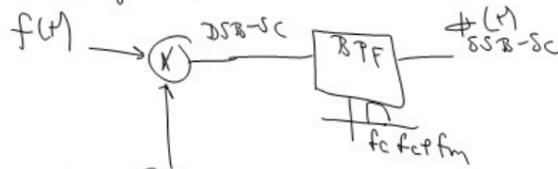


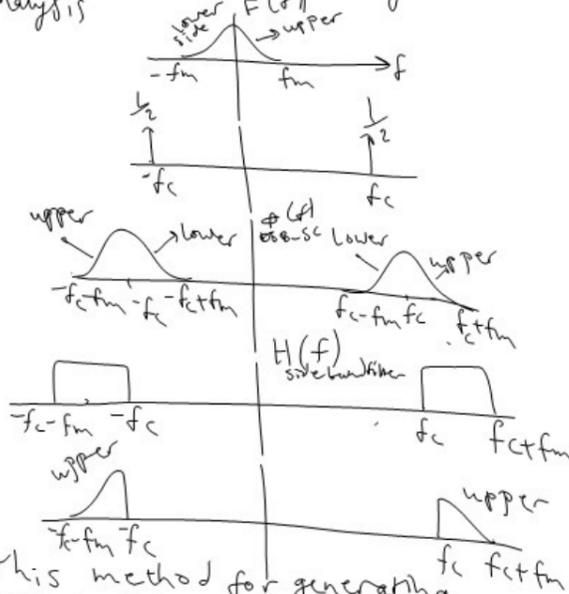
5.4.1 Generation of SSB-SC

* There are two ways to generate a single side band signals

1. Generate a double side band signal followed by a side band filter as shown by the following block diagram



* The principle of operation of this method is best illustrated by spectrum analysis

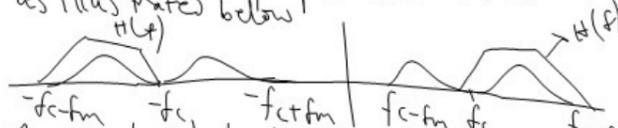


* This method for generating SSB modulation is suitable for signals that does not contain frequency down to zero because the side band filter is not ideal

* for example voice signals have frequency spectrum as the one shown below



* for this of signals If the filter is not ideal we can still have a proper SSB-modulation as illustrated below



* The single side band signal can be described mathematically by the following equations

$$\phi_{SSB-SC}(t) = f(t) e^{j\omega_c t}$$

$$\text{If } f(t) = e^{j\omega_m t} \text{ then } \phi(t) = e^{j(\omega_c + \omega_m)t}$$

by taking the real part of $\phi(t)$ we have the following equation

$$\text{Real} \{ e^{j(\omega_c + \omega_m)t} \} = \cos \omega_m t \cos \omega_c t - \sin \omega_m t \sin \omega_c t$$

* The above mentioned equation represents an upper single side band modulated signal

* for lower side band modulated signal, we have

$$f(t) = e^{-j\omega_m t}$$

* The resulting expression for the lower side band modulated signal is given by

$$\text{Real} \{ e^{j(\omega_c - \omega_m)t} \} = \cos \omega_m t \cos \omega_c t + \sin \omega_m t \sin \omega_c t$$

* In general the expression for single side band signal is given by

$$\phi_{SSB-SC}(t) = f(t) \cos \omega_c t \pm \hat{f}(t) \sin \omega_c t$$

where $\hat{f}(t)$ is a 90° phase shifted version of $f(t)$

* note that $\hat{f}(t)$ can be obtained from $f(t)$ by using Hilbert transform

* Hilbert transform can be expressed mathematically

by

$$\hat{f}(t) = f(t) \otimes \frac{1}{\pi t}$$

time domain

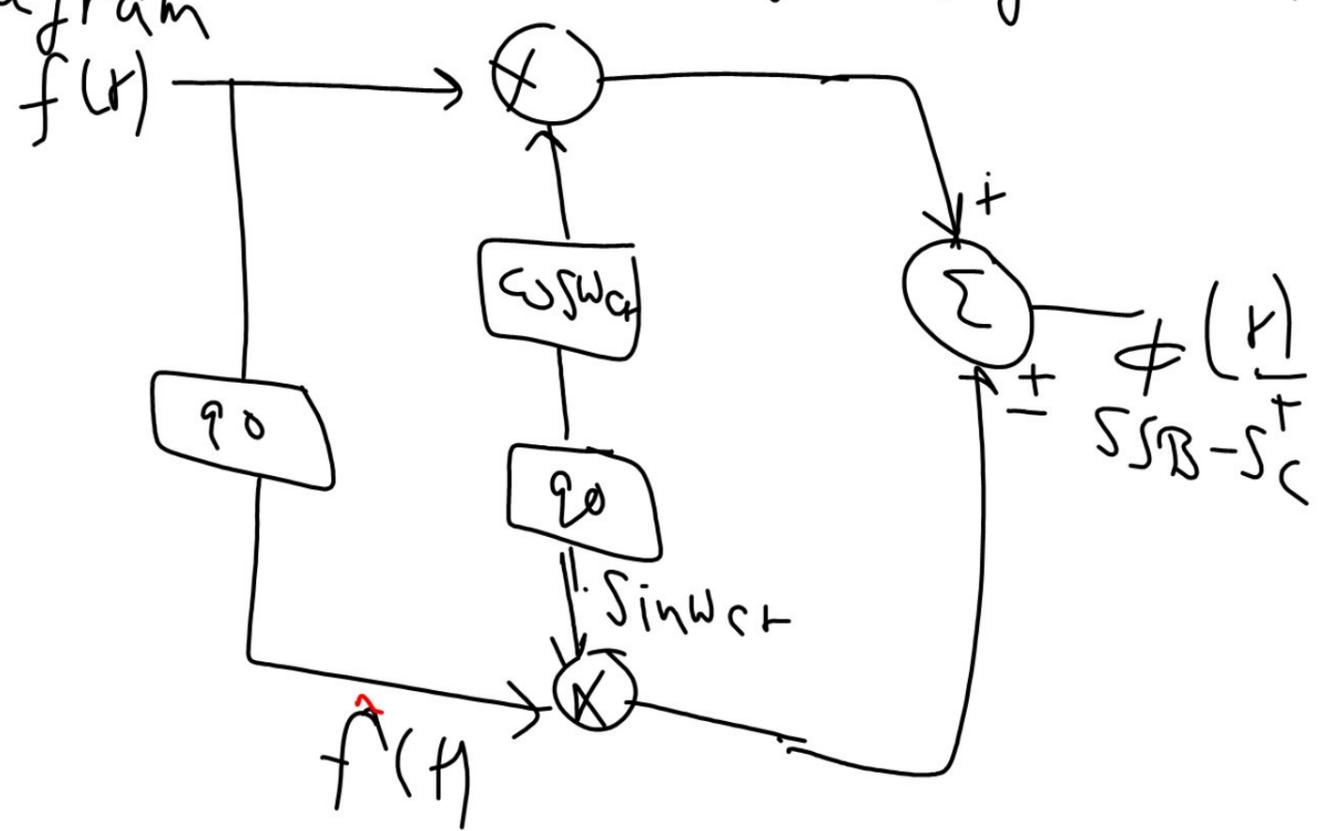
or

$$\hat{F}(\omega) = -j F(\omega) \text{Sgn}(\omega)$$

frequency domain

$$\text{Sgn}(\omega) = \begin{cases} 1 & \omega > 0 \\ -1 & \omega < 0 \end{cases}$$

* The SSB equation $\phi_{SSB}(t) = f(t) \cos \omega_c t \pm \hat{f}(t) \sin \omega_c t$ can be implemented by using the following block diagram



Ex A DSB-LC is generated using a 1 kHz carrier and the input signal $f(t) = \cos 200\pi t$. The modulation index $m = 80\%$.

The lower side band is attenuated using a side band filter. Find an expression for the resulting single side band modulated signal. If it develops 0.58 W at a cross section

Solution

$$\begin{aligned}\phi_{\text{DSB-LC}}(t) &= A(1 + m \cos \omega_m t) \cos \omega_c t \\ &= A \cos \omega_c t + mA \cos \omega_m t \cos \omega_c t \\ \phi_{\text{SSB-LC}}(t) &= A \cos \omega_c t + mA \frac{1}{2} \cos(\omega_c - \omega_m)t + mA \frac{1}{2} \cos(\omega_m + \omega_c)t \\ &= A \cos \omega_c t + \frac{mA}{2} \cos(\omega_c + \omega_m)t\end{aligned}$$

The power is given by

$$0.58 = \frac{A^2}{2} + \frac{m^2 A^2}{4}$$

$$0.58 = \frac{A^2}{2} \left[1 + \frac{(0.8)^2}{4} \right] \Rightarrow A = 1$$

$$\phi_{\text{SSB-LC}}(t) = \cos 2000\pi t + 0.4 \cos 2200\pi t$$