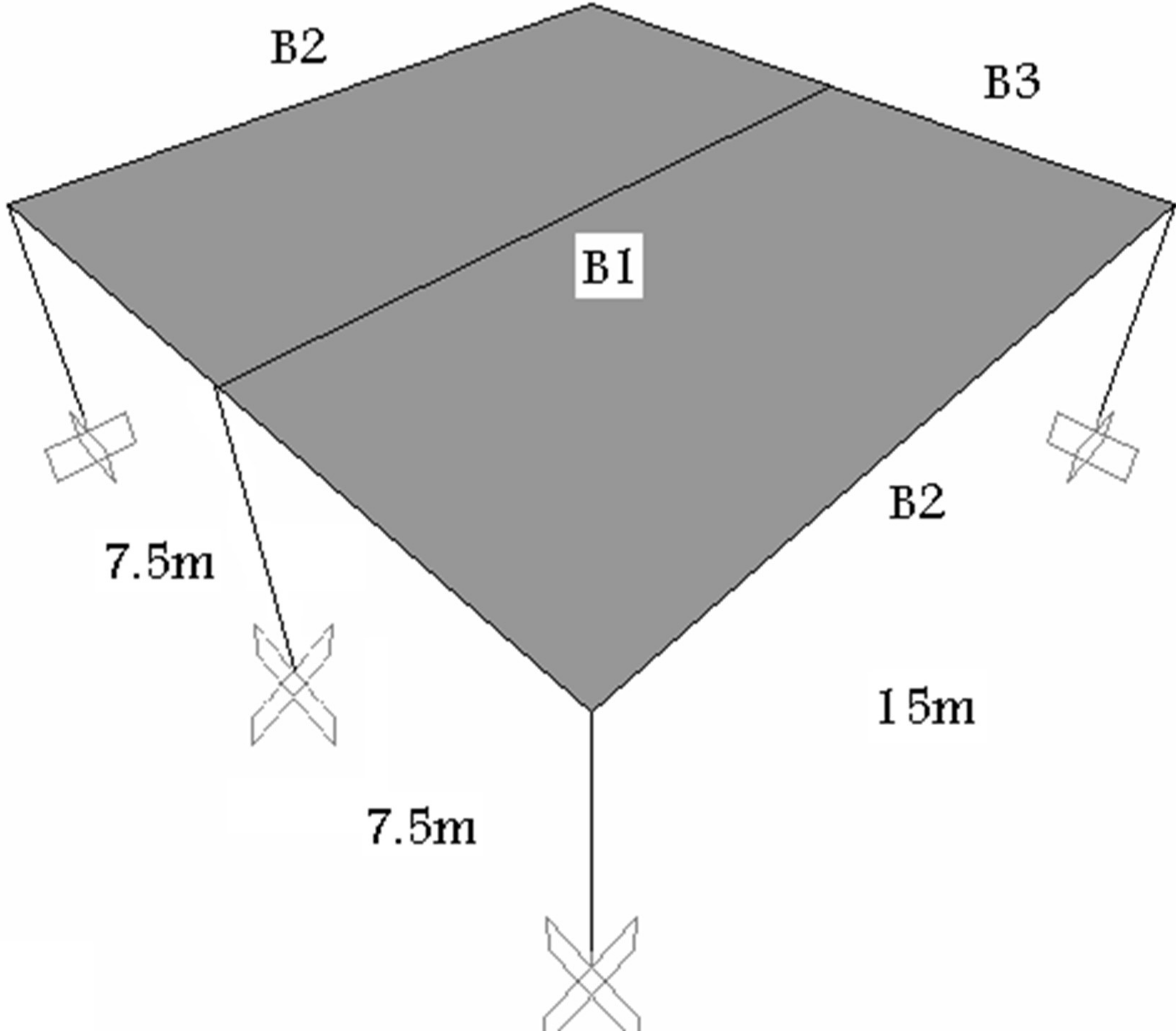


- Conceptual check for dead
  - $W_d = (.25 \times 24.5 + 5) \times 5 = 55.6 \text{ kN/m}$
  - $M_d = 55.6 \times 8^2 / 8 = 445 \text{ kN.m}$  (compare with  $250 + 190 = 440 \text{ kN.m}$  ok)
- Conceptual check for live
  - $W_L = 9 \times 5 = 45 \text{ kN/m}$
  - $M_L = 45 \times 8^2 / 8 = 360 \text{ kN.m}$  (compare with  $182 + 136 = 318 \text{ kN.m}$  ok)
- Conceptual design for positive moment
  - $M_u = 1.2 \times 250 + 1.6 \times 182 = 591 \text{ kN.m}$
  - $A_s = 3 \times 591 / 74 = 24 \text{ cm}^2$ .



- If 3D analysis results are used conceptual understanding of edge beam is wrong, thus expect failure in torsion

- Analyze and design a one story reinforced concrete structure (entertainment hall) made of one way solid slab sitting on drop beams supported on six square columns 50cm dimensions. The superimposed and live loads are  $3\text{KN/m}^2$  and  $4\text{KN/m}^2$  respectively.



**End of section 5.1**

Let Learning Continue



View of Pan Joist Slab from Below

## *Pan Joist Floor Systems*

- Definition: The type of slab is also called a ribbed slab. It consists of a floor slab, usually 5-10cm thick, supported by reinforced concrete ribs. The ribs are usually uniformly spaced at distances that do not exceed 75cm. The space between ribs is usually filled with permanent fillers to provide a horizontal slab soffit.

- ACI Requirements for Joist Construction  
(Sec. 8.13, ACI 318-08)
    - Slabs and ribs must be cast monolithically.
    - Ribs may not be less than 10cm in width
    - Depth of ribs may not be more than 3.5 times the minimum rib width
    - Clear spacing between ribs shall not exceed 750mm
- \*\* Ribbed slabs not meeting these requirements are designed as slabs and beams. \*\***

## Slab Thickness

– (ACI Sec. 8.13.6.1)

$$t \geq 5\text{cm}$$

$$t \geq \text{one twelfth the clear distance between ribs}$$

Building codes give minimum fire resistance rating:

1-hour fire rating: 2cm cover, 7.5-9cm slab thick.

2-hour fire rating: 2.5cm cover, 12cm slab thick.

## Shear strength

**8.13.8** — For joist construction,  $V_c$  shall be permitted to be 10 percent more than that specified in **Chapter 11**.

- Laying Out Pan Joist Floors (*cont.*)
  - Typically no stirrups are used in joists
  - Reducing Forming Costs:
    - Use constant joist depth for entire floor
    - Use same depth for joists and beams (not always possible)

### Distribution Ribs

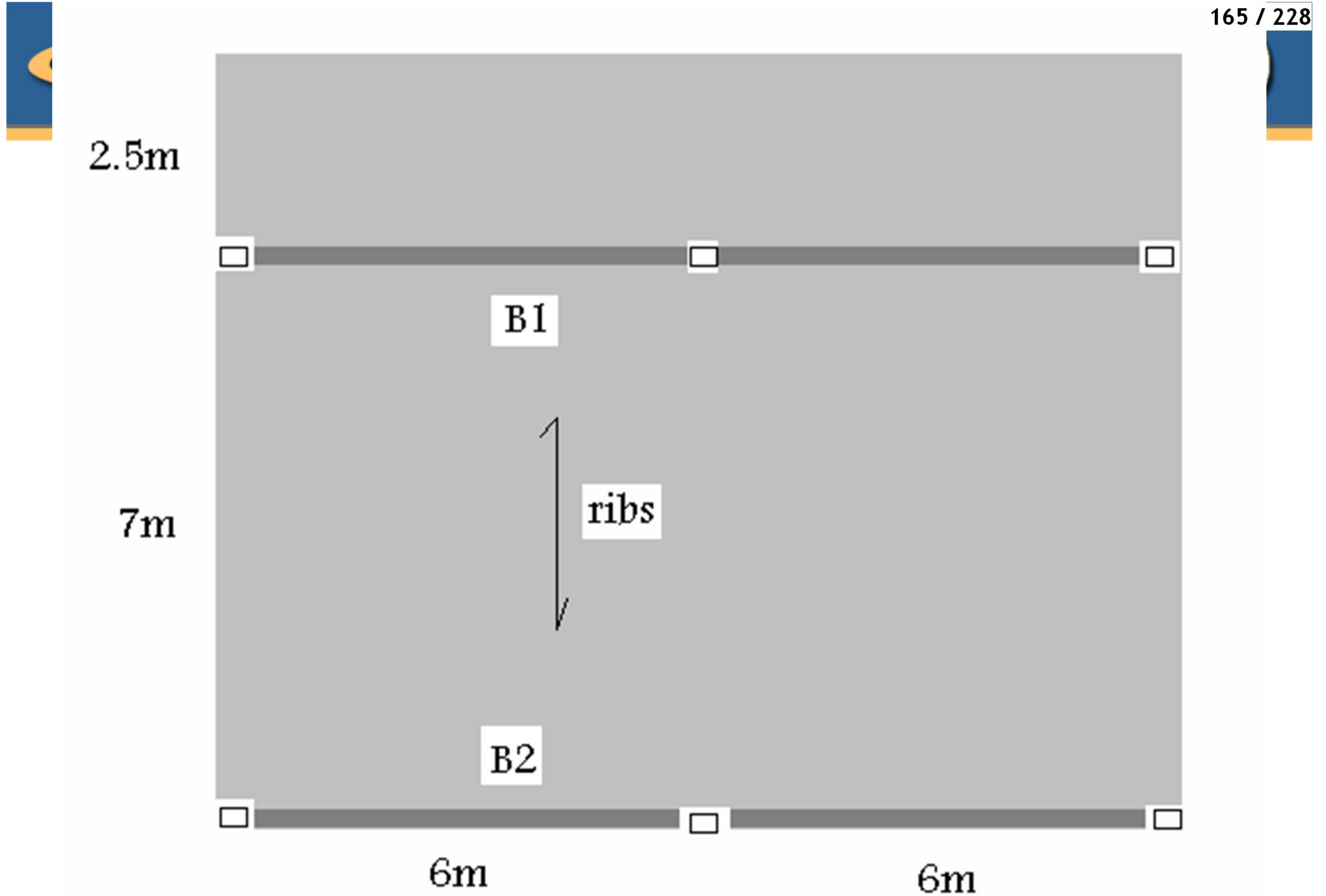
- Placed perpendicular to joists\*
- Spans < 6m.: None
- Spans 6-9m: Provided at midspan
- Spans > 9m: Provided at third-points
- At least one continuous #12mm bar is provided at top and bottom of distribution rib.



\*Note: not required directly by ACI Code, but typically used in construction and required indirectly in ACI 10.4.1:

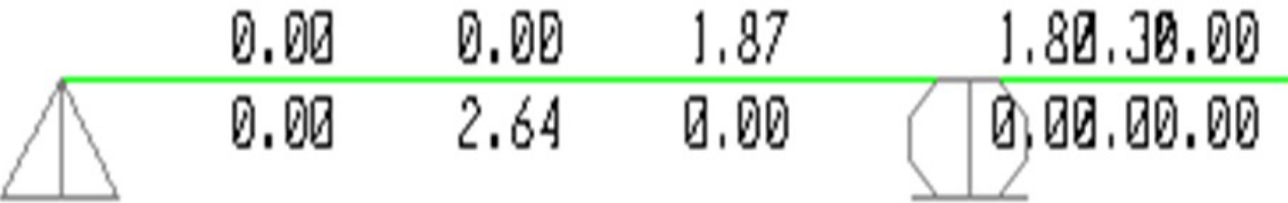
**10.4.1** — Spacing of lateral supports for a beam shall not exceed 50 times  $b$ , the least width of compression flange or face.

- Analyze and design (as a one-way ribbed slab in the 7m direction) the following one story structure (3m height) using 3D model (figure next slide):
  - A. Specifications: B250,  $f_y=4200 \text{ kg/cm}^2$ , superimposed=  $70 \text{ kg/m}^2$  , live loads=  $200 \text{ kg/m}^2$ , ribs 34cm height/ 15cm width, blocks 40X25X24cm height (density= $1 \text{ t/m}^3$  ), beam 25cm width by 50cm depth, column dimensions 25cmX25cm,

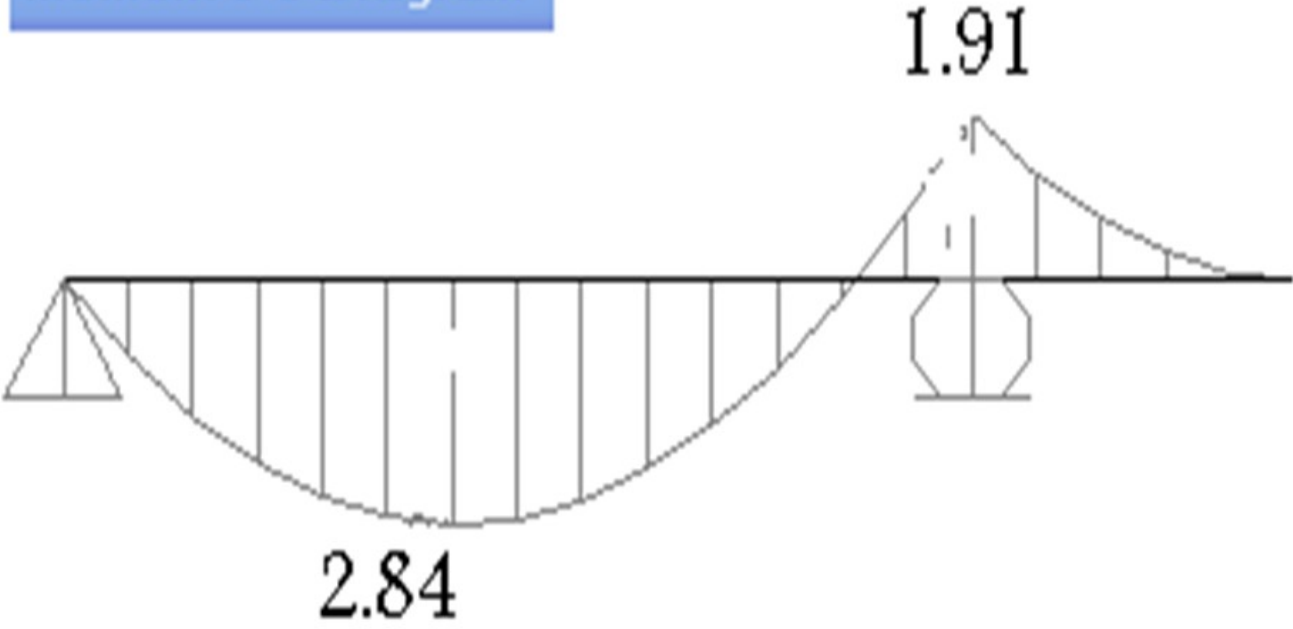


- Slab: assume  $c=5\text{cm}$ 
  - $w_d = [(0.15 * .24 + 0.55 * 0.1) * 2.5 + 0.4 * 0.24 * 1] / 0.55 + 0.07 = 0.658 \text{ t/m}^2$
  - $w_u = [1.2 * 0.658 + 1.6 * 0.2] * 0.55 = 0.61 \text{ t/m/rib}$
  - $M_u^- = 0.61(2.5)^2 / 2 = 1.91 \text{ t.m.}, A_s = 1.87 \text{ cm}^2$ .
  - $M_u^+ = 2.84 \text{ t.m.}, A_s = 2.64 \text{ cm}^2$
  - verify that change of shape (rectangular) or  $f_c$  (take 300) has minor effect on change of  $A_s$

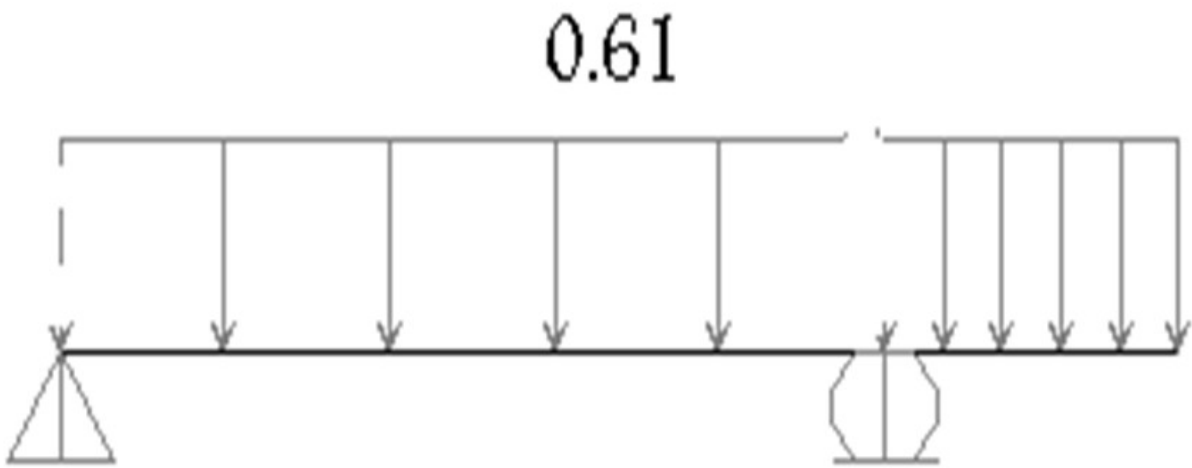
Area



Moment 3-3 Diagram



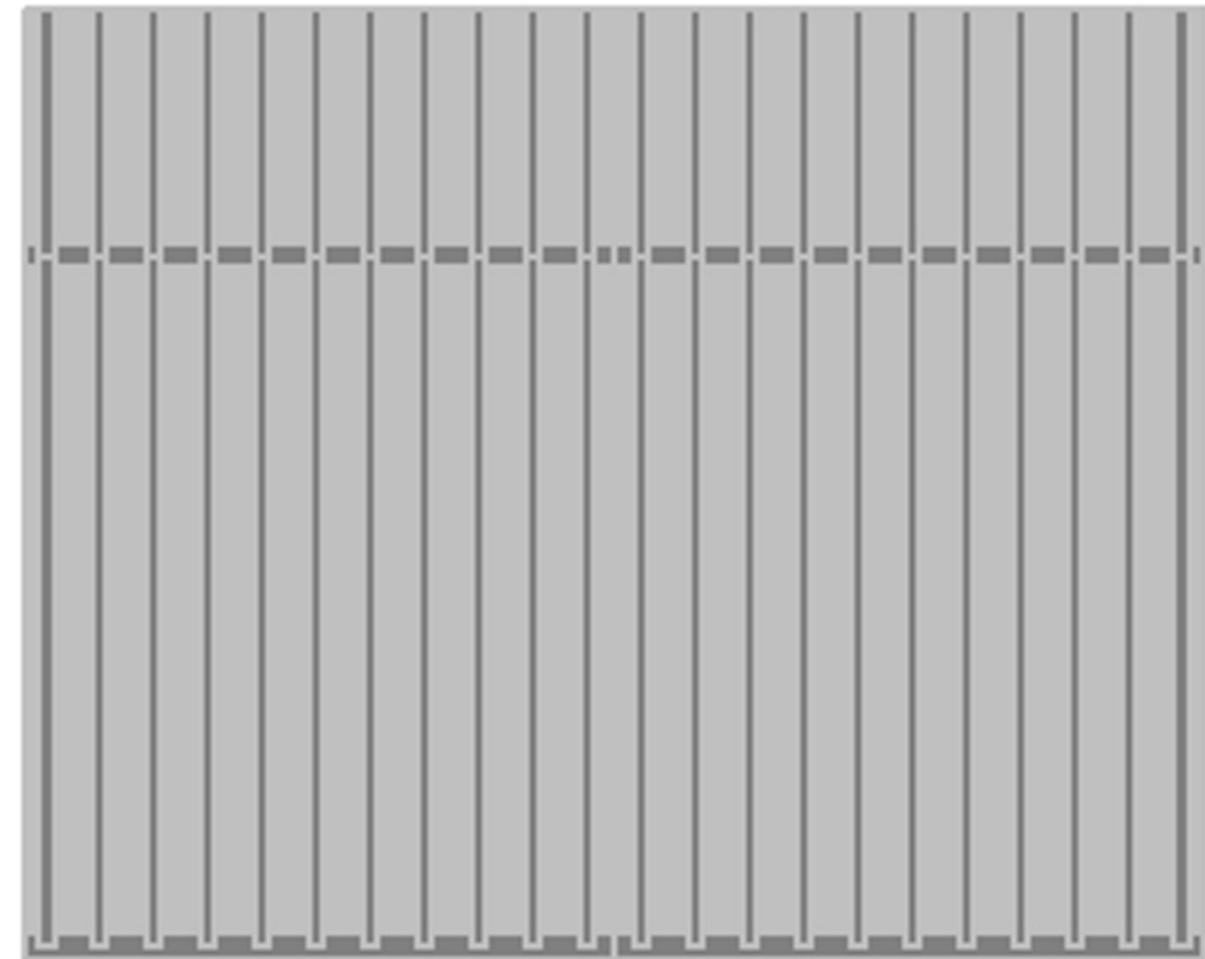
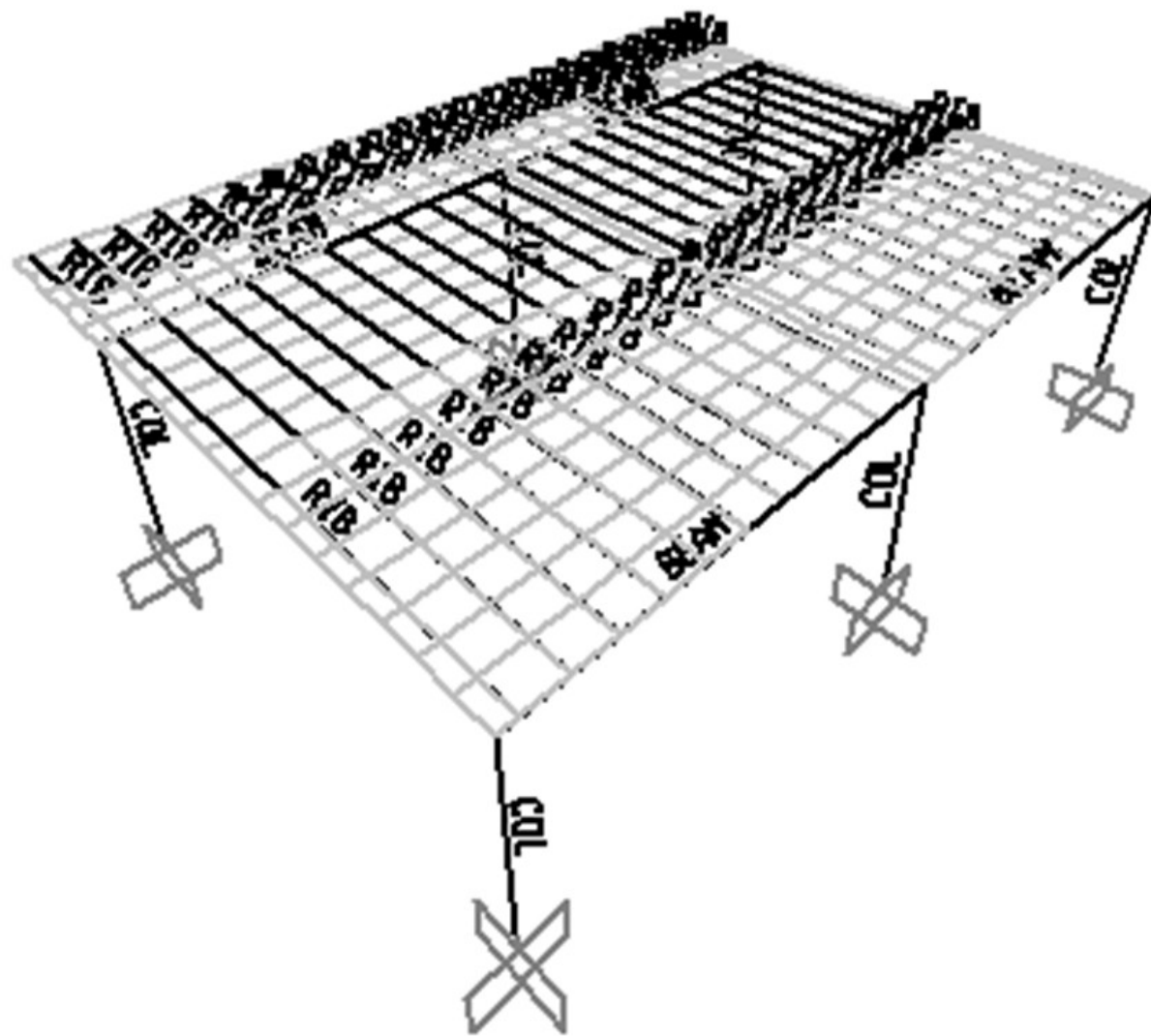
Span Loads



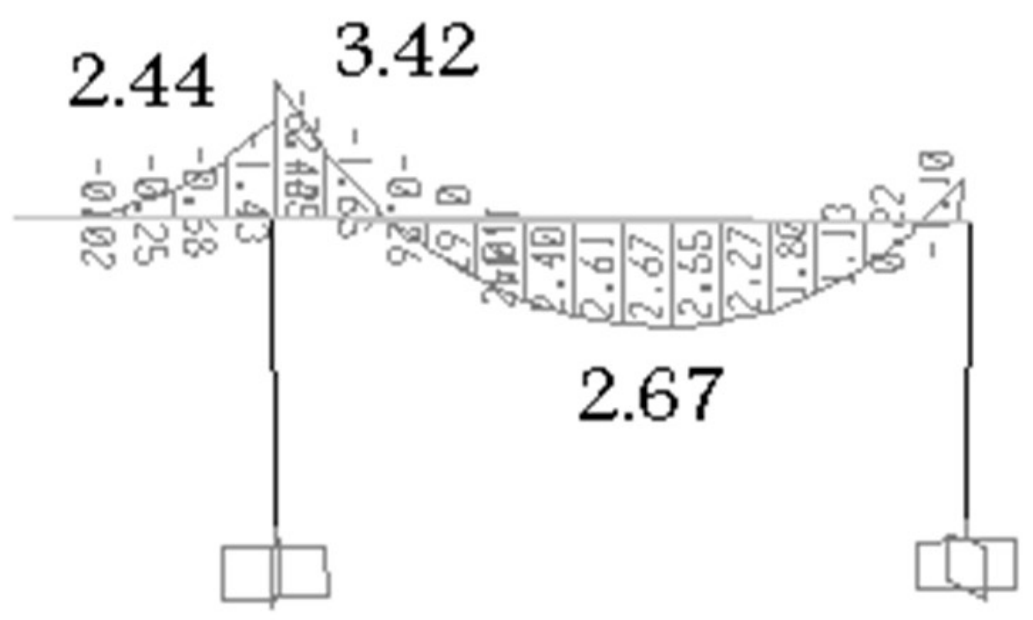
Joint Reactions



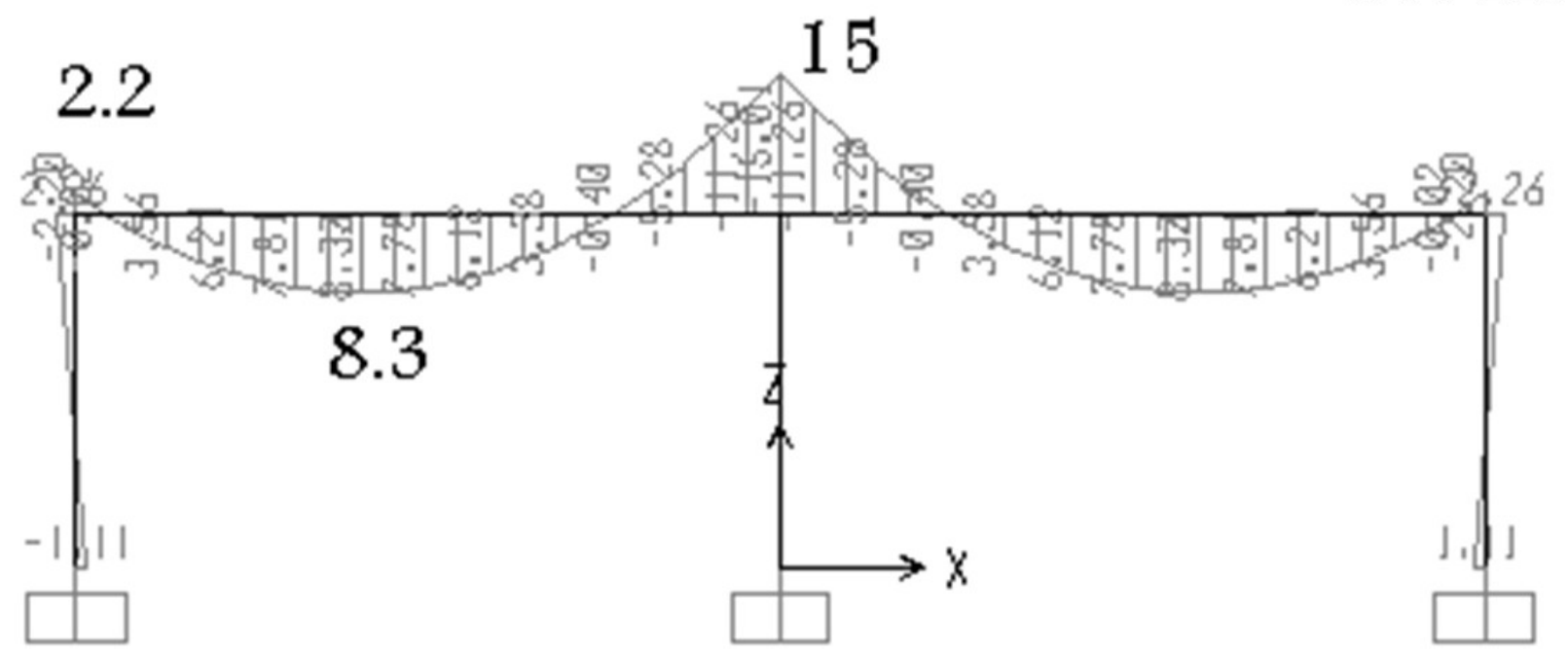
- Beam B1 (interior frame)
  - $w_u = (3.93/0.55) + 0.25 * 0.5 * 2.5 * 1.2 = 7.52 \text{ t/m}$
  - $M_u^- = 7.52(6)^2 / 8 = 33.8 \text{ t.m.}, A_s = 33.8 * 30 / 45 = 22.6 \text{ cm}^2$
  - $M_u^+ = 7.52(6)^2 / 14.2 = 19.1 \text{ t.m.}, A_s = 19.1 * 30 / 45 = 12.7 \text{ cm}^2$
- Beam B2: (exterior frame)
  - $w_u = (1.86/0.55) + 0.25 * 0.5 * 2.5 * 1.2 = 3.76 \text{ t/m}$
  - $M_u^- = 3.76(6)^2 / 8 = 16.9 \text{ t.m.}, A_s = 16.9 * 30 / 45 = 11.3 \text{ cm}^2$
  - $M_u^+ = 3.76(6)^2 / 14.2 = 9.53 \text{ t.m.}, A_s = 9.53 * 30 / 45 = 6.4 \text{ cm}^2$



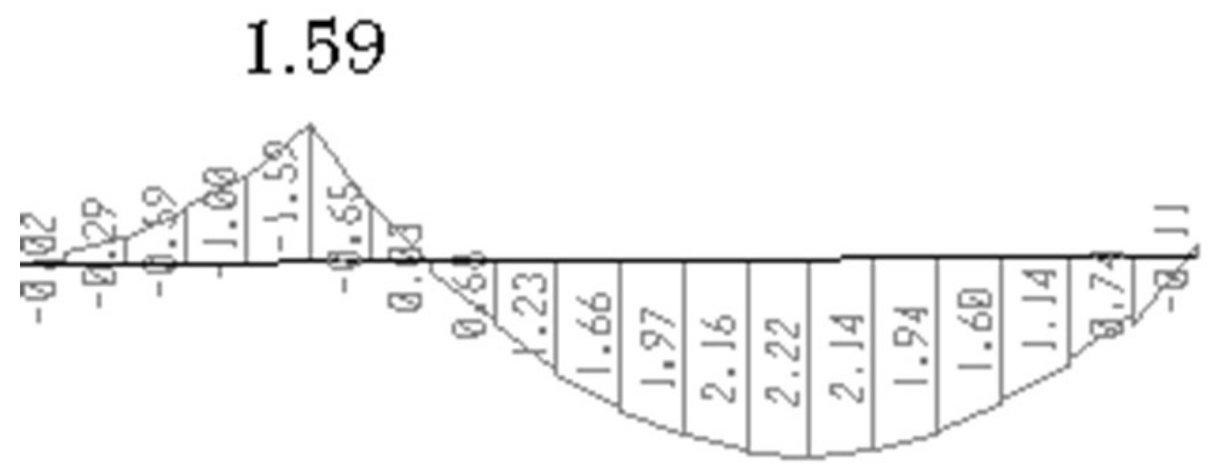
3D



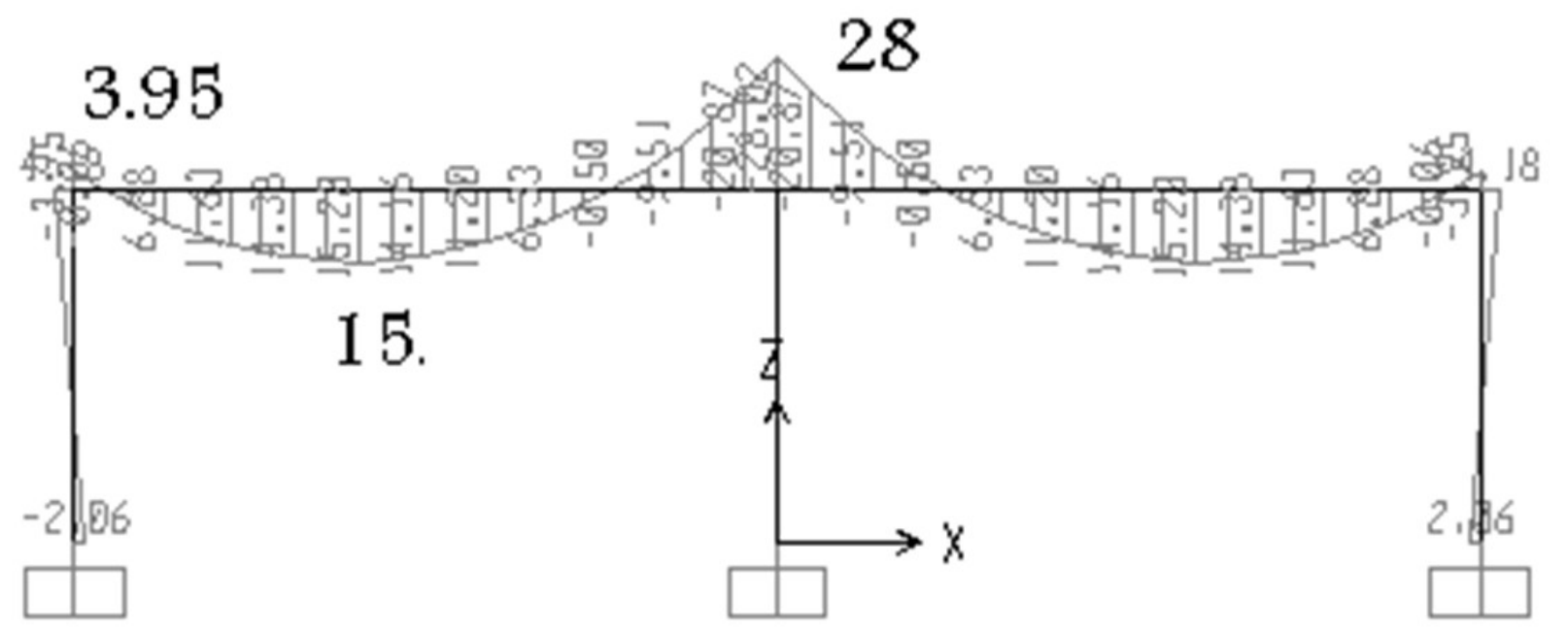
interior rib/ col



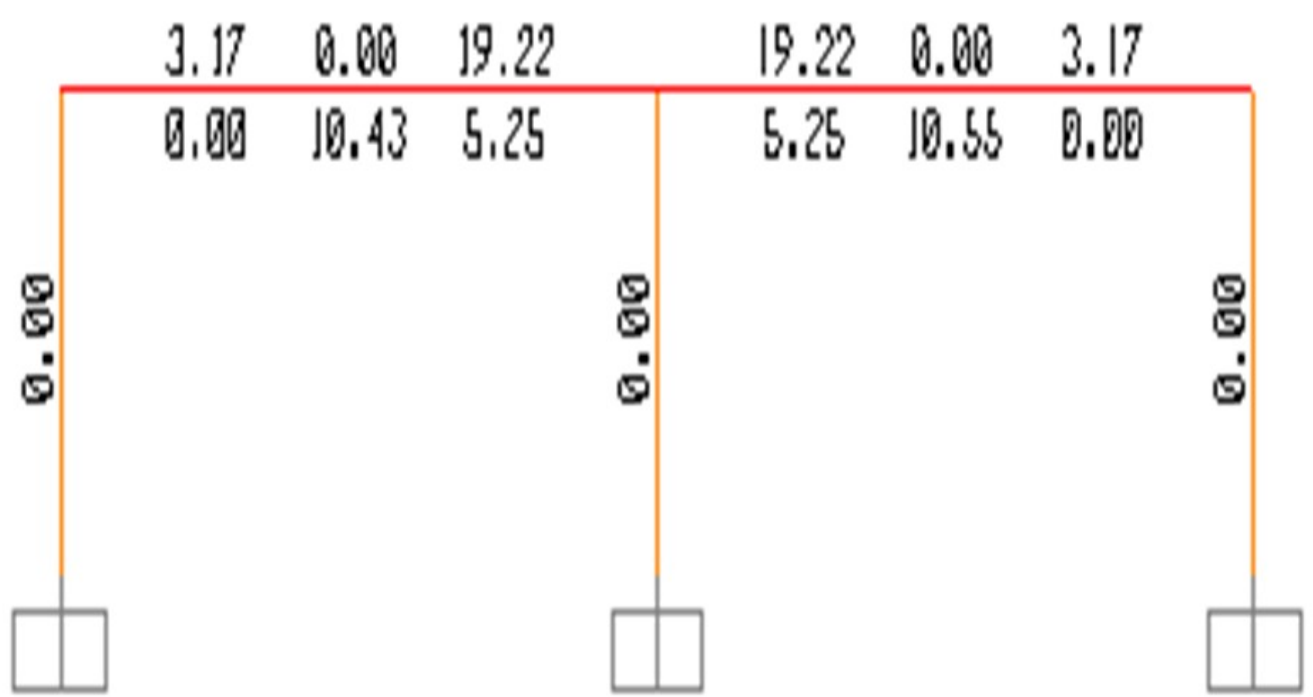
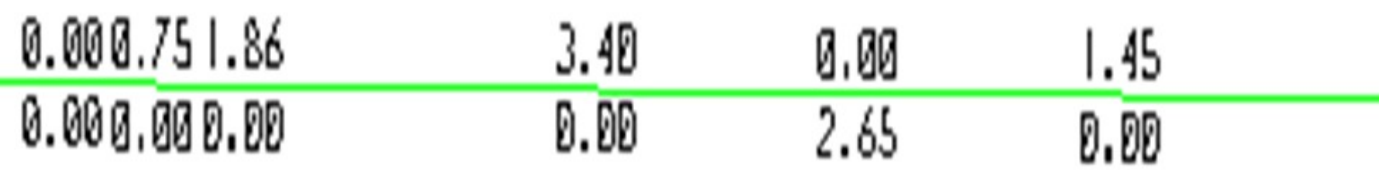
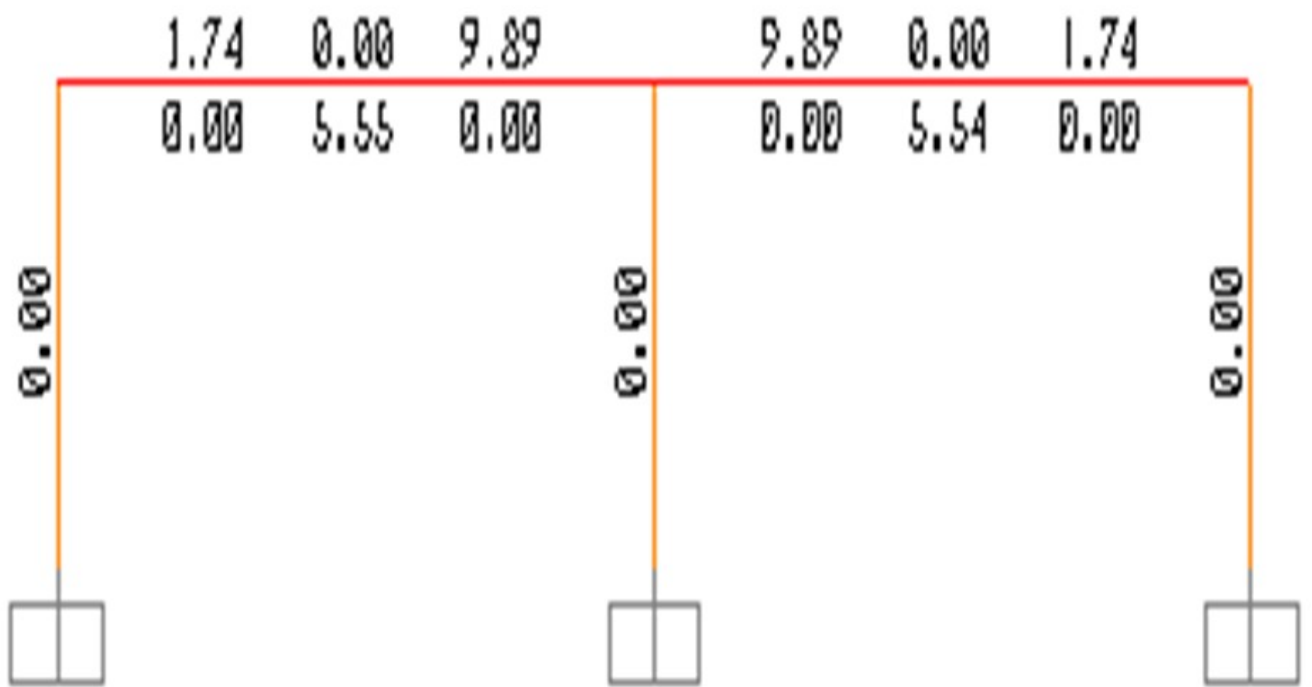
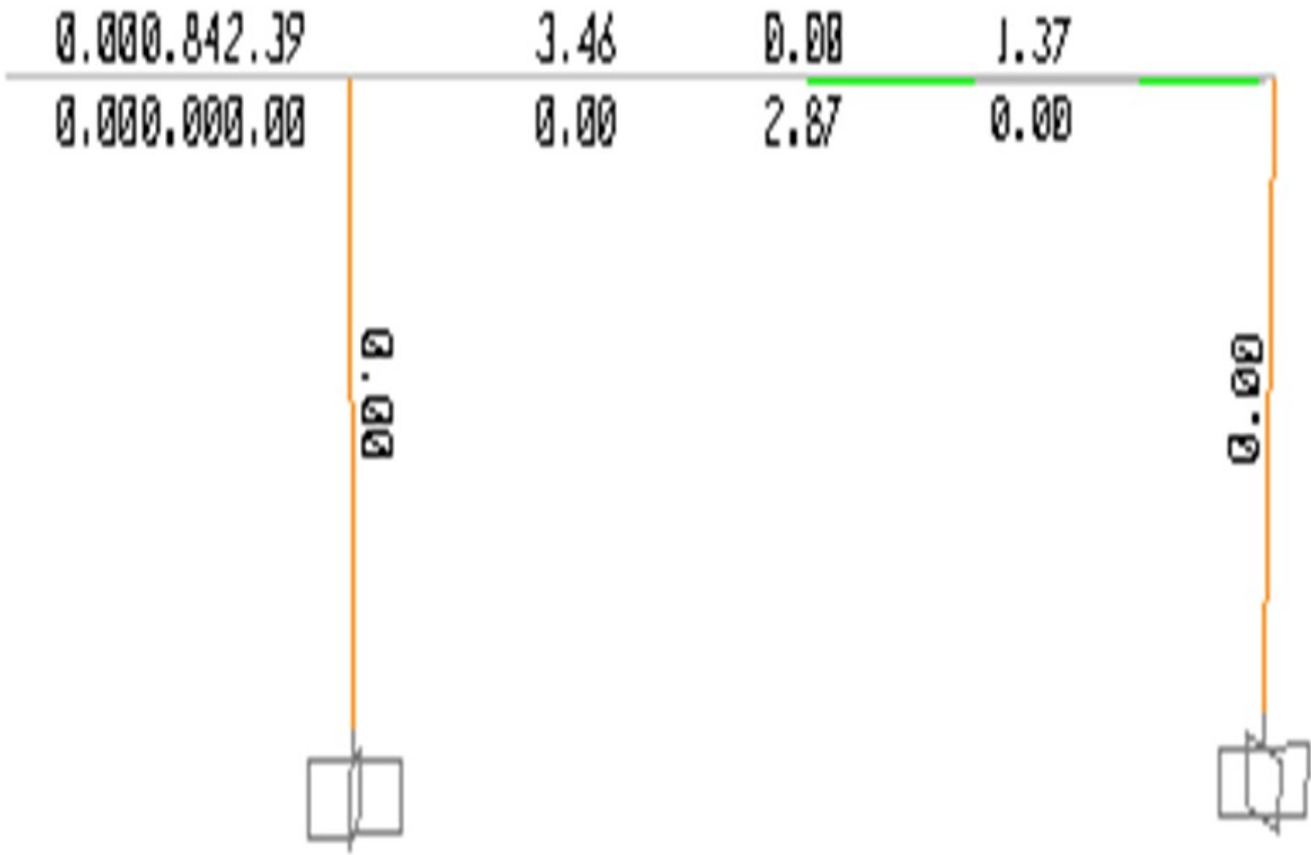
exterior frame



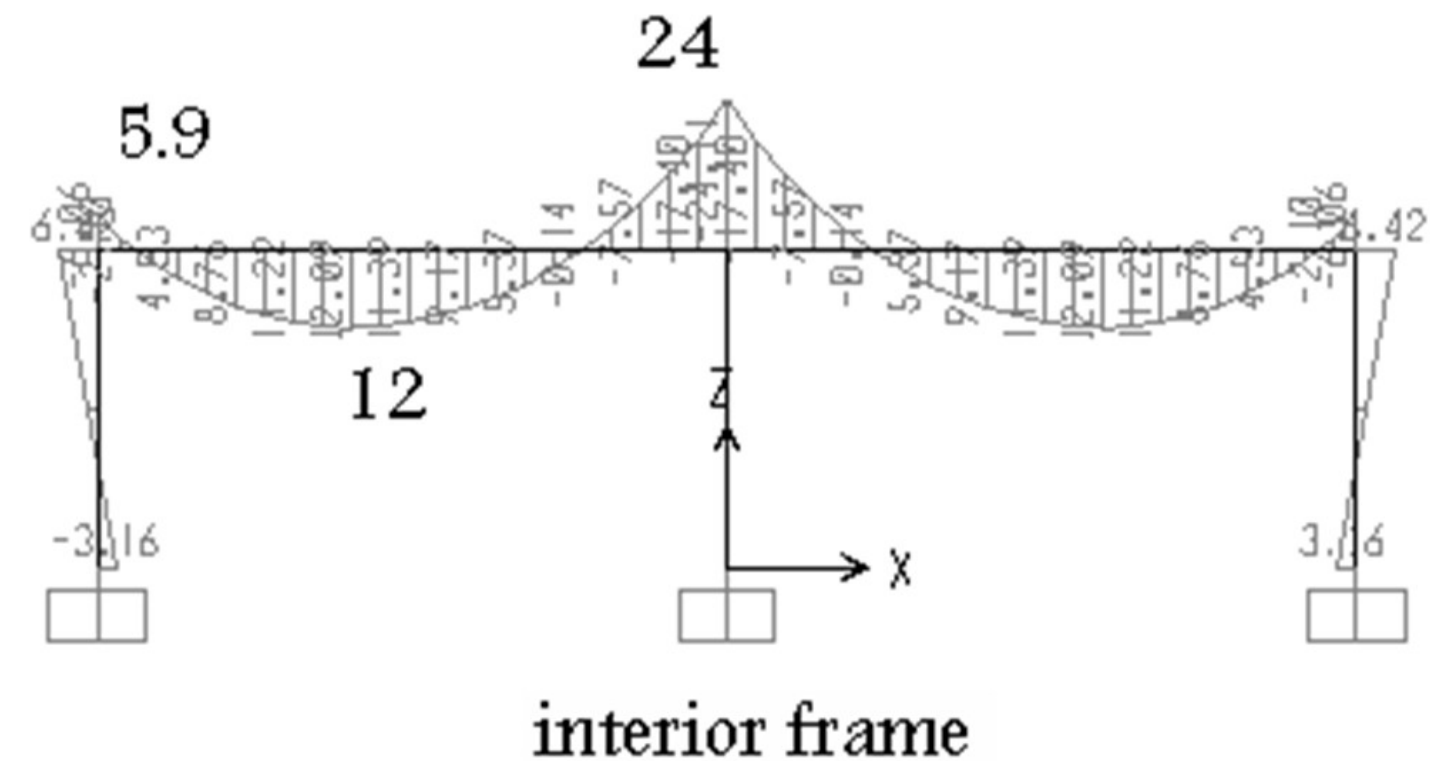
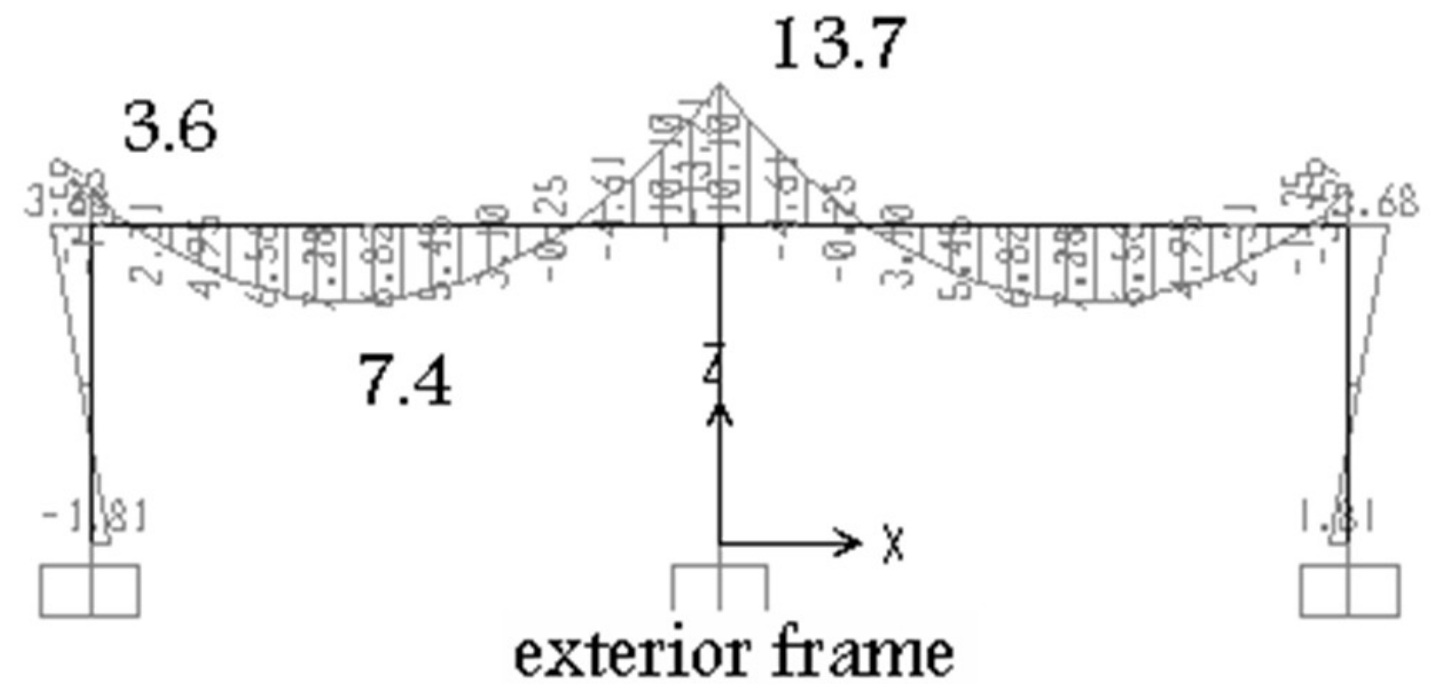
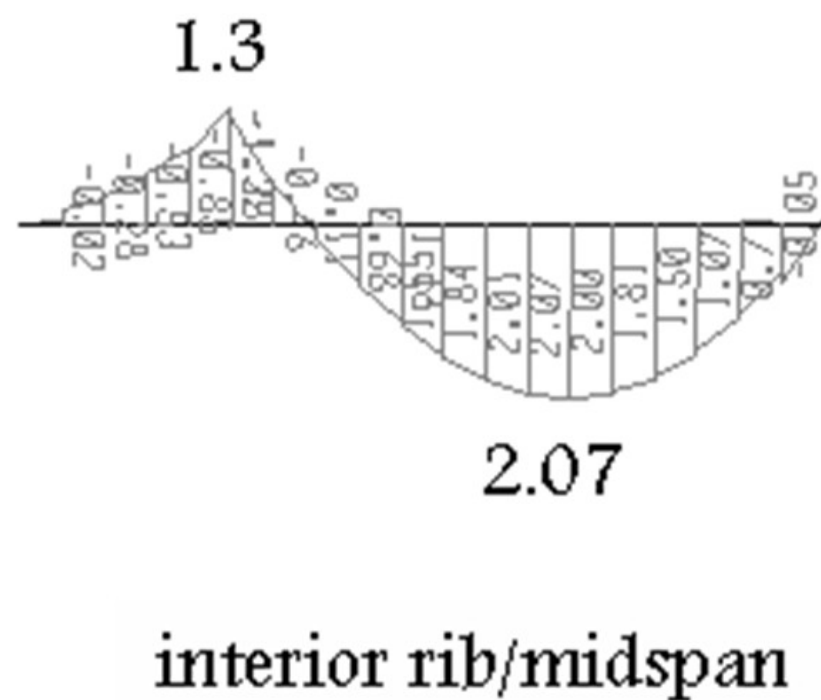
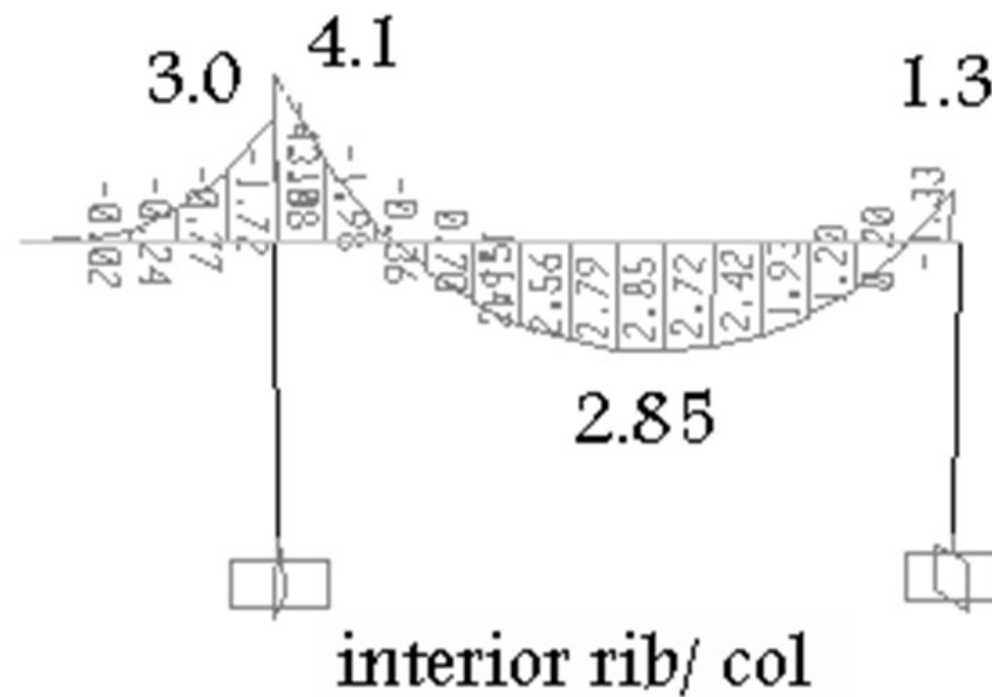
interior rib/midspan



interior frame



- Repeat previous example but if the beams are 34cm depth by 37cm width .(to preserve beam weight)
- Draw conclusions



Conclusions: Ribs

Moments increased on interior column strip and reduced on interior middle strip, which increases the difference existed previously. Why?

Do you expect problems in local practice, why? Yes, at cantilevers due to large increase

## Conclusions: beams

All moments are reduced (except at exterior, almost the same), why?

Smaller load is transferred to column directly

Exterior moment increases for hidden, why? Exterior end is more restrained by column for hidden, thus more fixity and more moment.

Do you expect problems in local practice? No, usually steel is provided at –ve moment in detailing practice at the support + beams are most of the time placed over masonry walls, so no stresses exist in them.

Is it now necessary to change local practice? Yes, steel savings

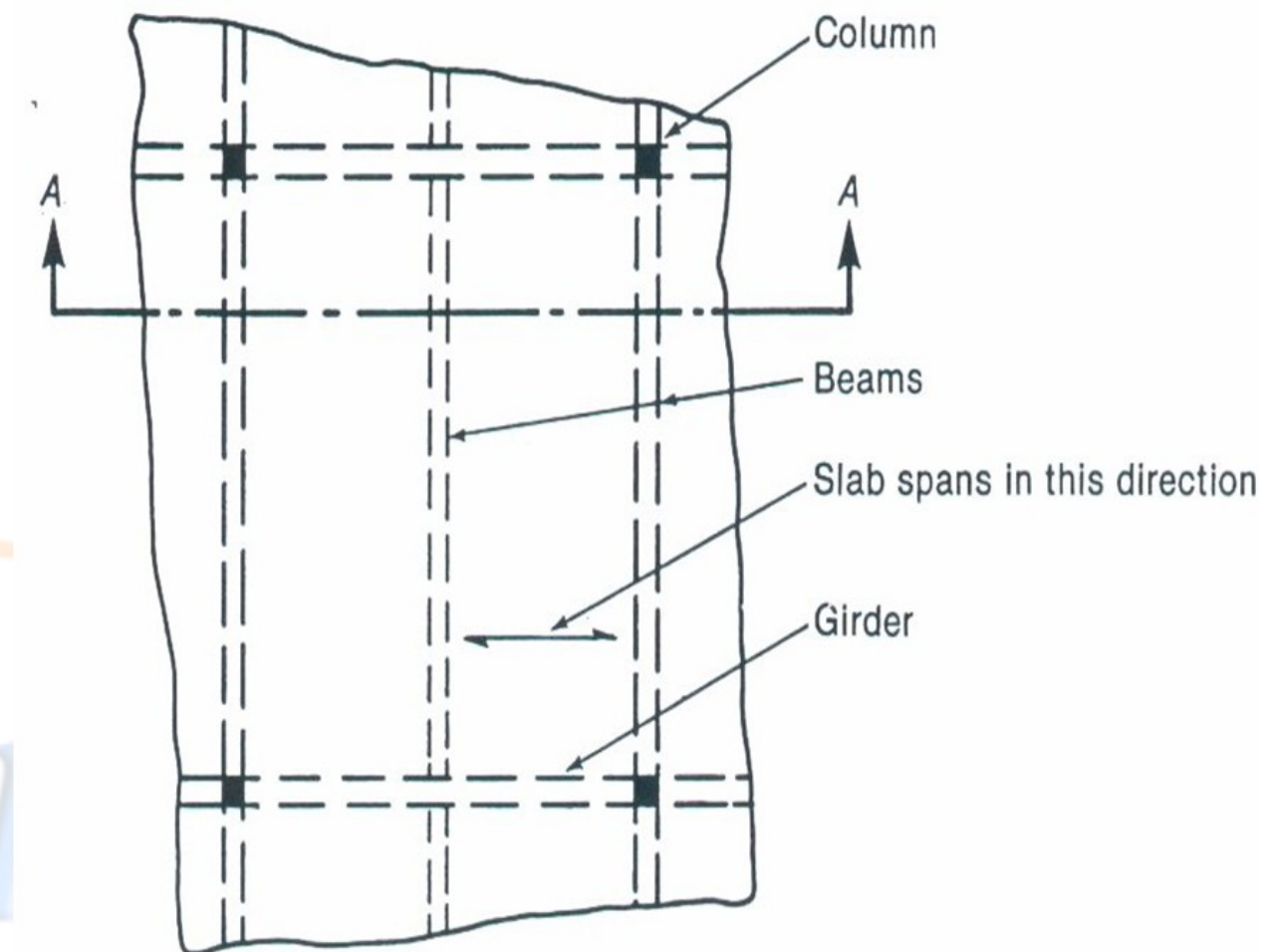
**End of section 5.2**

Let Learning Continue

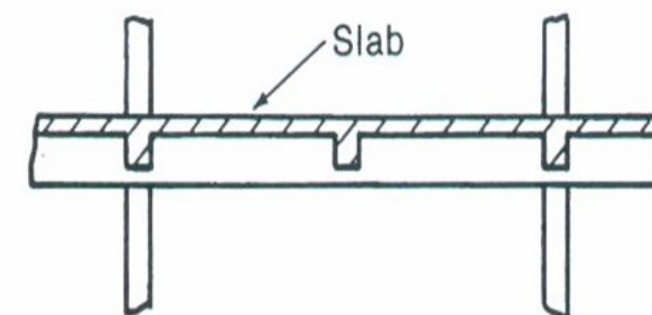


## 5.3 Two way slab systems review

- One-way Slab on beams suitable span 3 to 6m with  $LL = 3-5 \text{ kN/m}^2$ .
- Can be used for larger spans with relatively higher cost and higher deflections
- One-way joist system suitable span 6 to 9m with  $LL = 4-6 \text{ kN/m}^2$ .
- Deep ribs, the concrete and steel quantities are relatively low  
Expensive formwork expected.



(a) Plan-beams at middle of panel.



(b) Section A-A.

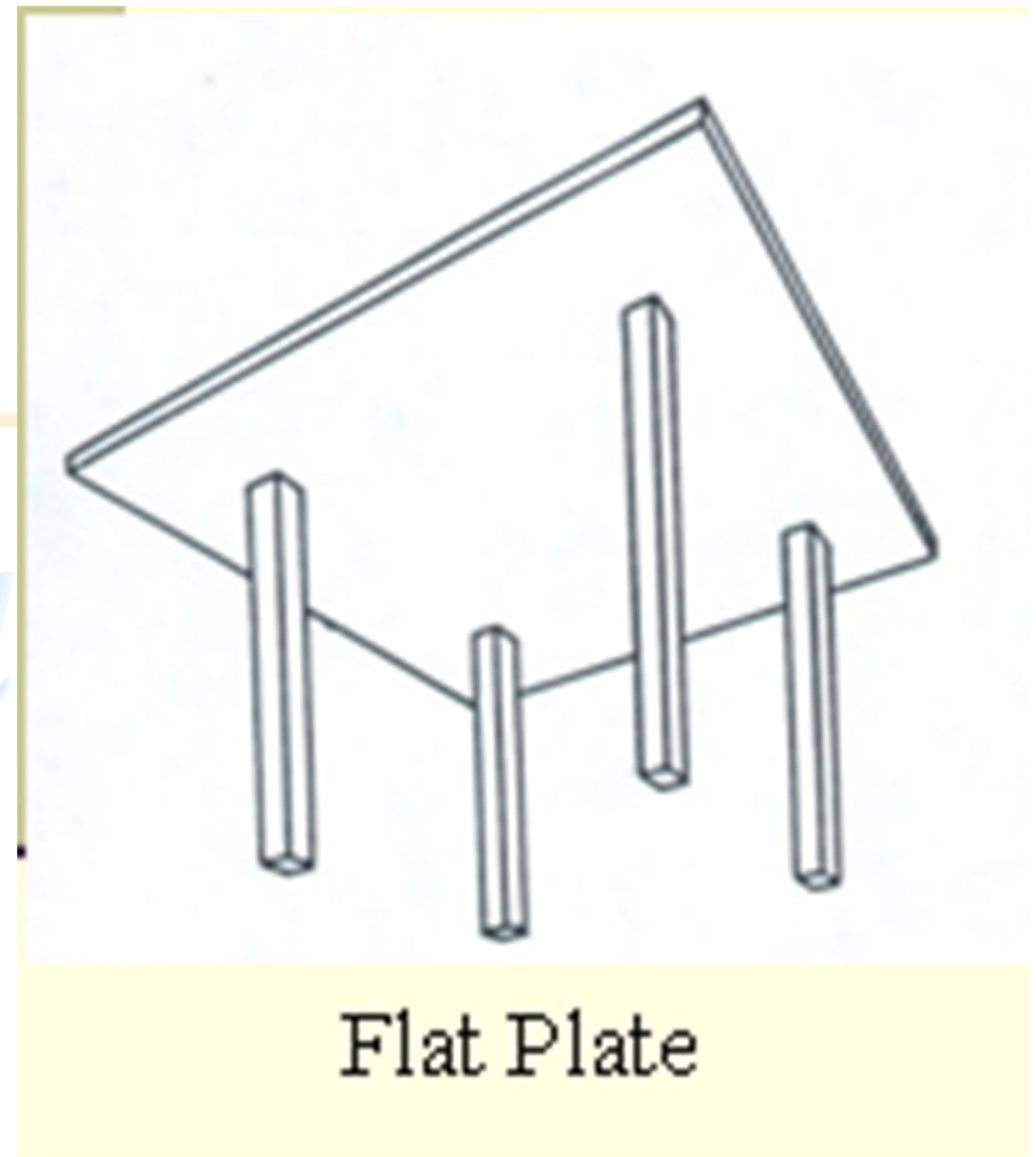
Flat Plate suitable span 6 to 7.5m  
with  $LL = 3-5 \text{ kN/m}^2$ .

### *Advantages*

- Low cost formwork
- Exposed flat ceilings
- Fast

### *Disadvantages*

- Low shear capacity
- Low Stiffness (notable deflection)



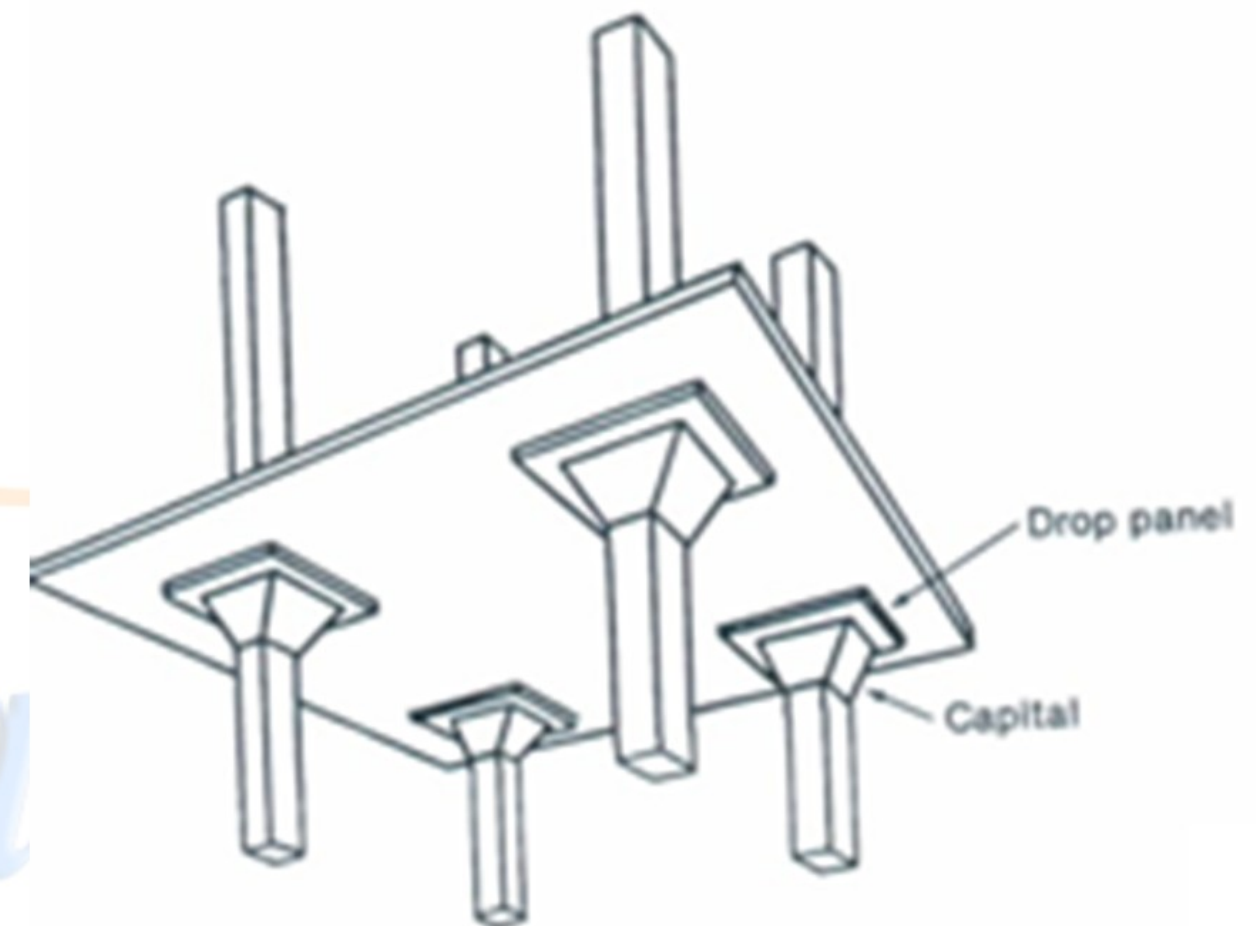
Flat Slab suitable span 6 to 9m  
with  $LL = 4\text{--}7.5\text{kN/m}^2$ .

#### *Advantages*

- Low cost formwork
- Exposed flat ceilings
- Fast

#### *Disadvantages*

- Need more formwork for capital and panels



Flat slab

- Waffle Slab suitable span 9 to 14.5m with  $LL = 4-7.5 \text{ kN/m}^2$ .

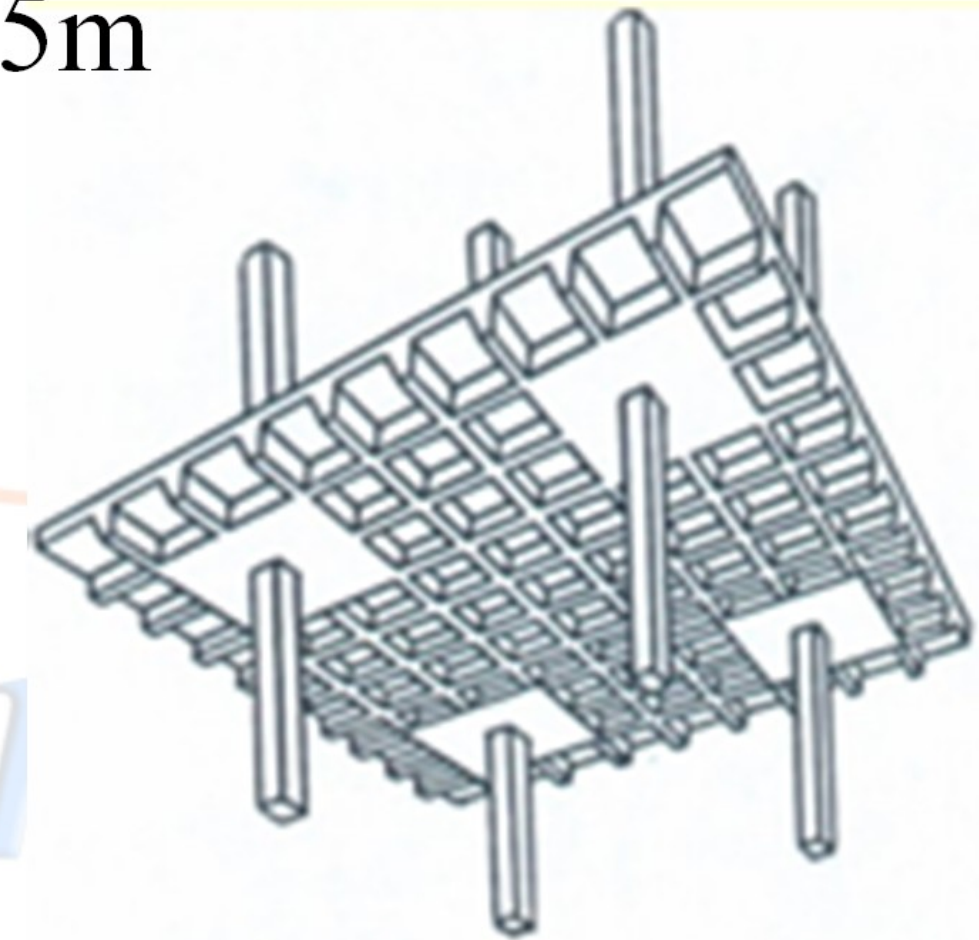
### *Advantages*

- Carries heavy loads
- Attractive exposed ceilings
- Fast

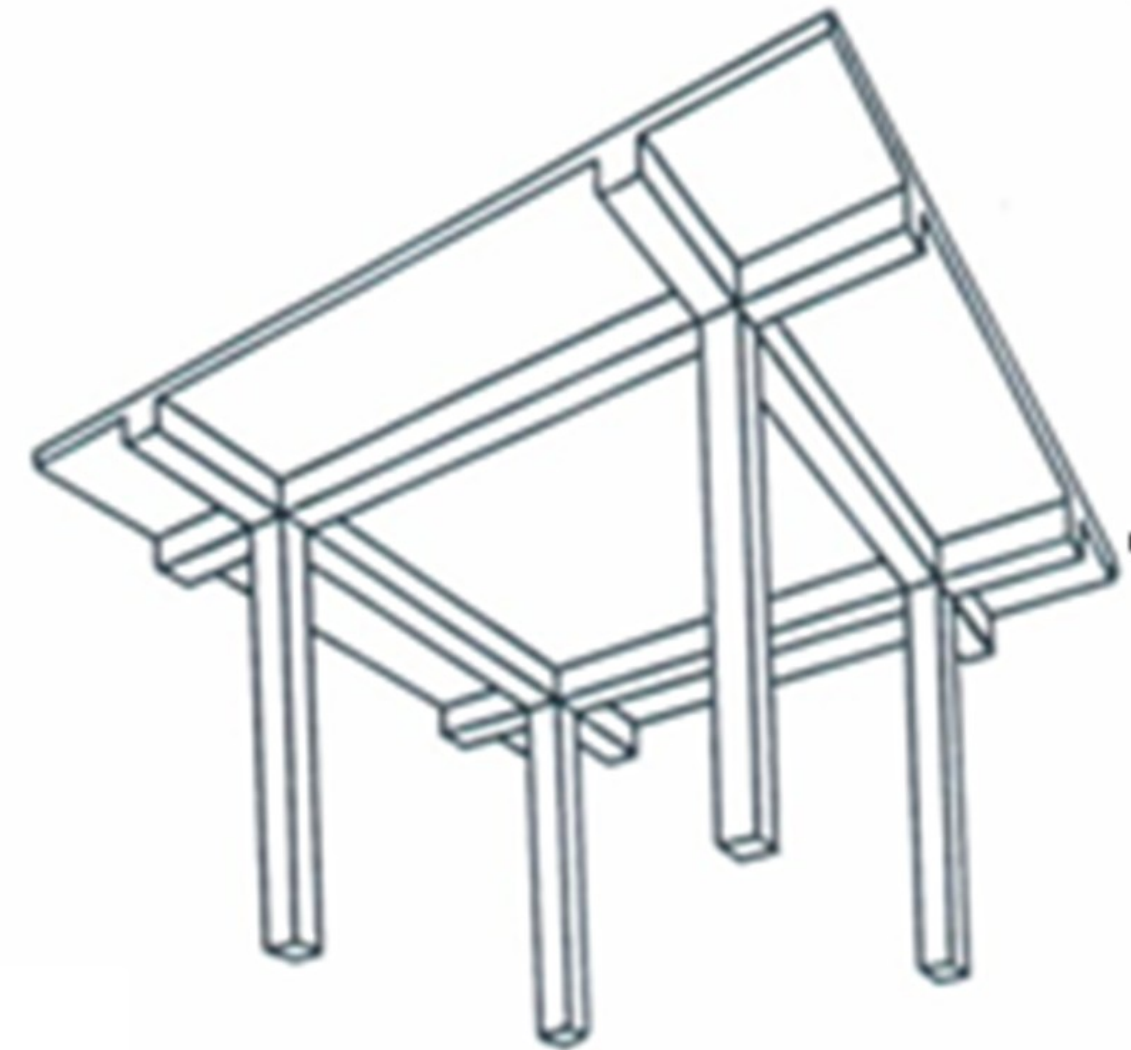
### *Disadvantages*

- Formwork with panels is expensive

The two-way ribbed slab and waffled slab system: General thickness of the slab is 5 to 10cm.



Waffle slab



Two-way slab with beams

$w_s$  = load taken by short direction

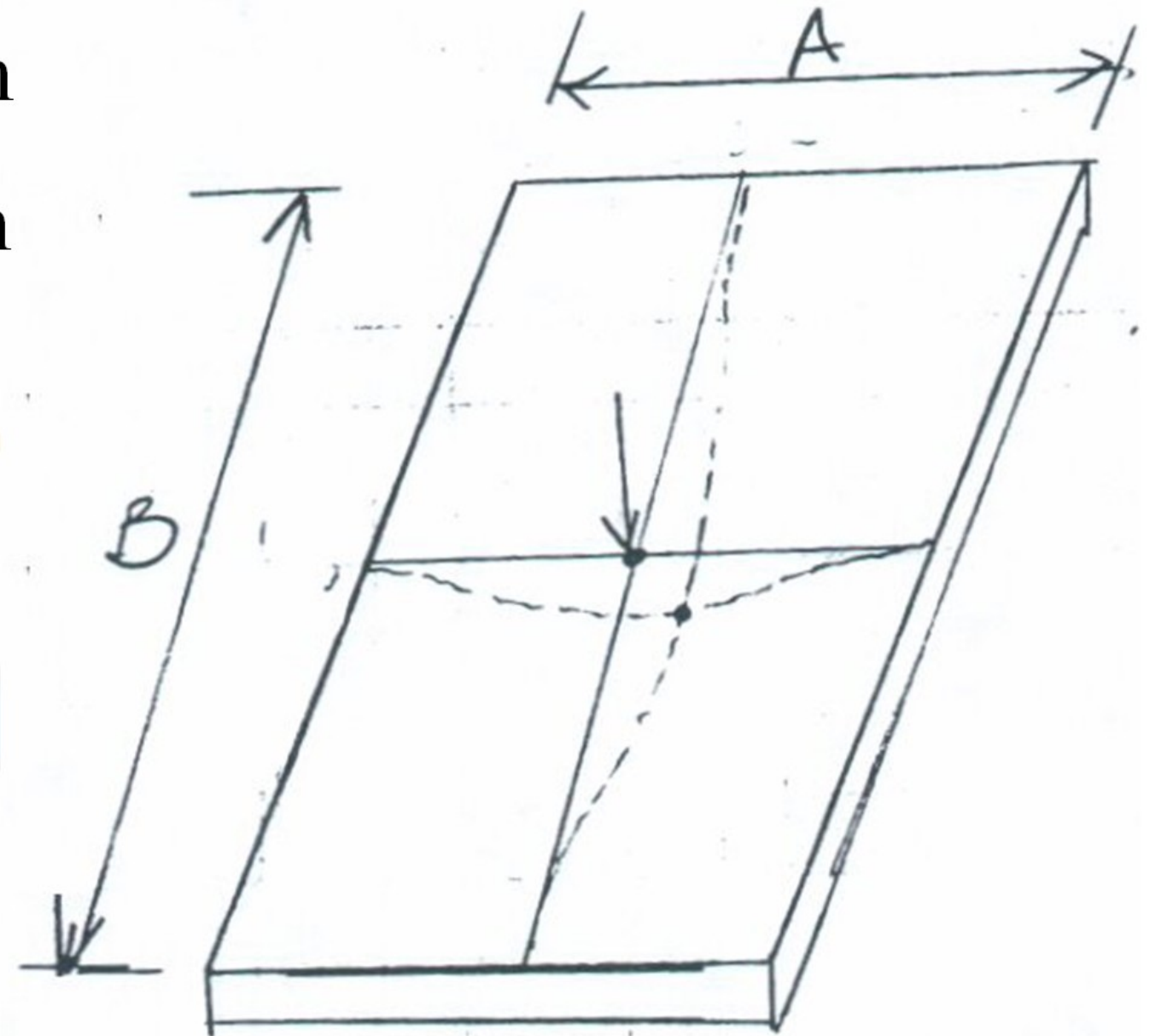
$w_l$  = load taken by long direction

$$\delta_A = \delta_B$$

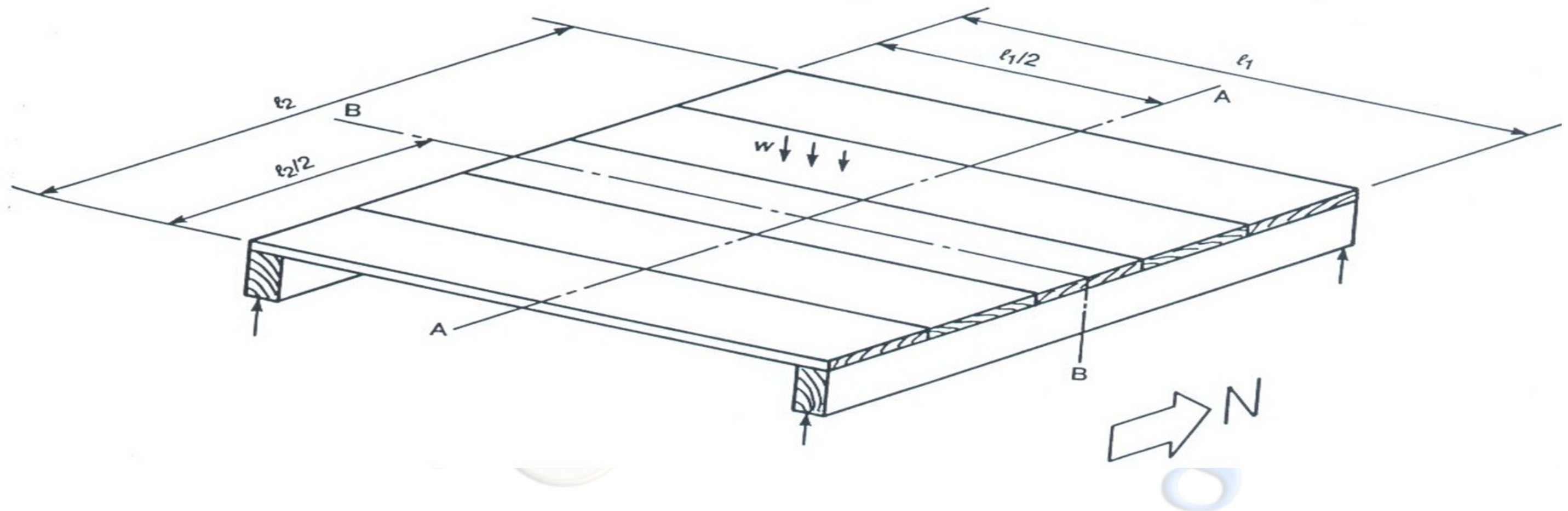
$$\frac{5w_s A^4}{384EI} = \frac{5w_l B^4}{384EI}$$

$$\frac{w_s}{w_l} = \frac{B^4}{A^4} \quad \text{For } B = 2A \Rightarrow w_s = 16w_l$$

**Rule of Thumb:** For  $B/A > 2$ ,  
design as one-way slab



# Analogy of 2-way slab to plank- beam floor

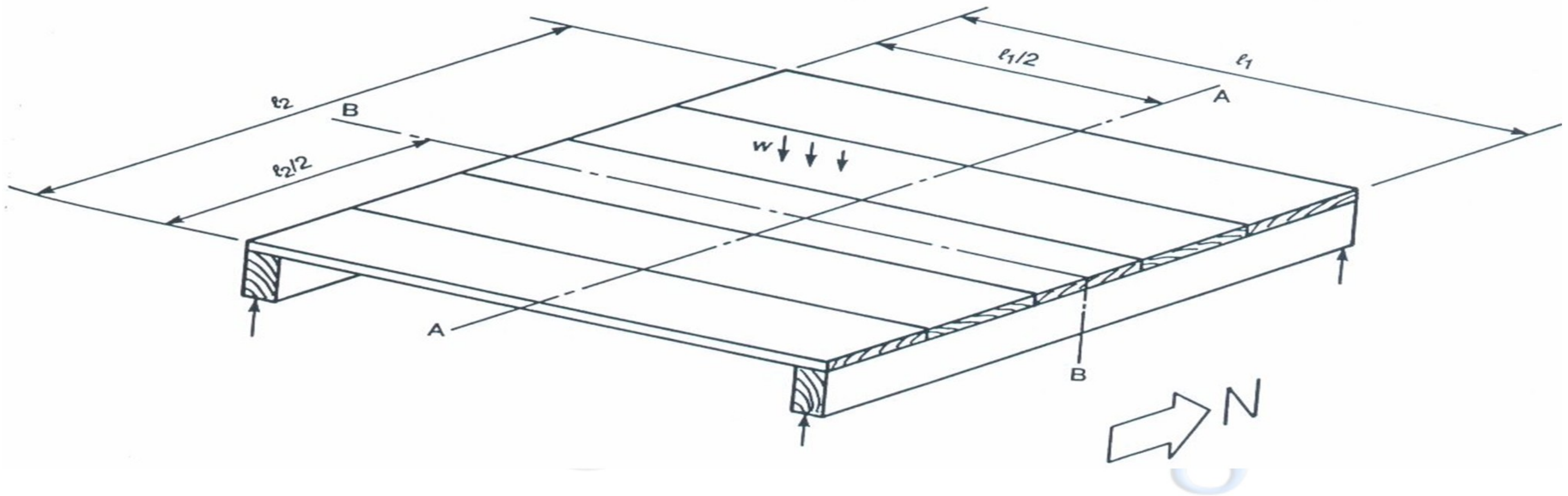


Section A-A:  $\Rightarrow M = \frac{wl_1^2}{8} \text{ KN-m/m}$

Moment per m width in planks

Total Moment  $\Rightarrow M_f = (wl_2) \frac{l_1^2}{8} \text{ KN-m}$

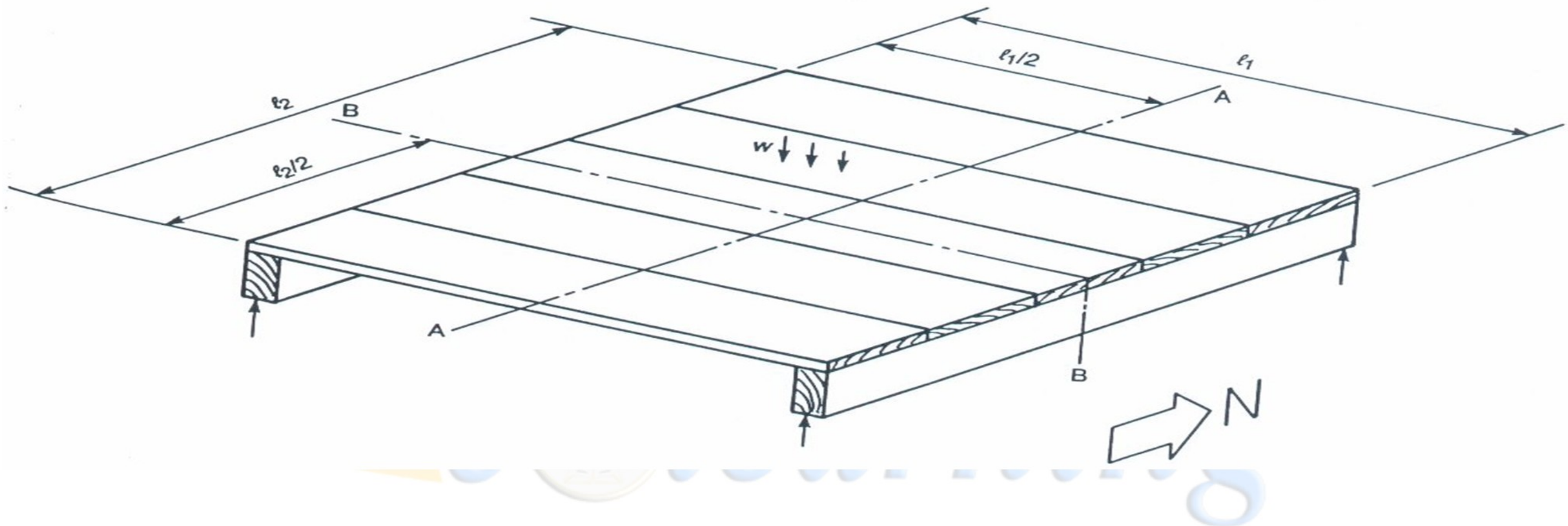
# Analogy of 2-way slab to plank-beam floor



Uniform load on each beam  $\Rightarrow \frac{wl_1}{2}$  KN/m

Moment in one beam (Sec: B-B)

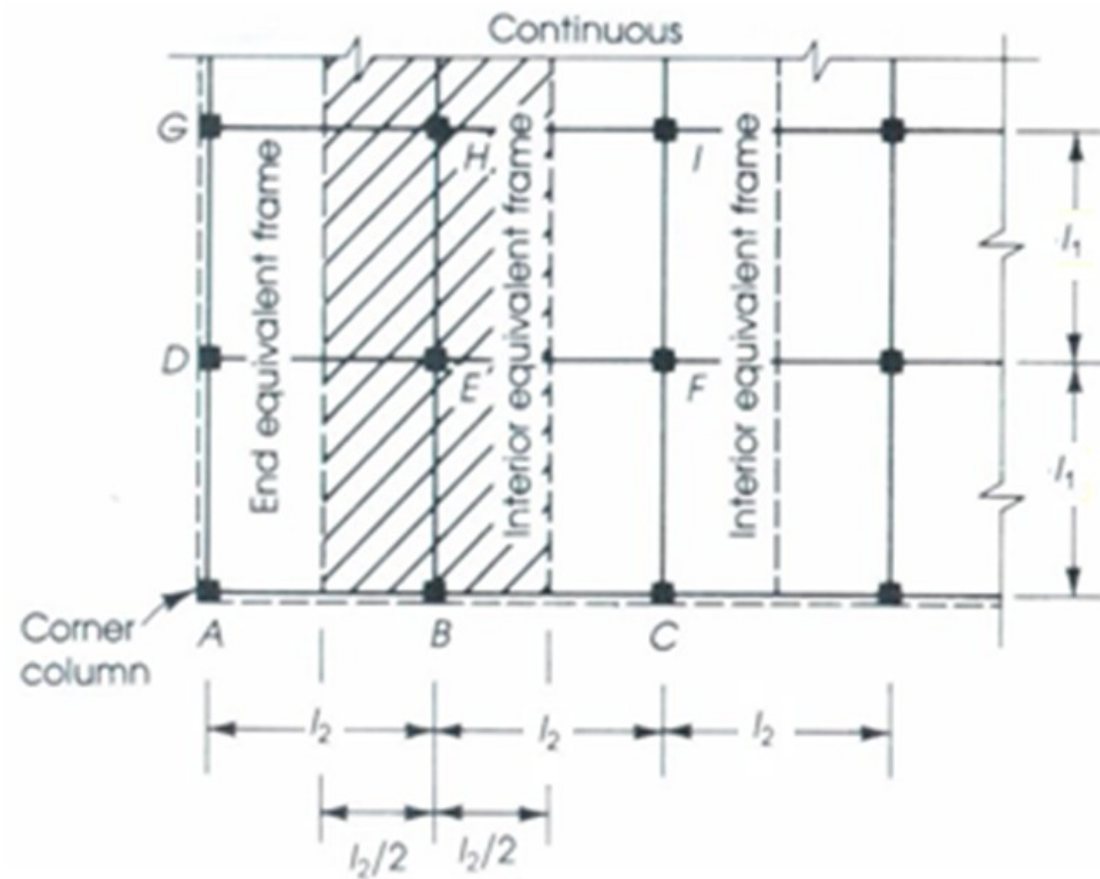
$$\Rightarrow M_{lb} = \left( \frac{wl_1}{2} \right) \frac{l_2^2}{8} \text{ KN.m}$$



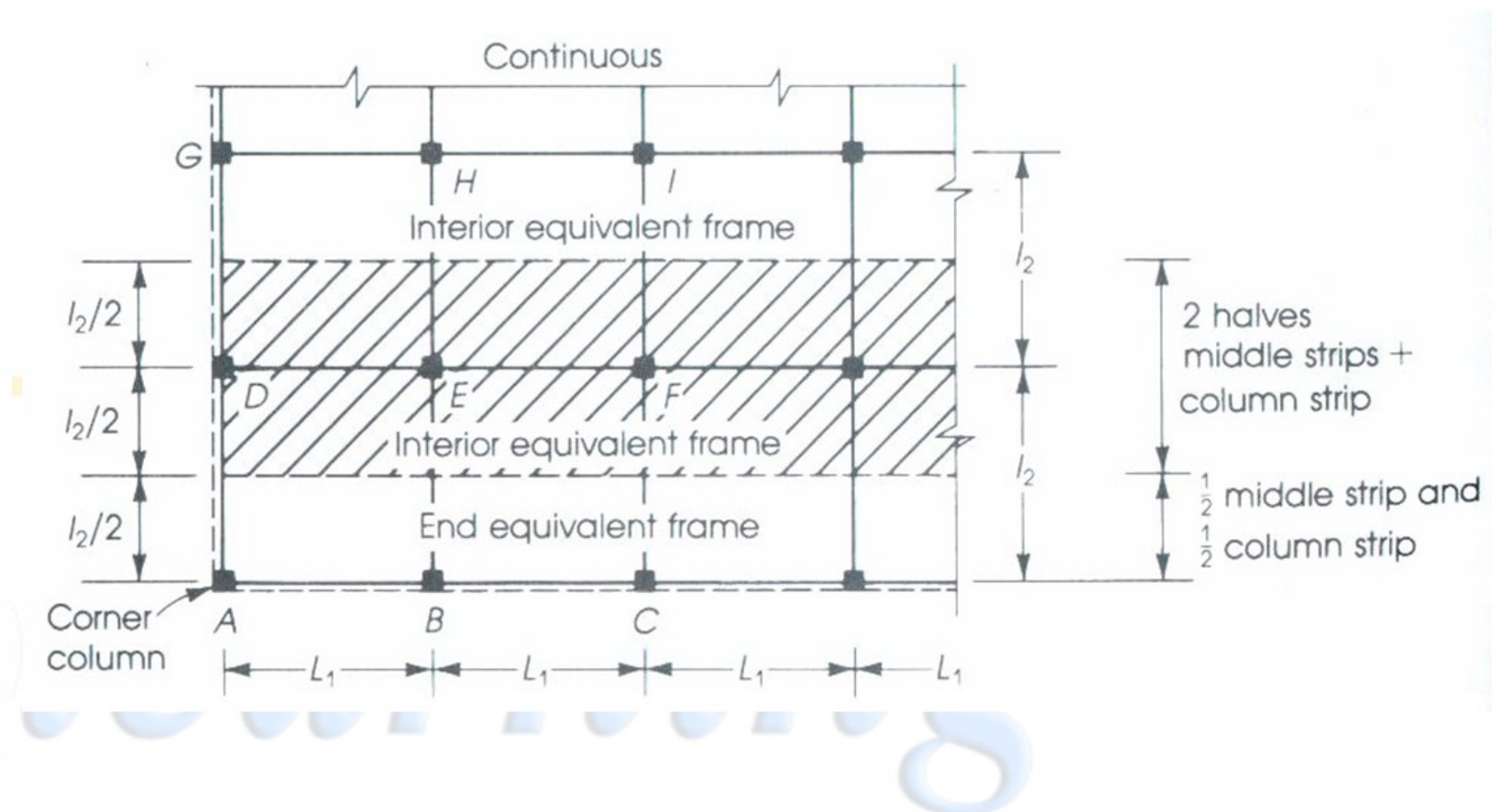
Total Moment in both beams  $\Rightarrow M = (wl_1) \frac{l_2^2}{8}$  KN.m

Full load was transferred east-west by the planks and then was transferred north-south by the beams;

The same is true for a two-way slab or any other floor system.



Longitudinal  
equivalent frame



Transverse equivalent  
frame

## (1) Direct Design Method (DDM)

Limited to slab systems to uniformly distributed loads and supported on equally spaced columns. Method uses a set of coefficients to determine the design moment at critical sections as long as two-way slab system meet the limitations of the ACI Code 13.6.1.

ACI Code 9.5.3 specifies min. thickness to control deflection. Three empirical limitations based on experimental research are necessary to be met:

(a) For  $0.2 \leq \alpha_{fm} \leq 2$

$$h = \frac{l_n \left( 0.8 + \frac{f_y}{1400} \right)}{36 + 5\beta (\alpha_{fm} - 0.2)}$$

$f_y$  in MPa. But h not less than 12.5cm

(b) For  $2 < \alpha_{fm}$

$$h = \frac{l_n \left( 0.8 + \frac{f_y}{1400} \right)}{36 + 9\beta}$$

$f_y$  in MPa. But h not less than 9cm.

(c) For  $\alpha_{fm} < 0.2$

Use table 9.5(c) in ACI code:

The definitions of the terms are:

$h$  = Minimum slab thickness without interior beams

$l_n$  = Clear span in long direction measured face to face of beam or column

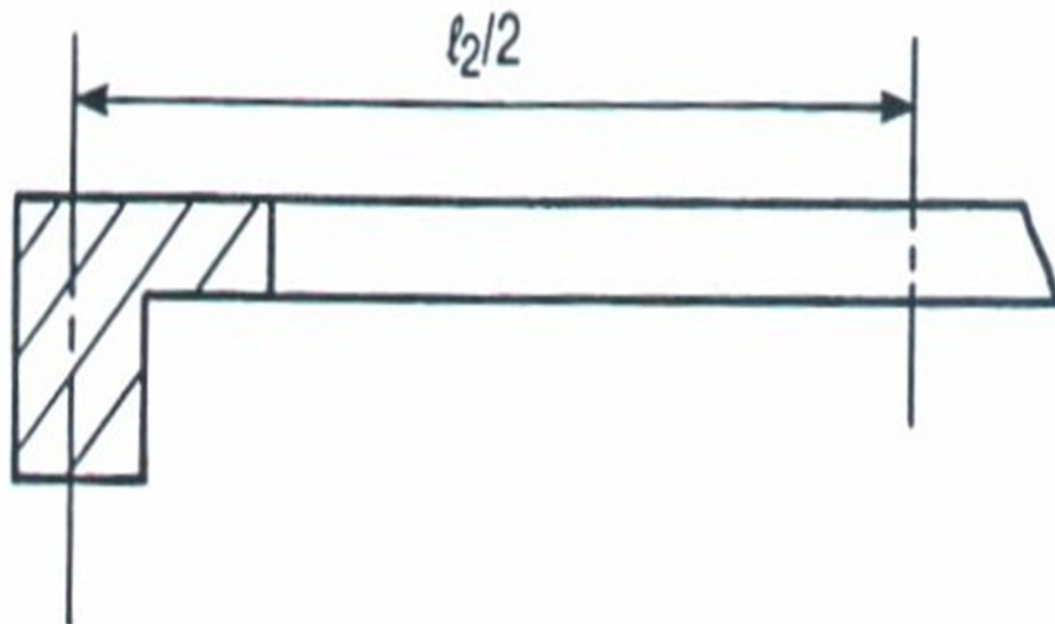
$\beta$  = ratio of the long to short clear span

$\alpha_{fm}$  = average value of  $\alpha_f$  for all beams on sides of panel.

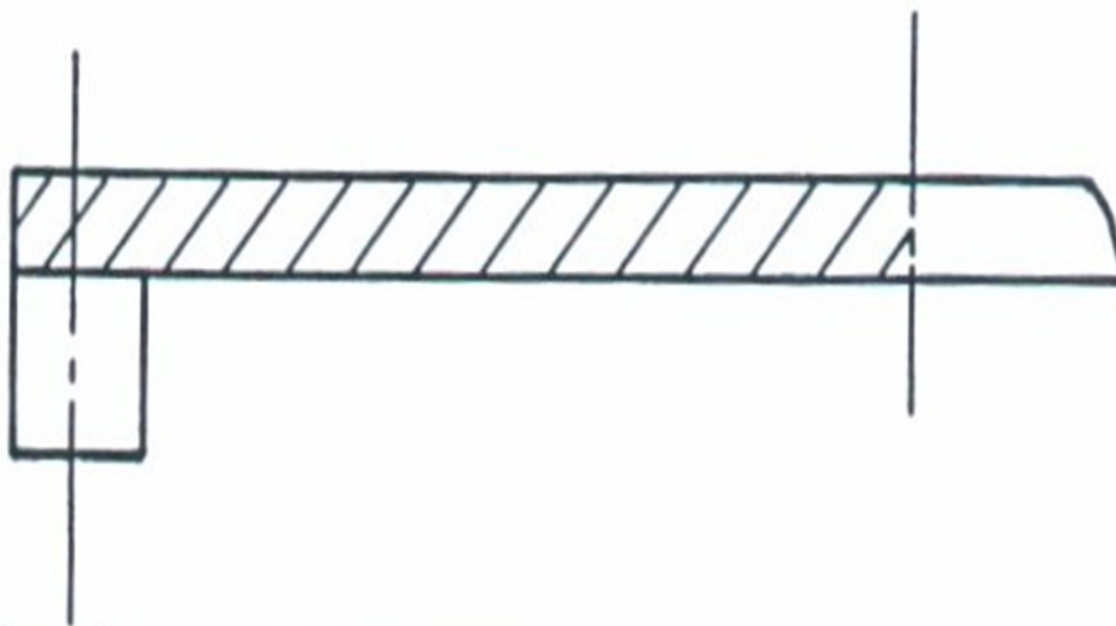
$$\alpha_f = \frac{\text{beam flex stiffn}}{\text{slab flex stiffn}} = \frac{4E_{cb}I_b / l}{4E_{cs}I_s / l} = \frac{E_{cb}I_b}{E_{cs}I_s}$$



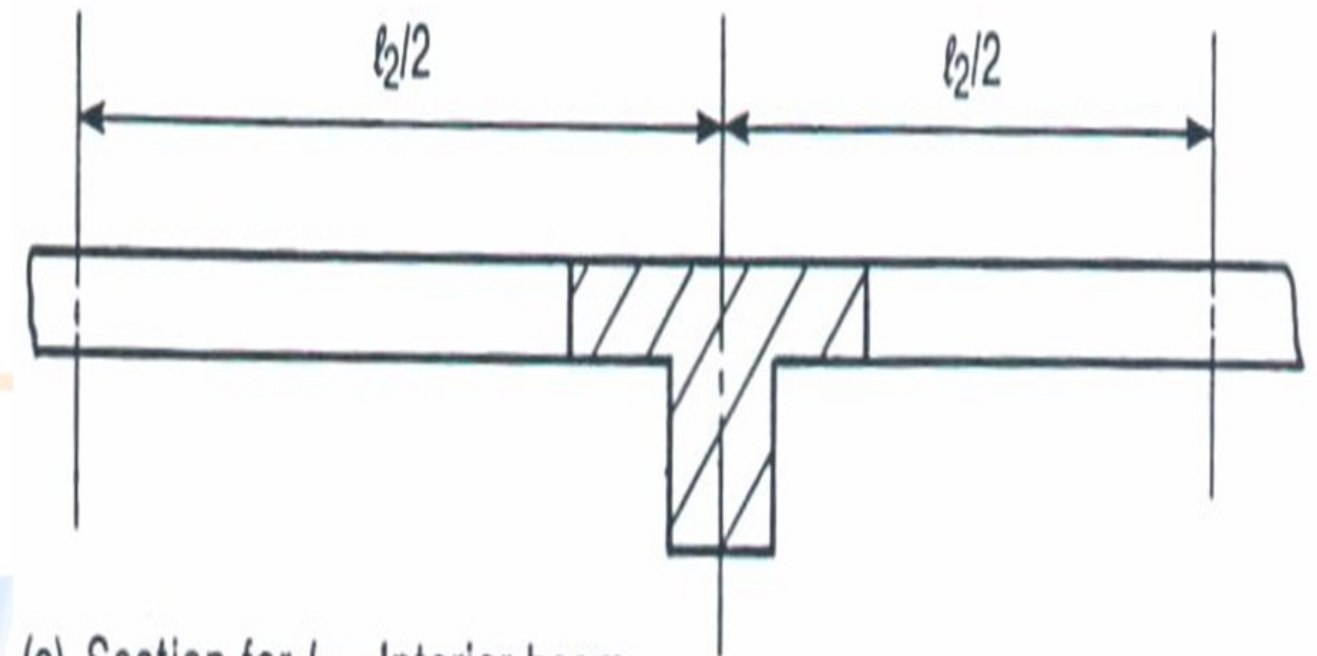
# Beam and Slab Sections for calculation of $\alpha$



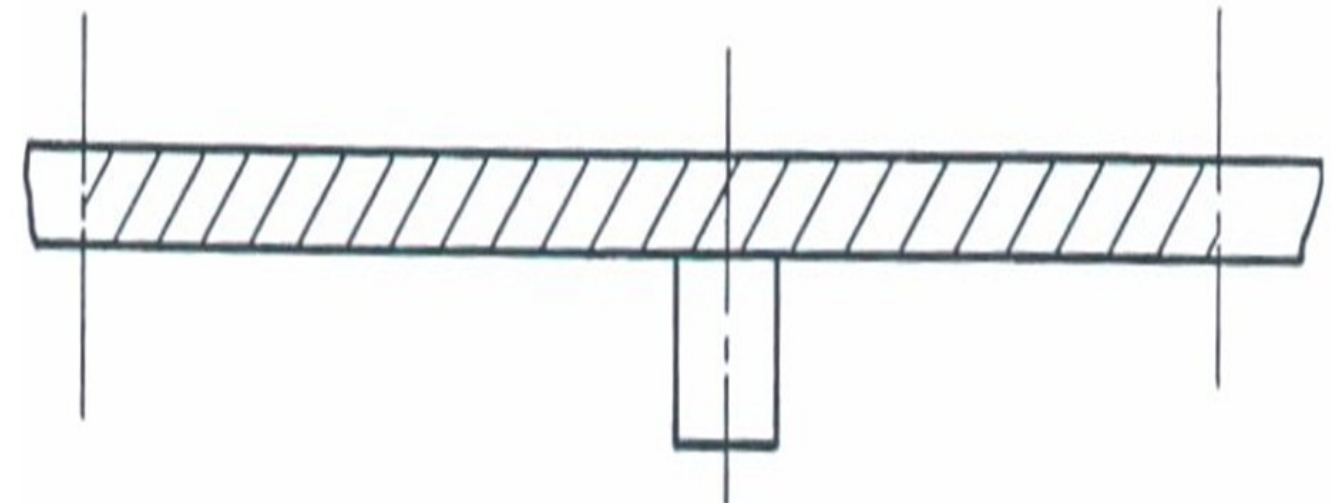
(a) Section for  $l_b$ —Edge beam.



(b) Section for  $l_s$ —Edge beam.

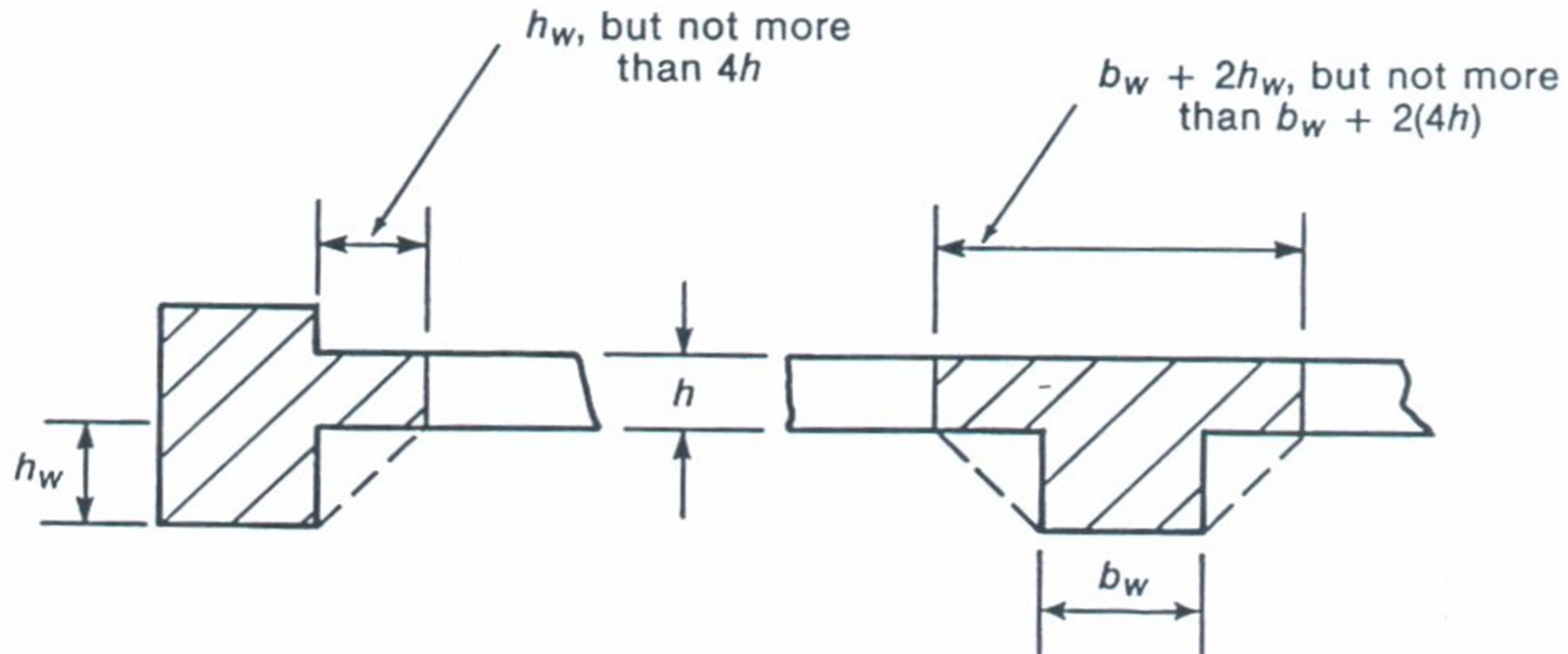


(c) Section for  $l_b$ —Interior beam.



(d) Section for  $l_s$ —Interior beam.

# Beam and Slab Sections for calculation of $\alpha$



Definition of beam cross-section, Charts used to calculate  $\alpha$

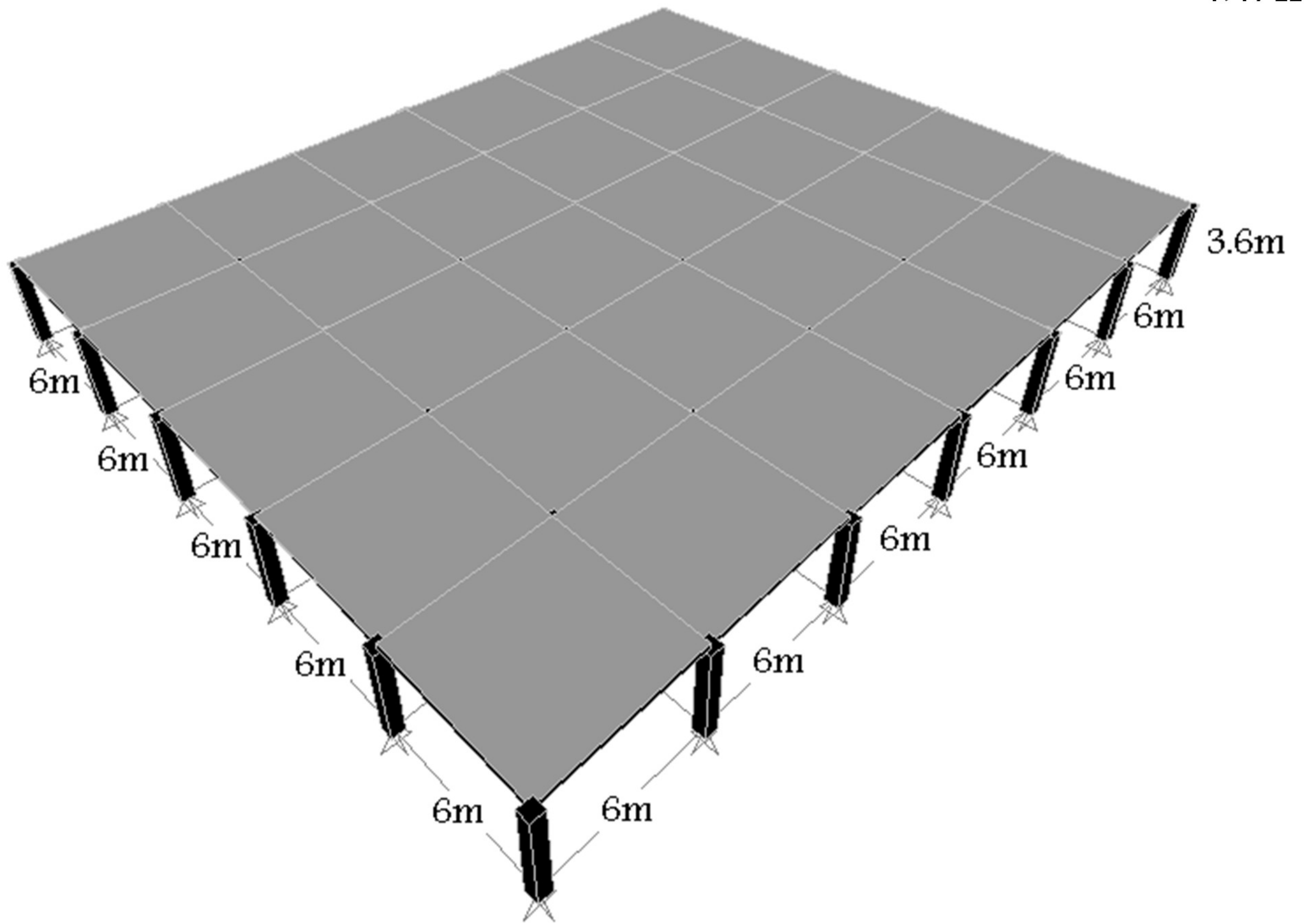
Slabs without drop panels meeting 13.3.7.1 and 13.3.7.2,

$h_{\min} = 12.5\text{cm}$

Slabs with drop panels meeting 13.3.7.1 and 13.3.7.2,

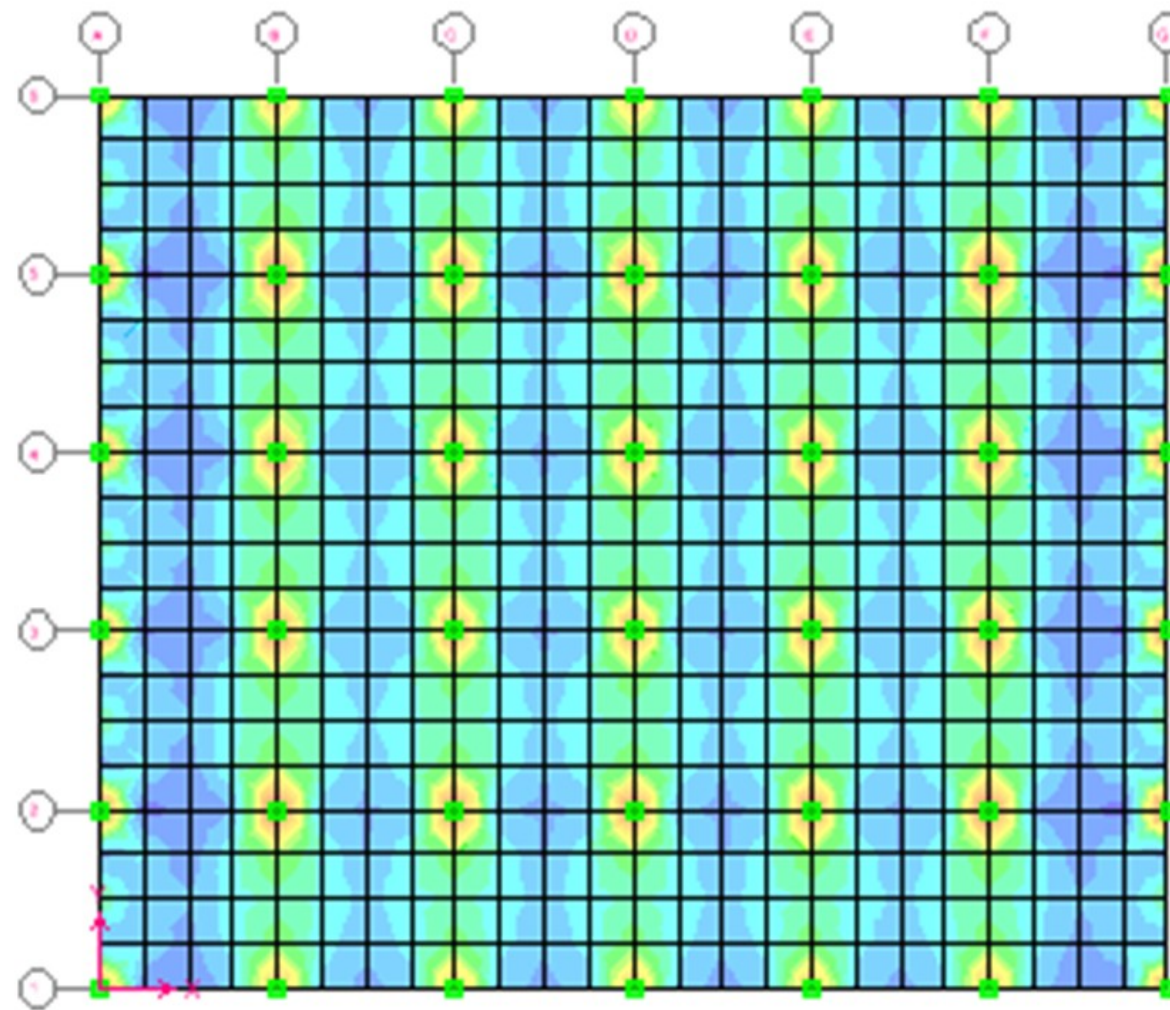
$h_{\min} = 10\text{cm}$

- Analyze and design (as a two way slab without beams) the following one story structure (3.6m height) using 3D model (figure next page):
  - Specifications: B350,  $f_y=4200 \text{ kg/cm}^2$ ,  
superimposed=  $50 \text{ kg/m}^2$  , live loads=  $350 \text{ kg/m}^2$ ,  
column dimensions 50cmX50cm



- Slab:
  - $h=550/30=18.33\text{cm}$  , use 20cm
  - $w_d = (0.2*2.5+0.05)=.55\text{t/m}^2$ ,  $w_l=0.35\text{t/m}^2$
  - $w_u=1.2*.55+1.6*0.35=1.22\text{t/m}^2$
  - $M_o = 1.22*6*(5.5)^2 / 8 = 27.7\text{t.m}$
  - $M_o^- = 0.65*27.7=18\text{t.m.}$ ,  $M_o^+ = 9.7\text{t.m.}$ ,
  - $(M_o^-)\text{c.s.} = 0.75*18=13.5\text{t.m.}$  ( $13.5/3=4.5\text{t.m/m}$ ),
  - $(M_o^-)\text{m.s.} = 0.25*18=4.5\text{t.m.}$  ( $4.5/3=1.5\text{t.m/m}$ ),
  - $(M_o^+)\text{c.s.} = 0.6*9.7=5.8\text{t.m.}$  ( $5.8/3=1.9\text{t.m/m}$ ),
  - $(M_o^+)\text{m.s.} = 0.4*9.7=3.9\text{t.m.}$  ( $3.9/3=1.3\text{t.m/m}$ ),

Support Reactions								
Story	Point	Load	FX	FY	FZ	MX	MY	MZ
BASE	34	LIVE	1.79	-0.25	130.35	0.270	2.147	0.000
BASE	42	LIVE	-4.88	-4.89	25.34	5.604	-5.581	0.000
Summation	0, 0, Base	DEAD	0.00	0.00	6747.84	101217.600	-121461.120	0.000
Summation	0, 0, Base	LIVE	0.00	0.00	3708.18	55622.700	-66747.240	0.000



# Column strip -ve: kN.m



## Section Cutting Line

	X	Y	Z
Start Point	18	19.5	3.6
End Point	18	16.5	3.6

## Resultant Force Location and Angle

X	Y	Z	Angle
18	18	3.6	-90.

Include ☒ Floors ☒ Beams ☐ Braces ☐ Columns ☐ Walls ☐ Ramps

## Integrated Forces

	Right Side			Left Side		
	1	2	Z	1	2	Z
Force	-0.3814	20.0929	-142.708	-0.3814	-20.0929	-142.708
Moment	166.1153	0.8749	-0.2674	-166.1153	0.8749	0.2674

# Middle strip -ve: kN.m



## Section Cutting Line

	X	Y	Z
Start Point	18	16.5	3.6
End Point	18	13.5	3.6

## Resultant Force Location and Angle

	X	Y	Z	Angle		
	18	15	3.6	-90.		
Include	<input checked="" type="checkbox"/> Floors	<input checked="" type="checkbox"/> Beams	<input type="checkbox"/> Braces	<input type="checkbox"/> Columns	<input type="checkbox"/> Walls	<input type="checkbox"/> Ramps

## Integrated Forces

	Right Side			Left Side		
	1	2	Z	1	2	Z
Force	-8.926E-14	20.0192	-19.3793	5.960E-14	-20.0192	-19.3793
Moment	42.5449	-1.798E-13	-4.965E-14	-42.5449	-7.411E-13	-3.268E-14

- Analyze and design (as a two way slab with beams) the previous one story structure Specifications: B350,  $f_y=4200$  kg/cm<sup>2</sup>, superimposed= 50 kg/m<sup>2</sup>, live loads= 350 kg/m<sup>2</sup>, beam 30cm width by 50cm depth, column dimensions 50cmX50cm,

- $h=550/36=15.3\text{cm}$  , use 20cm. Beam use 30cm\*50cm depth (ignore additional weight of beam)
  - $w_d = (0.2*2.5+0.05)=.55\text{t/m}^2$ ,  $w_l=0.35\text{t/m}^2$
  - $w_u=1.2*.55+1.6*0.35=1.22\text{t/m}^2$
  - $M_o = 1.22*6*(5.5)^2 / 8 = 27.7\text{t.m}$
  - $M_o^- = 0.65*27.7=18\text{t.m.}$ ,  $M_o^+ = 9.7\text{t.m.}$ ,
  - $I_b = 5*10^{-3} \text{ m}^4$ ,  $I_s = 4*10^{-3} \text{ m}^4$ ,  $\alpha=1.25$ ,  $\alpha I_2 / I_1 = 1.25$
  - $(M_o^-)_{cs}=0.75*18=13.5\text{t.m.}$  ( $2/2.1=0.95\text{t.m/m}$ ,  $B=11.5\text{t.m}$ )
  - $(M_o^-)_{ms}=0.25*18=4.5\text{t.m.}$  ( $4.5/3=1.5\text{t.m/m}$ ),
  - $(M_o^+)_{cs}= 0.75*9.7=7.3\text{t.m}$  ( $1.1/2.1=0.52\text{t.m/m}$ ,  $B=6.2\text{t.m}$ )
  - $(M_o^+)_{ms}= 0.25*9.7=2.4\text{t.m.}$  ( $2.4/3=0.8\text{t.m/m}$ ),



# Verify equilibrium: Etabs output

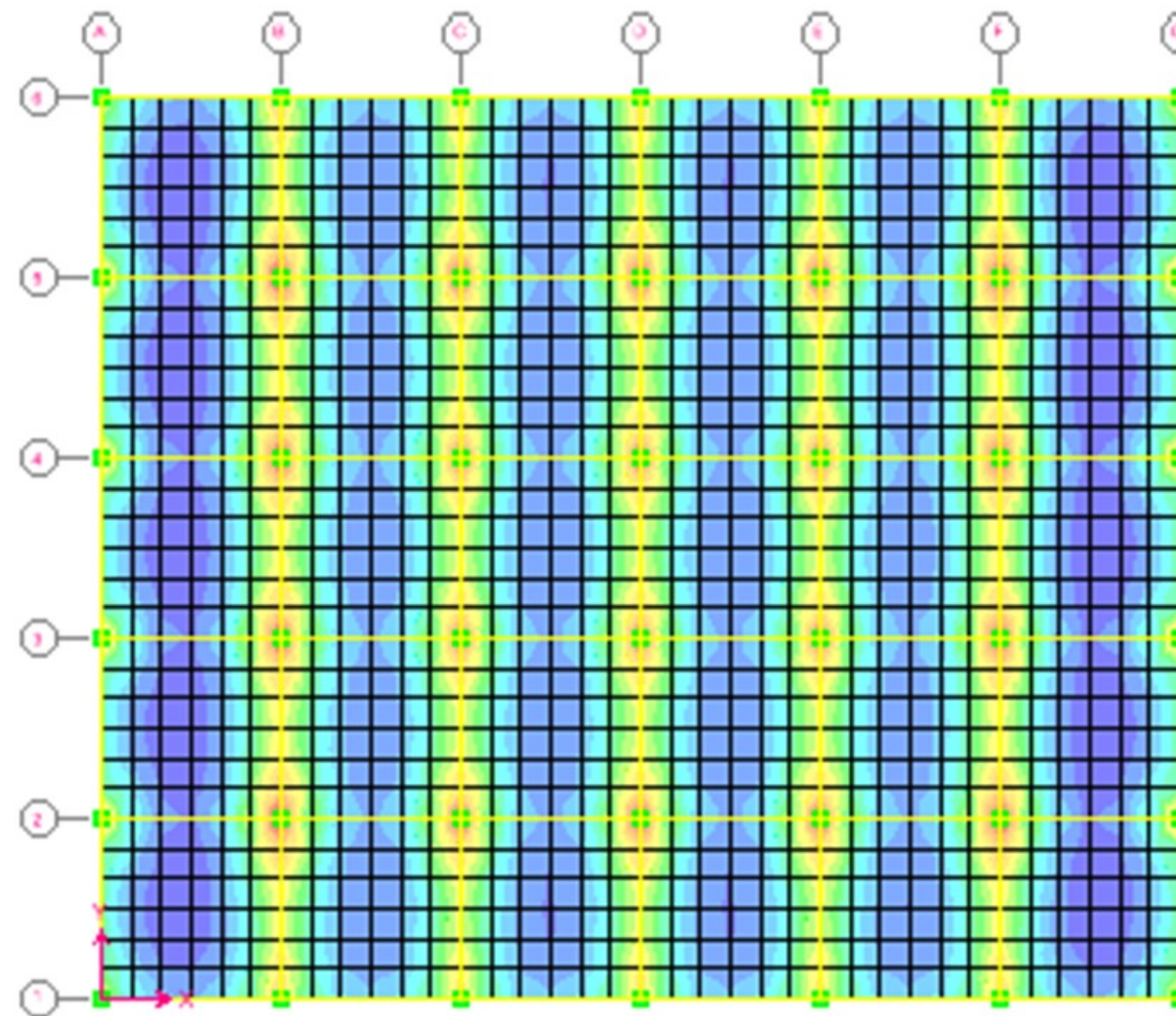


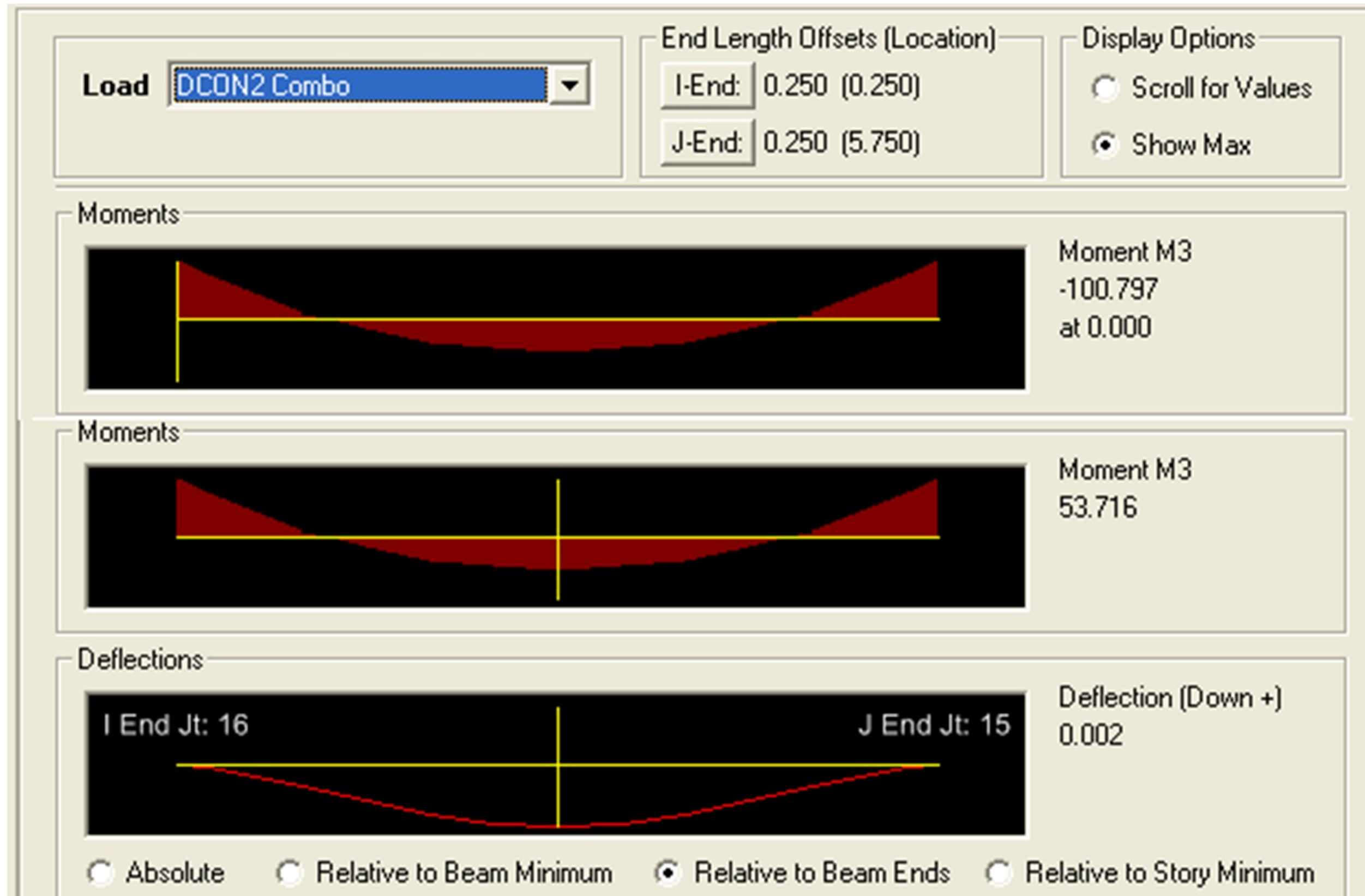
view

Support Reactions

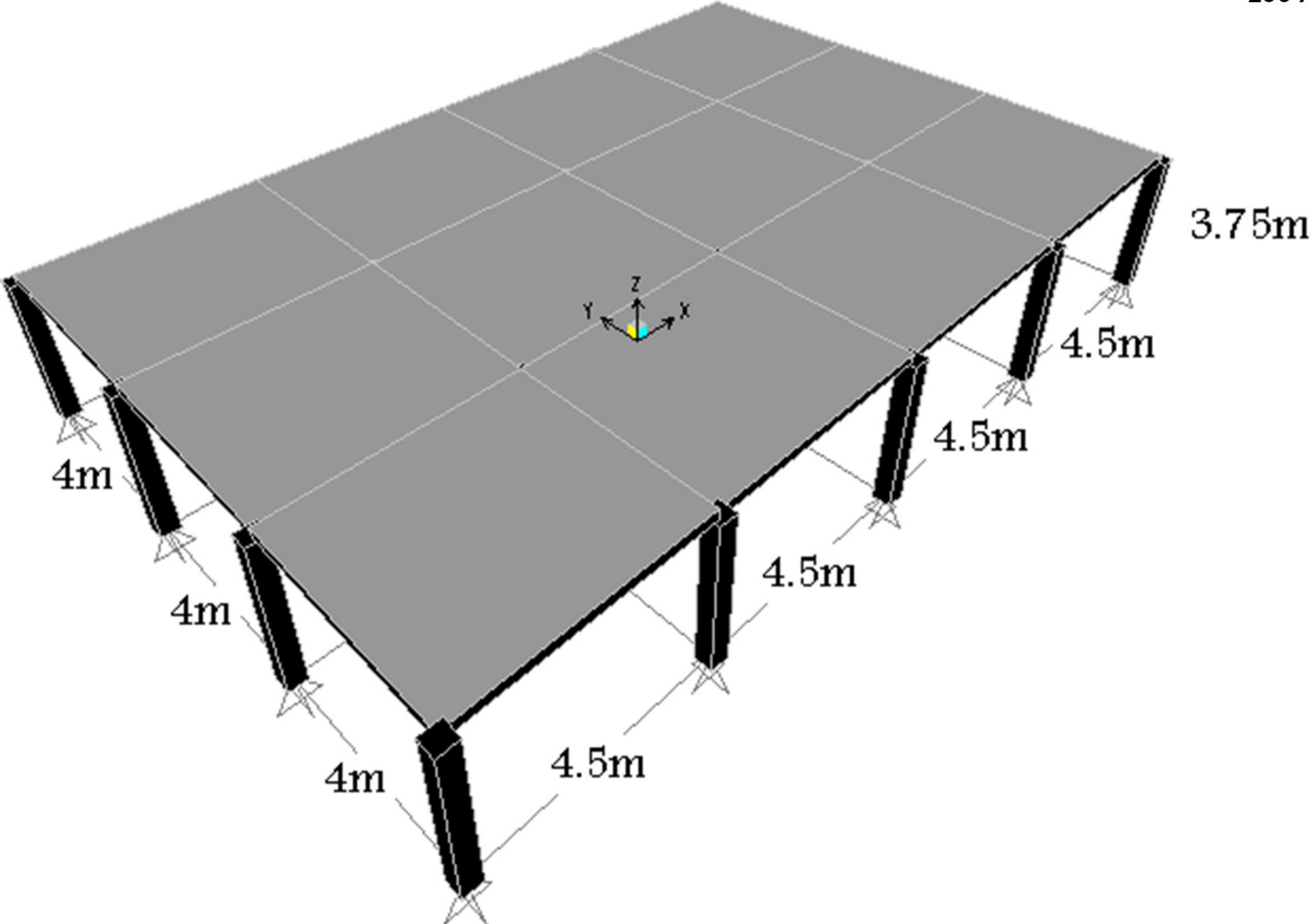
Story	Point	Load	FX	FY	FZ	MX	MY	MZ
BASE	38	DCON2	-47.81	-4.34	269.57	5.235	-55.265	0.010
Summation	0, 0, Base	DEAD	0.00	0.00	8313.39	124700.850	-149641.020	0.000
Summation	0, 0, Base	LIVE	0.00	0.00	3708.18	55622.700	-66747.240	0.000







- Analyze and design (as a two way slab) the following one story structure (3.75m height) using 3D model (figure next slide):
  - Specifications: B350,  $f_y=4200 \text{ kg/cm}^2$ ,  
superimposed=  $100 \text{ kg/m}^2$  , live loads=  $200 \text{ kg/m}^2$ ,  
column dimensions 35cmX35cm
- Slab without beams 14cm thickness
- Slab 14cm thickness, beams 35cm width by 55cm depth
- Slab 14cm thickness, beams 35cm width by 25cm depth

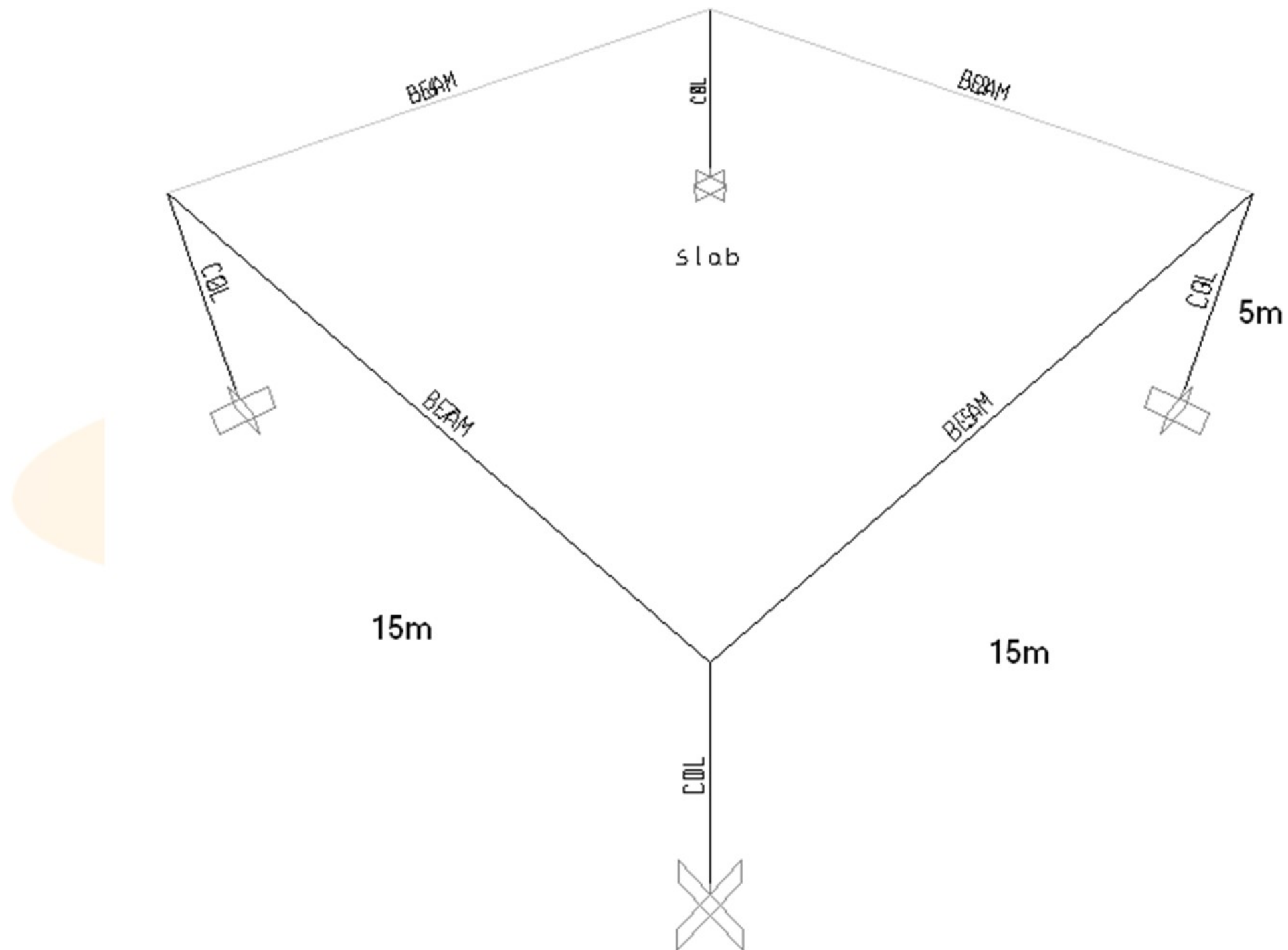


**End of section 5.3**

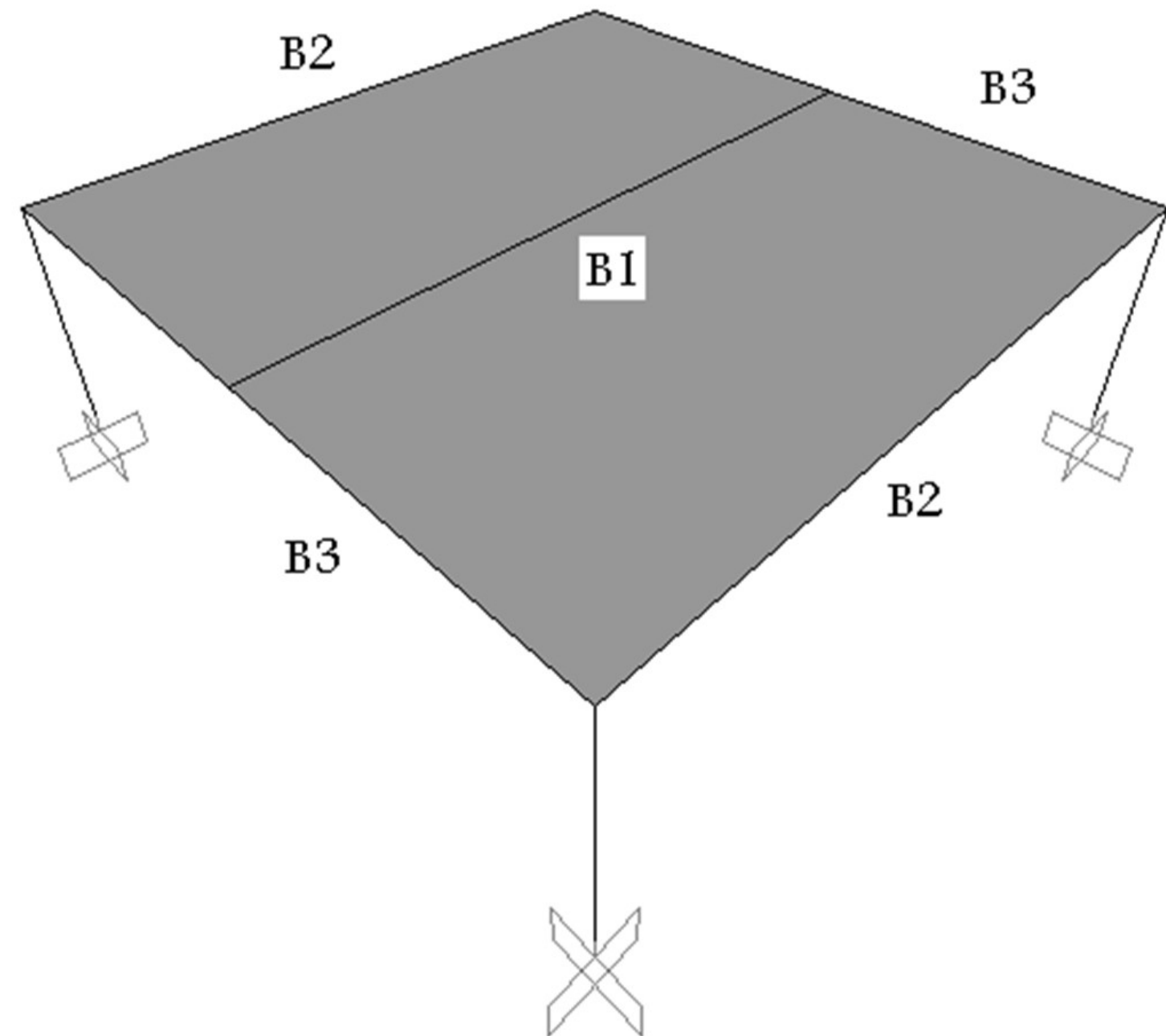
Let Learning Continue

## 5.4 Systems without vertical continuity

- Analyze a one story reinforced concrete structure (entertainment hall) made of one panel 50cm solid slab sitting on drop beams of 0.5m width and 1m depth supported on four square columns 50cm dimensions, 5m height and 15m span. The superimposed and live loads are  $300\text{kg/m}^2$  and  $400\text{kg/m}^2$  respectively.



- The structural engineer is required to consider the following design alternative for the entertainment hall



- Analyze the design alternative using local practice (slab-beam-column load path)
- Analyze the design alternative using 3D model:
- C. Compare A and B
- D. Write a report to the client persuading him the validity of your findings

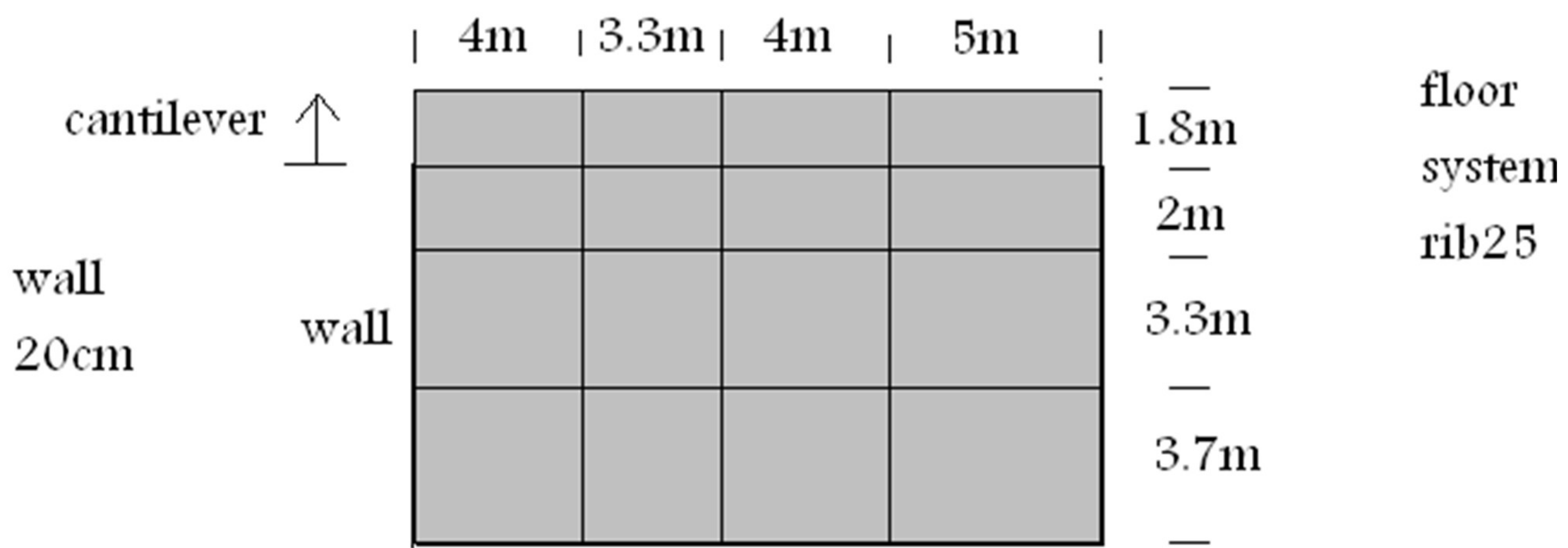
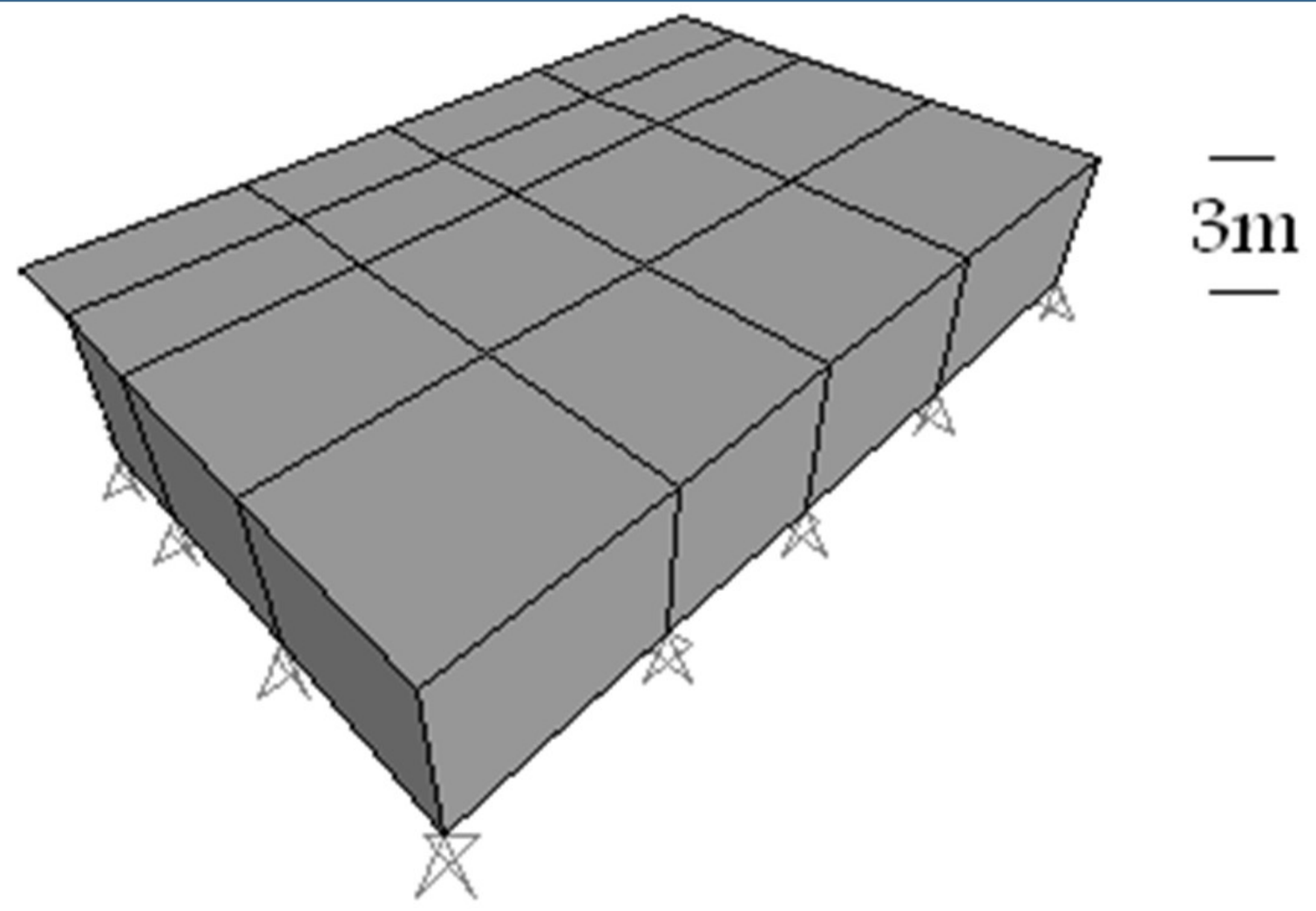
**End of section 5.4**

Let Learning Continue

Representation of ribs over slabs is usually inefficient modeling in general shape buildings. Another procedure is to use an equivalent solid slab of uniform thickness but preserving:

- ☐ Stiffness ratios in both directions.
- ☐ Dead weight of slab.

- **Floor system ribs 25cm**
- **Wall 20cm**
- **Superimposed  $300\text{kg/m}^2$**
- **Live load  $300\text{kg/m}^2$**
- **$E_{\text{con}}=2.20\text{Mt/m}^2$ , density= $2.5\text{t/m}^3$**
- **Columns are rectangular 20cmX30cm**



**End of section 5.5**

Let Learning Continue

- Table 1604.5 IBC2009\ Occupancy category
- Table 1607.1 IBC2009\ Live load
- Table 9.5a ACI code
- Table 9.5c
- Table 12.15.2
- ACI 13.6.1 DDM limitations
- Fig. 13.3.8

**TABLE 1604.5**  
**OCCUPANCY CATEGORY OF BUILDINGS AND OTHER STRUCTURES**

OCCUPANCY CATEGORY	NATURE OF OCCUPANCY
I	Buildings and other structures that represent a low hazard to human life in the event of failure, including but not limited to: <ul style="list-style-type: none"> <li>• Agricultural facilities.</li> <li>• Certain temporary facilities.</li> <li>• Minor storage facilities.</li> </ul>
II	Buildings and other structures except those listed in Occupancy Categories I, III and IV
III	Buildings and other structures that represent a substantial hazard to human life in the event of failure, including but not limited to: <ul style="list-style-type: none"> <li>• Buildings and other structures whose primary occupancy is public assembly with an occupant load greater than 300.</li> <li>• Buildings and other structures containing elementary school, secondary school or day care facilities with an occupant load greater than 250.</li> <li>• Buildings and other structures containing adult education facilities, such as colleges and universities with an occupant load greater than 500.</li> <li>• Group I-2 occupancies with an occupant load of 50 or more resident patients but not having surgery or emergency treatment facilities.</li> <li>• Group I-3 occupancies.</li> <li>• Any other occupancy with an occupant load greater than 5,000<sup>a</sup>.</li> <li>• Power-generating stations, water treatment facilities for potable water, waste water treatment facilities and other public utility facilities not included in Occupancy Category IV.</li> <li>• Buildings and other structures not included in Occupancy Category IV containing sufficient quantities of toxic or explosive substances to be dangerous to the public if released.</li> </ul>
IV	Buildings and other structures designated as essential facilities, including but not limited to: <ul style="list-style-type: none"> <li>• Group I-2 occupancies having surgery or emergency treatment facilities.</li> <li>• Fire, rescue, ambulance and police stations and emergency vehicle garages.</li> <li>• Designated earthquake, hurricane or other emergency shelters.</li> <li>• Designated emergency preparedness, communications and operations centers and other facilities required for emergency response.</li> <li>• Power-generating stations and other public utility facilities required as emergency backup facilities for Occupancy</li> </ul>

**TABLE 1607.1**  
**MINIMUM UNIFORMLY DISTRIBUTED LIVE LOADS,  $L_o$ , AND**  
**MINIMUM CONCENTRATED LIVE LOADS<sup>g</sup>**

OCCUPANCY OR USE	UNIFORM (psf)	CONCENTRATED (lbs.)
1. Apartments (see residential)	—	—
2. Access floor systems		
Office use	50	2,000
Computer use	100	2,000
3. Armories and drill rooms	150	—
4. Assembly areas and theaters		
Fixed seats (fastened to floor)	60	
Follow spot, projections and control rooms	50	—
Lobbies	100	
Movable seats	100	
Stages and platforms	125	
Other assembly areas	100	
5. Balconies (exterior) and decks <sup>h</sup>	Same as occupancy served	—
6. Bowling alleys	75	—
7. Catwalks	40	300
8. Cornices	60	—
9. Corridors, except as otherwise indicated	100	—

**TABLE 1607.1—continued**  
**MINIMUM UNIFORMLY DISTRIBUTED LIVE LOADS,  $L_o$ , AND**  
**MINIMUM CONCENTRATED LIVE LOADS<sup>g</sup>**

OCCUPANCY OR USE	UNIFORM (psf)	CONCENTRATED (lbs.)
23. Manufacturing		
Heavy	250	3,000
Light	125	2,000
24. Marquees	75	—
25. Office buildings		
Corridors above first floor	80	2,000
File and computer rooms shall be designed for heavier loads based on anticipated occupancy	—	—
Lobbies and first-floor corridors	100	2,000
Offices	50	2,000
26. Penal institutions		
Cell blocks	40	—
Corridors	100	
27. Residential		
One- and two-family dwellings		
Uninhabitable attics without storage <sup>i</sup>	10	
Uninhabitable attics with limited storage <sup>i, j, k</sup>	20	
Habitable attics and sleeping areas	30	
All other areas	40	—
Hotels and multifamily dwellings		
Private rooms and corridors serving them	40	
Public rooms and corridors serving them	100	

10. Dance halls and ballrooms	100	—
11. Dining rooms and restaurants	100	—
12. Dwellings (see residential)	—	—
13. Elevator machine room grating (on area of 4 in <sup>2</sup> )	—	300
14. Finish light floor plate construction (on area of 1 in <sup>2</sup> )	—	200
15. Fire escapes On single-family dwellings only	100 40	—
16. Garages (passenger vehicles only) Trucks and buses	40 See Section 1607.6	Note a
17. Grandstands (see stadium and arena bleachers)	—	—
18. Gymnasiums, main floors and balconies	100	—
19. Handrails, guards and grab bars	See Section 1607.7	
20. Hospitals Corridors above first floor Operating rooms, laboratories Patient rooms	80 60 40	1,000 1,000 1,000
21. Hotels (see residential)	—	—
22. Libraries Corridors above first floor Reading rooms Stack rooms	80 60 150 <sup>b</sup>	1,000 1,000 1,000

continued

28. Reviewing stands, grandstands and bleachers	Note c	
29. Roofs All roof surfaces subject to maintenance workers Awnings and canopies Fabric construction supported by a lightweight rigid skeleton structure All other construction Ordinary flat, pitched, and curved roofs Primary roof members, exposed to a work floor Single panel point of lower chord of roof trusses or any point along primary structural members supporting roofs: Over manufacturing, storage warehouses, and repair garages All other occupancies Roofs used for other special purposes Roofs used for promenade purposes Roofs used for roof gardens or assembly purposes	5 nonreducible 20 20       Note 1 60 100	300          2,000 300 Note 1
30. Schools Classrooms Corridors above first floor First-floor corridors	40 80 100	1,000 1,000 1,000
31. Scuttles, skylight ribs and accessible ceilings	—	200
32. Sidewalks, vehicular driveways and yards, subject to trucking	250 <sup>d</sup>	8,000 <sup>e</sup>
33. Skating rinks	100	—

continued

**TABLE 1607.1—continued**  
**MINIMUM UNIFORMLY DISTRIBUTED LIVE LOADS,  $L_u$ , AND**  
**MINIMUM CONCENTRATED LIVE LOADS<sup>g</sup>**

OCCUPANCY OR USE	UNIFORM (psf)	CONCENTRATED (lbs.)
34. Stadiums and arenas Bleachers Fixed seats (fastened to floor)	100 <sup>c</sup> 60 <sup>c</sup>	—
35. Stairs and exits One- and two-family dwellings All other	40 100	Note f
36. Storage warehouses (shall be designed for heavier loads if required for anticipated storage) Heavy Light	250 125	
37. Stores Retail First floor Upper floors Wholesale, all floors	100 75 125	1,000 1,000 1,000
38. Vehicle barrier systems	See Section 1607.7.3	
39. Walkways and elevated platforms (other than exitways)	60	—
40. Yards and terraces, pedestrians	100	—

For SI: 1 inch = 25.4 mm, 1 square inch = 645.16 mm<sup>2</sup>,  
1 square foot = 0.0929 m<sup>2</sup>,  
1 pound per square foot = 0.0479 kN/m<sup>2</sup>, 1 pound = 0.004448 kN,  
1 pound per cubic foot = 16 kg/m<sup>3</sup>

**TABLE 9.5(a) — MINIMUM THICKNESS OF NONPRESTRESSED BEAMS OR ONE-WAY SLABS UNLESS DEFLECTIONS ARE CALCULATED**

	Minimum thickness, $h$			
	Simply supported	One end continuous	Both ends continuous	Cantilever
Member	Members not supporting or attached to partitions or other construction likely to be damaged by large deflections			
Solid one-way slabs	$l/20$	$l/24$	$l/28$	$l/10$
Beams or ribbed one-way slabs	$l/16$	$l/18.5$	$l/21$	$l/8$

Notes:

Values given shall be used directly for members with normalweight concrete and Grade 420 reinforcement. For other conditions, the values shall be modified as follows:

a) For lightweight concrete having equilibrium density,  $w_c$ , in the range of 1440 to 1840 kg/m<sup>3</sup>, the values shall be multiplied by  $(1.65 - 0.0003w_c)$  but not less than 1.09.

b) For  $f_y$  other than 420 MPa, the values shall be multiplied by  $(0.4 + f_y/700)$ .

**TABLE 9.5(c)—MINIMUM THICKNESS OF SLABS WITHOUT INTERIOR BEAMS\***

$f_y$ , MPa <sup>†</sup>	Without drop panels <sup>‡</sup>			With drop panels <sup>‡</sup>		
	Exterior panels		Interior panels	Exterior panels		Interior panels
	Without edge beams	With edge beams <sup>§</sup>		Without edge beams	With edge beams <sup>§</sup>	
280	$\ell_n/33$	$\ell_n/36$	$\ell_n/36$	$\ell_n/36$	$\ell_n/40$	$\ell_n/40$
420	$\ell_n/30$	$\ell_n/33$	$\ell_n/33$	$\ell_n/33$	$\ell_n/36$	$\ell_n/36$
520	$\ell_n/28$	$\ell_n/31$	$\ell_n/31$	$\ell_n/31$	$\ell_n/34$	$\ell_n/34$

\*For two-way construction,  $\ell_n$  is the length of clear span in the long direction, measured face-to-face of supports in slabs without beams and face-to-face of beams or other supports in other cases.

<sup>†</sup>For  $f_y$  between the values given in the table, minimum thickness shall be determined by linear interpolation.

<sup>‡</sup>Drop panels as defined in 13.2.5.

<sup>§</sup>Slabs with beams between columns along exterior edges. The value of  $\alpha_f$  for the edge beam shall not be less than 0.8.

**TABLE R12.15.2 — TENSION LAP SPLICES**

$\frac{A_s \text{ provided}^*}{A_s \text{ required}}$	Maximum percent of $A_s$ spliced within required lap length	
	50	100
Equal to or greater than 2	Class A	Class B
Less than 2	Class B	Class B
<sup>*</sup> Ratio of area of reinforcement provided to area of reinforcement required by analysis at splice locations.		

### 13.6.1 — Limitations

Design of slab systems within the limitations of 13.6.1.1 through 13.6.1.8 by the direct design method shall be permitted.

**13.6.1.1** — There shall be a minimum of three continuous spans in each direction.

**13.6.1.2** — Panels shall be rectangular, with a ratio of longer to shorter span center-to-center of supports within a panel not greater than 2.

**13.6.1.3** — Successive span lengths center-to-center of supports in each direction shall not differ by more than one-third the longer span.

**13.6.1.4** — Offset of columns by a maximum of 10 percent of the span (in direction of offset) from either axis between centerlines of successive columns shall be permitted.

**13.6.1.5** — All loads shall be due to gravity only and uniformly distributed over an entire panel. The unfactored live load shall not exceed two times the unfactored dead load.

**13.6.1.6** — For a panel with beams between supports on all sides, Eq. (13-2) shall be satisfied for beams in the two perpendicular directions

$$0.2 \leq \frac{\alpha_{f1} \ell_2^2}{\alpha_{f2} \ell_1^2} \leq 5.0 \quad (13-2)$$

where  $\alpha_{f1}$  and  $\alpha_{f2}$  are calculated in accordance with Eq. (13-3).

$$\alpha_f = \frac{E_{cb} I_b}{E_{cs} I_s} \quad (13-3)$$

## CODE

## COMMENTARY

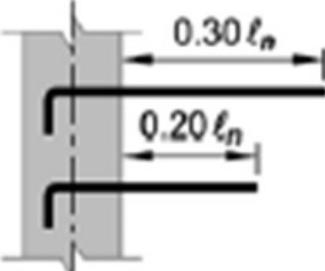
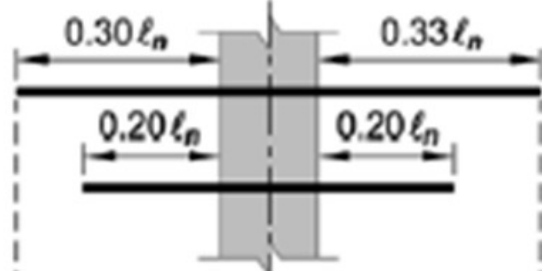
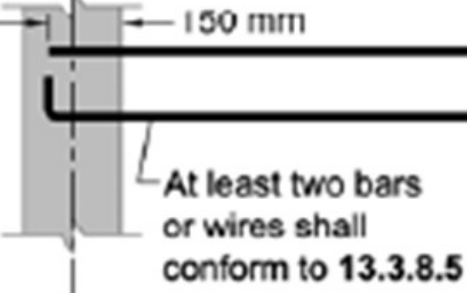
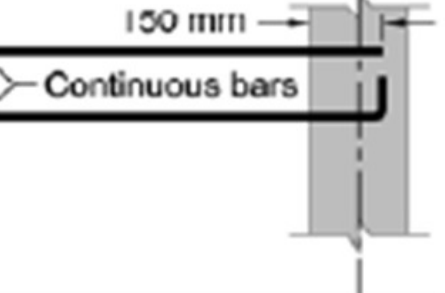
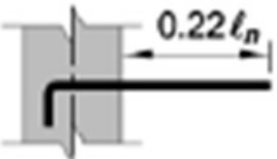

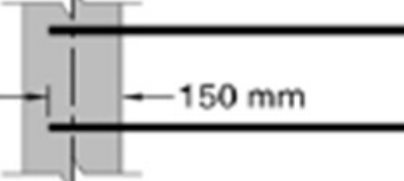
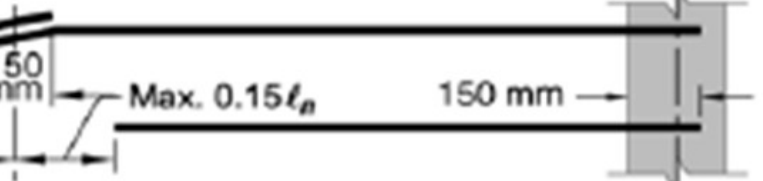
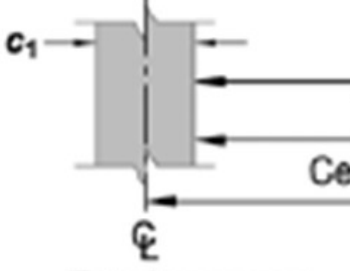
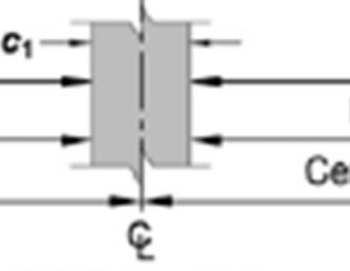
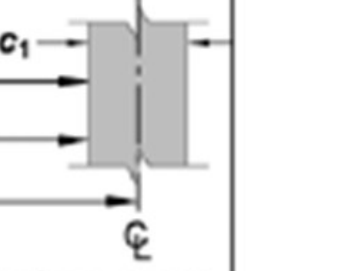
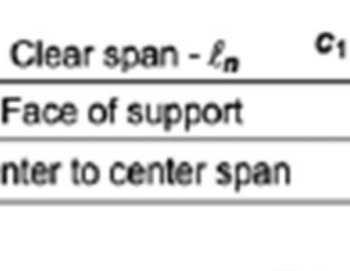
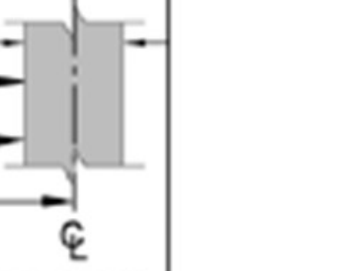

STRIP	LOCATION	MINIMUM - $A_s$ AT SECTION	WITHOUT DROP PANELS	WITH DROP PANELS
COLUMN STRIP	TOP	50% REMAINDER		
	BOTTOM	100%		
MIDDLE STRIP	TOP	100%		
	BOTTOM	50% REMAINDER		
			  	  
			<p>Exterior support (No slab continuity)</p> <p>Interior support (Continuity provided)</p> <p>Exterior support (No slab continuity)</p>	<p>Exterior support (No slab continuity)</p> <p>Interior support (Continuity provided)</p> <p>Exterior support (No slab continuity)</p>

Fig. 13.3.8—Minimum extensions for reinforcement in slabs without beams. (See 12.11.1 for reinforcement extension into supports).

**13.6.4.1** — Column strips shall be proportioned to resist the following portions in percent of interior negative factored moments:

$l_2/l_1$	0.5	1.0	2.0
$(\alpha_f l_2/l_1) = 0$	75	75	75
$(\alpha_f l_2/l_1) \geq 1.0$	90	75	45

**13.6.4.4** — Column strips shall be proportioned to resist the following portions in percent of positive factored moments:

$l_2/l_1$	0.5	1.0	2.0
$(\alpha_f l_2/l_1) = 0$	60	60	60
$(\alpha_f l_2/l_1) \geq 1.0$	90	75	45

**13.6.5.1** — Beams between supports shall be proportioned to resist 85 percent of column strip moments if  $\alpha_f l_2/l_1$  is equal to or greater than 1.0.

Linear interpolations shall be made between values shown.

**End of Appendices**

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