

Q: Given the following signal

$$m(t) = 0.75 \cos(2000\pi t)$$

is used to FM modulate a carrier

$$s(t) = 50 \cos(2\pi 10^7 t + 3 \sin(2000\pi t))$$

FM $2\pi(1000)t$

find:

① the peak freq deviation from the carrier and freq sensitivity?

$$f_i = f_c + \Delta f m(t) = \frac{1}{2\pi} \frac{d\phi_i}{dt}$$

$$f_i = 10^7 + 3000 \cos(2\pi(1000)t)$$

$$\Delta f = 3000 \text{ Hz} = 3 \text{ kHz}$$

$$\Delta f = k_f A_m$$

$$3 \text{ kHz} = k_f (0.75) \Rightarrow k_f = 4000 \text{ Hz} = 4 \text{ kHz}$$

$$\beta = \frac{\Delta f}{f_m} = \frac{3 \text{ kHz}}{1 \text{ kHz}} = 3$$

② Compute the total power of $s(t)$?

$$P_{av} = \frac{1}{2} A_c^2 = \frac{1}{2} (50)^2 = 1250 \text{ W}$$

③ find the power of the signal at 10 MHz given that

$$J_0(1) = 0.76, J_0(2) = 0.22, J_0(3) = -0.26$$

$$J_0(4) = -0.39?$$

$$P_{10 \text{ MHz}} = \frac{J_0^2(3)}{\sum_{n=-\infty}^{\infty} J_n^2(3)} P_{av} = \frac{(-0.26)^2}{1} \cdot 1250 = 84.5 \text{ W}$$

$$P_{10 \text{ MHz}} \% = \frac{84.5}{1250} =$$

④ find the approx B_T

$$B_T = 2(3 \text{ kHz}) + 2(1 \text{ kHz}) = 8000 \text{ Hz}$$

Q: A periodic square wave with 50% duty cycle frequency modulates an FM transmitter such that the peak angle deviation = δ . Assume the square wave has a peak amplitude of 5V and period of 10ms.



① find peak frequency deviation?

$$\Delta f = B f_m = \delta \left(\frac{1}{10 \times 10^{-3}} \right) = 600 \text{ Hz}$$

② find frequency sensitivity?

$$k_f = \frac{\Delta f}{A_m} = \frac{600}{5} = 120$$

③ sketch the spectrum give $f_c = 30$ MHz and using Bessel table?

$$J_0(\delta) = 0.1506, J_1(\delta) = -0.2767$$

$$J_2(\delta) = -0.2499, J_3(\delta) = 0.1148$$

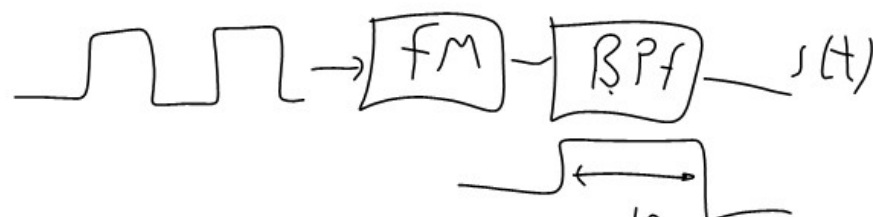
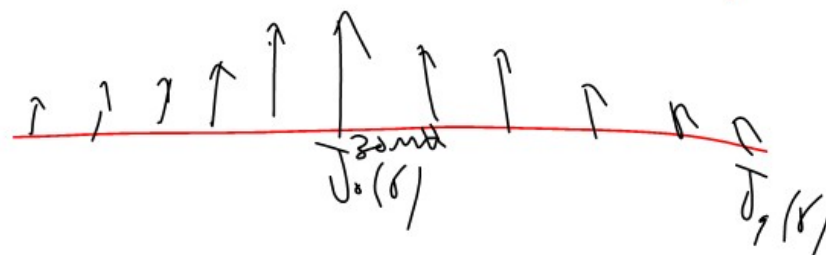
$$J_4(\delta) = 0.3627, J_5(\delta) = 0.2459$$

$$J_6(\delta) = 0.2418, |J_7(\delta)| > 0.01$$

$$|J_8(\delta)| > 0.01$$

$$|J_9(\delta)| > 0.01 \checkmark$$

$$J_{10}(\delta) = 0.007 < 0.01 \times$$



$$B_T = 2n_m f_m = 2(1)(100) = 200 \text{ kHz}$$